# t220_member_1 <br> (TMSbpeuuoF4J6sEA8UUvTFSgz3bvPvcHB3N) 

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Let $v 1 \_$membered $: ~ \iota \Rightarrow 0$ be given. Let $v 1 \_x c m p l x \_0: \iota \Rightarrow 0$ be given. Let $k 6 \_n u m b e r s: \iota$ be given. Let $k 25 \_$member_ $1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 5$ _xboole_0 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 7$ _member_1 : $\iota \Rightarrow \iota$ be given. Let k23_member_1: $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 1_{\_}$tarski : $\iota \Rightarrow \iota$ be given. Let $v 1 \_x$ boole_0 $: \iota \Rightarrow o$ be given. Let $k 15 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 13 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 7 \_m e m b e r \_1\right.\right.$
$\left(k 5 \_x b o o l e \_0 X 0 X 1\right)=k 5 \_x b o o l e \_0\left(k 7 \_m e m b e r \_1 X 0\right)\left(k 7 \_m e m b e r \_1\right.$ X1)))

Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 \quad X 2\right) \Rightarrow\left(\left(X 2 \neq k 6 \_n u m b e r s\right) \Rightarrow\left(k 23 \_m e m b e r \_1\left(k 5 \_x b o o l e \_0\right.\right.\right.$
$\left.\left.\left.\left.X 0 X 1) X 2=k 5 \_x b o o l e \_0\left(k 23 \_m e m b e r \_1 X 0 X 2\right)\left(k 23 \_m e m b e r \_1 X 1 X 2\right)\right)\right)\right)\right)$
Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 1 \_t a r s k i X 0\right)\right) \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d X 0\right) \wedge\left(v 1 \_m e m b e r e d ~ X 1\right)\right) \Rightarrow(  \tag{4}\\
\left.v 1 \_m e m b e r e d\left(k 5 \_x b o o l e \_0 X 0 X 1\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{align*}
& \forall X 0 .\left(\left(\neg v 1 \_x b o o l e \_0 X 0\right) \wedge\left(v 1 \_m e m b e r e d \quad X 0\right)\right) \Rightarrow\left(\left(\neg v 1 \_x b o o l e \_0\right.\right. \\
& \left.\left.\left(k 7 \_m e m b e r \_1 X 0\right)\right) \wedge\left(v 1 \_m e m b e r e d\left(k 7 \_m e m b e r \_1 X 0\right)\right)\right) \tag{5}
\end{align*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_x b o o l e \_0 X 0\right) \Rightarrow\left(\left(v 1 \_x b o o l e \_0\left(k 7 \_m e m b e r \_1 X 0\right)\right) \wedge\right. \\
\left.\left(v 1 \_m e m b e r e d\left(k 7 \_m e m b e r \_1 X 0\right)\right)\right) \tag{6}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 25 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 15 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right) \tag{7}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 23 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 13 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right) \tag{8}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d X 1\right) \Rightarrow\left(k 15 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 13 \_m e m b e r \_1 X 0\left(k 7 \_m e m b e r \_1 X 1\right)\right)\right) \tag{9}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . k 5 \_x b o o l e \_0 X 0 X 1=k 5 \_x b o o l e \_0 X 1 X 0 \tag{10}
\end{equation*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(\left(X 2 \neq k 6 \_n u m b e r s\right) \Rightarrow\left(k 25 \_m e m b e r \_1\right.\right.$ ( $k 5$ _xboole_0
$\left.\left.\left.\left.X 0 X 1) X 2=k 5 \_x b o o l e \_0\left(k 25 \_m e m b e r \_1 X 0 X 2\right)\left(k 25 \_m e m b e r \_1 X 1 X 2\right)\right)\right)\right)\right)$

