# t222_member_1 <br> (TMSAM93KJ19vJPCswfHKUaX4HpfuAp18iqg) 

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Let $v 1_{\_}$membered : $\iota \Rightarrow O$ be given. Let $v 1 \_x c m p l x \_0: \iota \Rightarrow O$ be given. Let r1_tarski : $\iota \Rightarrow \iota \Rightarrow 0$ be given. Let $k 25$ _member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 4_{-}$binop_2 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 11 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 1 \_t a r s k i: \iota \Rightarrow \iota$ be given. Let $k 15 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 6 \_x c m p l x \_0$ : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 11 \_m e m b e r \_1\right.\right.$
$\left.\left.\left(k 1 \_t a r s k i ~ X 0\right)\left(k 1 \_t a r s k i ~ X 1\right)=k 1 \_t a r s k i\left(k 4 \_b i n o p \_2 X 0 X 1\right)\right)\right)$
Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d X 1\right) \Rightarrow(\forall X 2 \text {. }\right. \\
\left(v 1 \_m e m b e r e d X 2\right) \Rightarrow\left(r 1 \_ \text { tarski } \left(k 15 \_m e m b e r \_1\left(k 11 \_m e m b e r \_1 X 0 X 1\right)\right.\right. \\
\left.\left.\left.X 2)\left(k 11 \_m e m b e r \_1\left(k 15 \_m e m b e r \_1 X 0 X 2\right)\left(k 15 \_m e m b e r \_1 X 1 X 2\right)\right)\right)\right)\right) \tag{2}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_x c m p l x \_0 X 0\right) \wedge\left(v 1 \_x c m p l x \_0 X 1\right)\right) \Rightarrow( \\
\left.k 4 \_b i n o p \_2 X 0 X 1=k 6 \_x c m p l x \_0 X 0 X 1\right) \tag{3}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 1 \_t a r s k i X 0\right)\right) \tag{4}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_x c m p l x \_0 X 0\right) \wedge\left(v 1 \_x c m p l x \_0 X 1\right)\right) \Rightarrow( \\
\left.v 1 \_x c m p l x \_0\left(k 6 \_x c m p l x \_0 X 0 X 1\right)\right) \tag{5}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 25 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 15 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right) \tag{6}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 \quad X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 \quad X 2\right) \Rightarrow\left(r 1 \_t a r s k i\left(k 25 \_m e m b e r \_1 X 0\left(k 4 \_b i n o p \_2 X 1 X 2\right)\right)\right.$
(k11_member_1 (k25_member_1 X0 X1) (k25_member_1 X0 X2)))))

