

# t22\_hausdorf (TMWUhbDtdjkBTwSkGWK- meAKR6QHn4ihqbWT)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v6\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v7\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v8\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v9\_metric\_1 : \iota \Rightarrow o$  be given. Let  $l1\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_pcomps\_1 : \iota \Rightarrow \iota$  be given. Let  $v2\_compts\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_weierstr : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_weierstr : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_weierstr : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_metric\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $k2\_metric\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v2\_valued\_0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_topc : \iota \Rightarrow o$  be given. Let  $k3\_topmetr : \iota$  be given. Let  $v3\_topmetr : \iota \Rightarrow o$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v3\_membered : \iota \Rightarrow o$  be given. Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_numbers : \iota$  be given. Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $v2\_membered : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v6\_metric\_1 X0) \wedge ((v7\_metric\_1 \\
& X0) \wedge ((v8\_metric\_1 X0) \wedge ((v9\_metric\_1 X0) \wedge (l1\_metric\_1 X0)))))) \Rightarrow \\
& (\forall X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 (k3\_pcomps\_1 \\
& X0)))) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 \\
& (k3\_pcomps\_1 X0)))) \Rightarrow (((v2\_compts\_1 X1 (k3\_pcomps\_1 X0)) \wedge (v2\_compts\_1 \\
& X2 (k3\_pcomps\_1 X0))) \Rightarrow (\forall X3. (m1\_subset\_1 X3 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X4. (m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (((X3 \in X1) \wedge \\
& (X4 \in X2)) \Rightarrow ((r1\_xxreal\_0 (k7\_weierstr X0 X1 X2) (k4\_metric\_1 X0 \\
& X3 X4)) \wedge (r1\_xxreal\_0 (k4\_metric\_1 X0 X3 X4) (k10\_weierstr X0 X1 \\
& X2))))))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0. (v1\_xreal\_0 X0) \Rightarrow (\forall X1. (v1\_xreal\_0 X1) \Rightarrow (\forall X2. \\
& (v1\_xreal\_0 X2) \Rightarrow (((r1\_xxreal\_0 X0 X1) \wedge (r1\_xxreal\_0 X1 X2)) \Rightarrow \\
& (r1\_xxreal\_0 X0 X2))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v6\_metric\_1 X0) \wedge ((v7\_metric\_1 \\ & X0) \wedge ((v8\_metric\_1 X0) \wedge ((v9\_metric\_1 X0) \wedge (l1\_metric\_1 X0)))))) \Rightarrow \\ & (\forall X1.((\neg v1\_xboole\_0 X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (u1\_struct\_0 (k3\_pcomps\_1 X0)))))) \Rightarrow (\forall X2.(m1\_subset\_1 \\ & X2 (u1\_struct\_0 X0)) \Rightarrow (\exists X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\ & X0)) \wedge ((X3 \in X1) \wedge (r1\_xreal\_0 (k1\_funct\_1 (k6\_weierstr X0 X1) X2) \\ & (k4\_metric\_1 X0 X3 X2)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((v8\_metric\_1 X0) \wedge (l1\_metric\_1 \\ & X0)) \wedge ((m1\_subset\_1 X1 (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 X2 (u1\_struct\_0 \\ & X0)))) \Rightarrow (k4\_metric\_1 X0 X1 X2 = k2\_metric\_1 X0 X1 X2) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v2\_valued\_0 \\ & X0))) \Rightarrow (v1\_xreal\_0 (k1\_funct\_1 X0 X1)) \end{aligned} \quad (5)$$

Assume the following.

$$(v2\_pre\_topc k3\_topmetr) \wedge (v3\_topmetr k3\_topmetr) \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((v3\_topmetr X0) \wedge (l1\_struct\_0 X0)) \Rightarrow (v3\_membered \\ & (u1\_struct\_0 X0)) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0. (l1\_pre\_topc X0) \Rightarrow (l1\_struct\_0 X0) \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge ((v6\_metric\_1 X0) \wedge \\ & ((v7\_metric\_1 X0) \wedge ((v8\_metric\_1 X0) \wedge ((v9\_metric\_1 X0) \wedge (l1\_metric\_1 \\ & X0)))))) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 (k3\_pcomps\_1 \\ & X0)))))) \Rightarrow ((v1\_funct\_1 (k6\_weierstr X0 X1)) \wedge ((v1\_funct\_2 (k6\_weierstr \\ & X0 X1) (u1\_struct\_0 (k3\_pcomps\_1 X0)) (u1\_struct\_0 k3\_topmetr)) \wedge \\ & (m1\_subset\_1 (k6\_weierstr X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 \\ & (k3\_pcomps\_1 X0)) (u1\_struct\_0 k3\_topmetr)))))) \end{aligned} \quad (9)$$

Assume the following.

$$(v2\_pre\_topc k3\_topmetr) \wedge (l1\_pre\_topc k3\_topmetr) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(((l1\_metric\_1 X0)\wedge((m1\_subset\_1 X1 (u1\_struct\_0 X0))\wedge(m1\_subset\_1 X2 (u1\_struct\_0 X0))))\Rightarrow(m1\_subset\_1 (k2\_metric\_1 X0 X1 X2) k1\_numbers)) \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0)\wedge((v6\_metric\_1 X0)\wedge((v7\_metric\_1 X0)\wedge((v8\_metric\_1 X0)\wedge((v9\_metric\_1 X0)\wedge(l1\_metric\_1 X0))))))\wedge((m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 (k3\_pcomps\_1 X0))))\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 (k3\_pcomps\_1 X0))))))\Rightarrow(m1\_subset\_1 (k10\_weierstr X0 X1 X2) k1\_numbers)) \quad (12)$$

Assume the following.

$$\forall X0.(v1\_xreal\_0 X0)\Rightarrow(v1\_xxreal\_0 X0) \quad (13)$$

Assume the following.

$$\forall X0.(v3\_membered X0)\Rightarrow(v2\_membered X0) \quad (14)$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k1\_numbers)\Rightarrow(v1\_xreal\_0 X0) \quad (15)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))\Rightarrow(v1\_relat\_1 X2) \quad (16)$$

Assume the following.

$$\forall X0.\forall X1.(v2\_membered X1)\Rightarrow(\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))\Rightarrow(v2\_valued\_0 X2)) \quad (17)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(((\neg v2\_struct\_0 X0)\wedge((v6\_metric\_1 X0)\wedge((v7\_metric\_1 X0)\wedge((v8\_metric\_1 X0)\wedge((v9\_metric\_1 X0)\wedge(l1\_metric\_1 X0))))))\Rightarrow \\ & (\forall X1.(((\neg v1\_xboole\_0 X1)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 (k3\_pcomps\_1 X0))))))\Rightarrow(\forall X2.(((\neg v1\_xboole\_0 X2)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 (k3\_pcomps\_1 X0))))))\Rightarrow \\ & (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0))\Rightarrow(((v2\_compts\_1 X1 (k3\_pcomps\_1 X0))\wedge((v2\_compts\_1 X2 (k3\_pcomps\_1 X0))\wedge(X3 \in X2)))\Rightarrow(r1\_xxreal\_0 (k1\_funct\_1 (k6\_weierstr X0 X1) X3) (k10\_weierstr X0 X1 X2)))))) \end{aligned}$$