

t22\_matroid0  
(TMGqRK5owVrWhQXbTyGj5W3QjhK1ijzen7d)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v3\_pencil\_1 : \iota \Rightarrow o$  be given. Let  $v1\_matroid0 : \iota \Rightarrow o$  be given. Let  $v2\_matroid0 : \iota \Rightarrow o$  be given. Let  $v4\_matroid0 : \iota \Rightarrow o$  be given. Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $m1\_matroid0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v3\_pre\_topc : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_matroid0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $k2\_struct\_0 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0. (&(\neg v2\_struct\_0 X0) \wedge (\neg v3\_pencil\_1 X0) \wedge ((v1\_matroid0 \\ &X0) \wedge ((v4\_matroid0 X0) \wedge (l1\_pre\_topc X0)))) \Rightarrow (((\neg v2\_struct\_0 \\ &X0) \wedge ((\neg v3\_pencil\_1 X0) \wedge ((v1\_matroid0 X0) \wedge ((v2\_matroid0 X0) \wedge \\ &(l1\_pre\_topc X0)))))) \Leftrightarrow (\forall X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ &(u1\_struct\_0 X0))) \Rightarrow (\forall X2. ((v3\_pre\_topc X2 X0) \wedge (m1\_subset\_1 \\ &X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow (\forall X3. ((v3\_pre\_topc \\ &X3 X0) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow (((r1\_matroid0 \\ &X0 X2 X1) \wedge (r1\_matroid0 X0 X3 X1)) \Rightarrow (k5\_card\_1 X2 = k5\_card\_1 X3)))))) \end{aligned} \quad (1)$$

Assume the following.

$$\forall X0. ((\neg v3\_pencil\_1 X0) \wedge ((v4\_matroid0 X0) \wedge (l1\_pre\_topc X0))) \Rightarrow (\forall X1. (m1\_matroid0 X1 X0) \Rightarrow ((v3\_pre\_topc X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))))) \quad (2)$$

Assume the following.

$$\forall X0. (l1\_pre\_topc X0) \Rightarrow (l1\_struct\_0 X0) \quad (3)$$

Assume the following.

$$\forall X0. (l1\_struct\_0 X0) \Rightarrow (m1\_subset\_1 (k2\_struct\_0 X0) (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \quad (4)$$

Assume the following.

$$\forall X0. ((\neg v3\_pencil\_1 X0) \wedge ((v4\_matroid0 X0) \wedge (l1\_pre\_topc X0))) \Rightarrow (\forall X1. ((v3\_pre\_topc X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow ((m1\_matroid0 X1 X0) \Leftrightarrow (r1\_matroid0 X0 X1 (k2\_struct\_0 X0)))) \quad (5)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v3\_pencil\_1 X0) \wedge ((v1\_matroid0 \\ & X0) \wedge ((v2\_matroid0 X0) \wedge ((v4\_matroid0 X0) \wedge (l1\_pre\_topc X0)))))) \Rightarrow \\ & (\forall X1.(m1\_matroid0 X1 X0) \Rightarrow (\forall X2.(m1\_matroid0 X2 X0) \Rightarrow \\ & (k5\_card\_1 X1 = k5\_card\_1 X2))) \end{aligned}$$