

t22\_vectsp10  
(TMF7onc2cLNVAmy2sqJmqkaxm5sgB9VizT2)

October 27, 2020

Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $v4\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v5\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v8\_vectsp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v9\_vectsp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v10\_vectsp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v11\_vectsp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_vectsp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_vectsp\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k6\_vectsp10 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m2\_vectsp\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_vectsp\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $v7\_vectsp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_vectsp10 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_algstr\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_vectsp10 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k4\_vectsp10 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_vectsp\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_vectsp10 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. (m1\_subset\_1 X0 X1) \Rightarrow ((v1\_xboole\_0 X1) \vee (X0 \in X1)) \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 \\ & X0) \wedge ((v3\_group\_1 X0) \wedge ((v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge \\ & (v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 \\ & X0)))))))) \wedge (((\neg v2\_struct\_0 X1) \wedge ((v13\_algstr\_0 X1) \wedge ((v8\_vectsp\_1 \\ & X1 X0) \wedge ((v9\_vectsp\_1 X1 X0) \wedge ((v10\_vectsp\_1 X1 X0) \wedge ((v11\_vectsp\_1 \\ & X1 X0) \wedge ((v2\_rlvect\_1 X1) \wedge ((v3\_rlvect\_1 X1) \wedge ((v4\_rlvect\_1 X1) \wedge \\ & (l1\_vectsp\_1 X1 X0)))))))))) \wedge (m1\_vectsp\_4 X2 X0 X1)) \Rightarrow (\forall X3. \\ & (m2\_vectsp\_4 X3 X0 X1 X2) \Rightarrow (m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X1)))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge (v13\_algstr\_0 \\
& X0) \wedge (v2\_rlvect\_1 X0) \wedge (v3\_rlvect\_1 X0) \wedge (v4\_rlvect\_1 X0) \wedge \\
& ((v3\_group\_1 X0) \wedge (v4\_vectsp\_1 X0) \wedge (v5\_vectsp\_1 X0) \wedge (l6\_algstr\_0 \\
& X0)))))) \wedge (((\neg v2\_struct\_0 X1) \wedge (v13\_algstr\_0 X1) \wedge (v2\_rlvect\_1 \\
& X1) \wedge (v3\_rlvect\_1 X1) \wedge (v4\_rlvect\_1 X1) \wedge (v8\_vectsp\_1 X1 X0) \wedge \\
& ((v9\_vectsp\_1 X1 X0) \wedge (v10\_vectsp\_1 X1 X0) \wedge (v11\_vectsp\_1 X1 \\
& X0) \wedge (l1\_vectsp\_1 X1 X0)))))) \wedge (m1\_vectsp\_4 X2 X0 X1)) \Rightarrow (( \\
& \neg v2\_struct\_0 (k6\_vectsp10 X0 X1 X2)) \wedge (v13\_algstr\_0 (k6\_vectsp10 \\
& X0 X1 X2)) \wedge (v2\_rlvect\_1 (k6\_vectsp10 X0 X1 X2)) \wedge (v3\_rlvect\_1 \\
& (k6\_vectsp10 X0 X1 X2)) \wedge (v4\_rlvect\_1 (k6\_vectsp10 X0 X1 X2)) \wedge \\
& (v7\_vectsp\_1 (k6\_vectsp10 X0 X1 X2) X0) \wedge (v8\_vectsp\_1 (k6\_vectsp10 \\
& X0 X1 X2) X0) \wedge (v9\_vectsp\_1 (k6\_vectsp10 X0 X1 X2) X0) \wedge (v10\_vectsp\_1 \\
& (k6\_vectsp10 X0 X1 X2) X0) \wedge (v11\_vectsp\_1 (k6\_vectsp10 X0 X1 X2) \\
& X0) \wedge (l1\_vectsp\_1 (k6\_vectsp10 X0 X1 X2) X0))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge (v13\_algstr\_0 \\
& X0) \wedge (v2\_rlvect\_1 X0) \wedge (v3\_rlvect\_1 X0) \wedge (v4\_rlvect\_1 X0) \wedge \\
& ((v3\_group\_1 X0) \wedge (v4\_vectsp\_1 X0) \wedge (v5\_vectsp\_1 X0) \wedge (l6\_algstr\_0 \\
& X0)))))) \wedge (((\neg v2\_struct\_0 X1) \wedge (v13\_algstr\_0 X1) \wedge (v2\_rlvect\_1 \\
& X1) \wedge (v3\_rlvect\_1 X1) \wedge (v4\_rlvect\_1 X1) \wedge (v8\_vectsp\_1 X1 X0) \wedge \\
& ((v9\_vectsp\_1 X1 X0) \wedge (v10\_vectsp\_1 X1 X0) \wedge (v11\_vectsp\_1 X1 \\
& X0) \wedge (l1\_vectsp\_1 X1 X0)))))) \wedge (m1\_vectsp\_4 X2 X0 X1)) \Rightarrow (( \\
& \neg v1\_xboole\_0 (k2\_vectsp10 X0 X1 X2)) \wedge (m1\_subset\_1 (k2\_vectsp10 \\
& X0 X1 X2) (k1\_zfmisc\_1 (k1\_zfmisc\_1 (u1\_struct\_0 X1))))))
\end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0. ((\neg v2\_struct\_0 X0) \wedge (v13\_algstr\_0 X0) \wedge (v3\_group\_1 \\
& X0) \wedge (v4\_vectsp\_1 X0) \wedge (v5\_vectsp\_1 X0) \wedge (v2\_rlvect\_1 X0) \wedge \\
& ((v3\_rlvect\_1 X0) \wedge (v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))) \Rightarrow \\
& (\forall X1. ((\neg v2\_struct\_0 X1) \wedge (v13\_algstr\_0 X1) \wedge (v8\_vectsp\_1 \\
& X1 X0) \wedge (v9\_vectsp\_1 X1 X0) \wedge (v10\_vectsp\_1 X1 X0) \wedge (v11\_vectsp\_1 \\
& X1 X0) \wedge (v2\_rlvect\_1 X1) \wedge (v3\_rlvect\_1 X1) \wedge (v4\_rlvect\_1 X1) \wedge \\
& (l1\_vectsp\_1 X1 X0)))) \Rightarrow (\forall X2. (m1\_vectsp\_4 X2 X0 X1)) \Rightarrow \\
& (\forall X3. (m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X1))) \Rightarrow \\
& ((m2\_vectsp\_4 X3 X0 X1 X2) \Leftrightarrow (\exists X4. (m1\_subset\_1 X4 (u1\_struct\_0 \\
& X1)) \wedge (X3 = k3\_vectsp\_4 X0 X1 X4 X2))))))
\end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v3\_group\_1 X0) \wedge \\
& (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge (l6\_algstr\_0 X0))))))))) \Rightarrow \\
& (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((v13\_algstr\_0 X1) \wedge ((v2\_rlvect\_1 \\
& X1) \wedge ((v3\_rlvect\_1 X1) \wedge ((v4\_rlvect\_1 X1) \wedge ((v8\_vectsp\_1 X1 X0) \wedge \\
& ((v9\_vectsp\_1 X1 X0) \wedge ((v10\_vectsp\_1 X1 X0) \wedge ((v11\_vectsp\_1 X1 \\
& X0) \wedge (l1\_vectsp\_1 X1 X0))))))))) \Rightarrow (\forall X2.(m1\_vectsp\_4 X2 \\
& X0 X1) \Rightarrow (\forall X3.((\neg v2\_struct\_0 X3) \wedge ((v13\_algstr\_0 X3) \wedge (( \\
& v2\_rlvect\_1 X3) \wedge ((v3\_rlvect\_1 X3) \wedge ((v4\_rlvect\_1 X3) \wedge ((v7\_vectsp\_1 \\
& X3 X0) \wedge ((v8\_vectsp\_1 X3 X0) \wedge ((v9\_vectsp\_1 X3 X0) \wedge ((v10\_vectsp\_1 \\
& X3 X0) \wedge ((v11\_vectsp\_1 X3 X0) \wedge (l1\_vectsp\_1 X3 X0))))))))) \Rightarrow ( \\
& (X3 = k6\_vectsp10 X0 X1 X2) \Leftrightarrow ((u1\_struct\_0 X3 = k2\_vectsp10 X0 X1 X2) \wedge \\
& ((r1\_funct\_2 (k2\_zfmisc\_1 (u1\_struct\_0 X3) (u1\_struct\_0 X3)) \\
& (u1\_struct\_0 X3) (k2\_zfmisc\_1 (k2\_vectsp10 X0 X1 X2) (k2\_vectsp10 \\
& X0 X1 X2)) (k2\_vectsp10 X0 X1 X2) (u1\_algstr\_0 X3) (k3\_vectsp10 X0 \\
& X1 X2)) \wedge ((k4\_struct\_0 X3 = k4\_vectsp10 X0 X1 X2) \wedge (r1\_funct\_2 (k2\_zfmisc\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X3)) (u1\_struct\_0 X3) (k2\_zfmisc\_1 \\
& (u1\_struct\_0 X0) (k2\_vectsp10 X0 X1 X2)) (k2\_vectsp10 X0 X1 X2) ( \\
& u1\_vectsp\_1 X0 X3) (k5\_vectsp10 X0 X1 X2))))))))) \tag{6}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v3\_group\_1 X0) \wedge \\
& (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge (l6\_algstr\_0 X0))))))))) \Rightarrow \\
& (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((v13\_algstr\_0 X1) \wedge ((v2\_rlvect\_1 \\
& X1) \wedge ((v3\_rlvect\_1 X1) \wedge ((v4\_rlvect\_1 X1) \wedge ((v8\_vectsp\_1 X1 X0) \wedge \\
& ((v9\_vectsp\_1 X1 X0) \wedge ((v10\_vectsp\_1 X1 X0) \wedge ((v11\_vectsp\_1 X1 \\
& X0) \wedge (l1\_vectsp\_1 X1 X0))))))))) \Rightarrow (\forall X2.(m1\_vectsp\_4 X2 \\
& X0 X1) \Rightarrow (k2\_vectsp10 X0 X1 X2 = \text{ReplSep} (\text{toset} (\lambda X3 : \iota.m2\_vectsp\_4 \\
& X3 X0 X1 X2)) (\lambda X3 : \iota.True) (\lambda X3 : \iota.X3)))) \tag{7}
\end{aligned}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v3\_group\_1 X0) \wedge \\
& (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge (l6\_algstr\_0 X0))))))))) \Rightarrow \\
& (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((v13\_algstr\_0 X1) \wedge ((v2\_rlvect\_1 \\
& X1) \wedge ((v3\_rlvect\_1 X1) \wedge ((v4\_rlvect\_1 X1) \wedge ((v8\_vectsp\_1 X1 X0) \wedge \\
& ((v9\_vectsp\_1 X1 X0) \wedge ((v10\_vectsp\_1 X1 X0) \wedge ((v11\_vectsp\_1 X1 \\
& X0) \wedge (l1\_vectsp\_1 X1 X0))))))))) \Rightarrow (\forall X2.(m1\_vectsp\_4 X2 \\
& X0 X1) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 (k6\_vectsp10 \\
& X0 X1 X2))) \Rightarrow ((m2\_vectsp\_4 X3 X0 X1 X2) \wedge (\exists X4.(m1\_subset\_1 \\
& X4 (u1\_struct\_0 X1)) \wedge (X3 = k3\_vectsp\_4 X0 X1 X4 X2))))))
\end{aligned}$$