# t234 member 1 <br> (TMGr7FNSoF2DddCFvAPMLUHT7LP3SCjNogN) 

October 27, 2020

Let $v 1 \_$membered $: ~ \iota \Rightarrow o$ be given. Let $v 1_{\_} x c m p l x \_0: ~ \iota \Rightarrow o$ be given. Let $k 27 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k9_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 7 \_$member_1 : $\iota \Rightarrow \iota$ be given. Let $k 1_{\_}$tarski : $\iota \Rightarrow \iota$ be given. Let $k 2 \_$_binop_2 : $\iota \Rightarrow \iota$ be given. Let $k 23 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 2 \_n u m b e r s: \iota$ be given. Let $m 1 \_$subset_1 : $\iota \Rightarrow \iota \Rightarrow o$ be given. Let $k 15 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 13$ _member_ $1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$
\begin{align*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow & \left(k 7 \_ \text {member_1 }\left(k 1^{\prime} \text { _tarski } X 0\right)=k 1 \_t a r s k i\right. \\
& \left.\left(k 2 \_b i n o p \_2 X 0\right)\right) \tag{1}
\end{align*}
$$

Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1\right.$. $\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(k 23 \_m e m b e r \_1\left(k 9 \_m e m b e r \_1 X 0 X 1\right) X 2=k 9 \_m e m b e r \_1\right.$ (k23_member_1 X0 X2) (k23_member_1 X1 X2))))

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d \quad\left(k 1 \_t a r s k i X 0\right)\right) \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d X 0\right) \wedge\left(v 1 \_m e m b e r e d ~ X 1\right)\right) \Rightarrow( \\
\left.v 1 \_m e m b e r e d\left(k 9 \_m e m b e r \_1 X 0 X 1\right)\right) \tag{4}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
v 1 \_m e m b e r e d ~ k 2 \_n u m b e r s \tag{5}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\left.\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(m 1 \_s u b s e t \_1 \text { (k2_binop_2 } X 0\right) k 2 \_n u m b e r s\right) \tag{6}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 27 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 15 \_m e m b e r \_1 X 0\left(k 1 \_t a r s k i X 1\right)\right)\right) \tag{7}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 23 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 13 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right) \tag{8}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 15 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 13 \_m e m b e r \_1 X 0\left(k 7 \_m e m b e r \_1 X 1\right)\right)\right) \tag{9}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d X 0\right) \wedge\left(v 1 \_m e m b e r e d ~ X 1\right)\right) \Rightarrow(  \tag{10}\\
\left.k 13 \_m e m b e r \_1 X 0 X 1=k 13 \_m e m b e r \_1 X 1 X 0\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(m 1 \_s u b s e t \_1 X 1 \quad X 0\right) \Rightarrow\right. \\
\left.\left(v 1 \_x c m p l x \_0 X 1\right)\right) \tag{11}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1\right.$. $\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2$.
(v1_xcmplx_0 X2) $\Rightarrow\left(k 27 \_m e m b e r \_1\right.$ (k9_member_1 X0 X1) X2 = k9_member_1 (k27_member_1 X0 X2) (k27_member_1 X1 X2))))

