

## t23\_circcomb2

(TMS18rjVcMGh3xVAz4VwMw97Ew6URiAFX97)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_msafree2 : \iota \Rightarrow o$  be given. Let  $l1\_msualg\_1 : \iota \Rightarrow o$  be given. Let  $r1\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_msafree2 : \iota \Rightarrow \iota$  be given. Let  $k3\_msafree2 : \iota \Rightarrow \iota$  be given. Let  $k2\_circcomb : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v4\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_msafree2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_circcomb : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_circcomb : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_card\_3 : \iota \Rightarrow \iota$  be given. Let  $u3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_circuit2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_facirc\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_msafree2 \\
 & \quad X0) \wedge (l1\_msualg\_1 X0)))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((\neg \\
 & \quad v11\_struct\_0 X1) \wedge ((v2\_msafree2 X1) \wedge (l1\_msualg\_1 X1)))) \Rightarrow (\forall X2. \\
 & \quad ((\neg v2\_struct\_0 X2) \wedge ((\neg v11\_struct\_0 X2) \wedge ((v2\_msafree2 X2) \wedge ( \\
 & \quad l1\_msualg\_1 X2)))) \Rightarrow ((X2 = k2\_circcomb X0 X1) \Rightarrow (\forall X3.((v4\_msualg\_1 \\
 & \quad X3 X0) \wedge ((v4\_msafree2 X3 X0) \wedge (l3\_msualg\_1 X3 X0)))) \Rightarrow (\forall X4. \\
 & \quad ((v4\_msualg\_1 X4 X1) \wedge ((v4\_msafree2 X4 X1) \wedge (l3\_msualg\_1 X4 X1)))) \Rightarrow \\
 & \quad (\forall X5.((v4\_msualg\_1 X5 X2) \wedge ((v4\_msafree2 X5 X2) \wedge (l3\_msualg\_1 \\
 & \quad X5 X2)))) \Rightarrow (((r2\_circcomb X0 X1 X3 X4) \wedge (X5 = k3\_circcomb X0 X1 X3 X4)) \Rightarrow \\
 & \quad (\forall X6.(m1\_subset\_1 X6 (k4\_card\_3 (u3\_msualg\_1 X2 X5)))) \Rightarrow \\
 & \quad ((v1\_circuit2 X6 X2 X5) \Rightarrow ((\forall X7.(m1\_subset\_1 X7 (k4\_card\_3 \\
 & \quad (u3\_msualg\_1 X0 X3)))) \Rightarrow ((X7 = k5\_relat\_1 X6 (u1\_struct\_0 X0)) \Rightarrow ( \\
 & \quad v1\_circuit2 X7 X0 X3))) \wedge (\forall X7.(m1\_subset\_1 X7 (k4\_card\_3 \\
 & \quad (u3\_msualg\_1 X1 X4)))) \Rightarrow ((X7 = k5\_relat\_1 X6 (u1\_struct\_0 X1)) \Rightarrow ( \\
 & \quad v1\_circuit2 X7 X1 X4))))))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_msafree2 \\
& \quad X0) \wedge (l1\_msualg\_1 X0)))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((\neg \\
& \quad v11\_struct\_0 X1) \wedge (v2\_msafree2 X1) \wedge (l1\_msualg\_1 X1)))) \Rightarrow (\forall X2. \\
& \quad ((\neg v2\_struct\_0 X2) \wedge ((\neg v11\_struct\_0 X2) \wedge ((v2\_msafree2 X2) \wedge ( \\
& \quad l1\_msualg\_1 X2)))) \Rightarrow (((r1\_xboole\_0 (k2\_msafree2 X1) (k3\_msafree2 \\
& \quad X0)) \wedge (X2 = k2\_circcomb X0 X1)) \Rightarrow (\forall X3.((v4\_msualg\_1 X3 X0) \wedge \\
& \quad ((v4\_msafree2 X3 X0) \wedge (l3\_msualg\_1 X3 X0)))) \Rightarrow (\forall X4.((v4\_msualg\_1 \\
& \quad X4 X1) \wedge ((v4\_msafree2 X4 X1) \wedge (l3\_msualg\_1 X4 X1)))) \Rightarrow (\forall X5. \\
& \quad ((v4\_msualg\_1 X5 X2) \wedge ((v4\_msafree2 X5 X2) \wedge (l3\_msualg\_1 X5 X2)))) \Rightarrow \\
& \quad (((r2\_circcomb X0 X1 X3 X4) \wedge (X5 = k3\_circcomb X0 X1 X3 X4)) \Rightarrow (\forall X6. \\
& \quad (m1\_subset\_1 X6 (k4\_card\_3 (u3\_msualg\_1 X2 X5)))) \Rightarrow (\forall X7. \\
& \quad (m1\_subset\_1 X7 (k4\_card\_3 (u3\_msualg\_1 X1 X4)))) \Rightarrow ((X7 = k5\_relat\_1 \\
& \quad X6 (u1\_struct\_0 X1)) \Rightarrow (\forall X8.(v7\_ordinal1 X8) \Rightarrow (k5\_relat\_1 \\
& \quad (k5\_facirc\_1 X2 X5 X6 X8) (u1\_struct\_0 X1) = k5\_facirc\_1 X1 X4 X7 X8))))))))) \\
& \hspace{15em} (2)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_msafree2 \\
& \quad X0) \wedge (l1\_msualg\_1 X0)))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((\neg \\
& \quad v11\_struct\_0 X1) \wedge (v2\_msafree2 X1) \wedge (l1\_msualg\_1 X1)))) \Rightarrow (\forall X2. \\
& \quad ((\neg v2\_struct\_0 X2) \wedge ((\neg v11\_struct\_0 X2) \wedge ((v2\_msafree2 X2) \wedge ( \\
& \quad l1\_msualg\_1 X2)))) \Rightarrow (((r1\_xboole\_0 (k2\_msafree2 X0) (k3\_msafree2 \\
& \quad X1)) \wedge (X2 = k2\_circcomb X0 X1)) \Rightarrow (\forall X3.((v4\_msualg\_1 X3 X0) \wedge \\
& \quad ((v4\_msafree2 X3 X0) \wedge (l3\_msualg\_1 X3 X0)))) \Rightarrow (\forall X4.((v4\_msualg\_1 \\
& \quad X4 X1) \wedge ((v4\_msafree2 X4 X1) \wedge (l3\_msualg\_1 X4 X1)))) \Rightarrow (\forall X5. \\
& \quad ((v4\_msualg\_1 X5 X2) \wedge ((v4\_msafree2 X5 X2) \wedge (l3\_msualg\_1 X5 X2)))) \Rightarrow \\
& \quad (((r2\_circcomb X0 X1 X3 X4) \wedge (X5 = k3\_circcomb X0 X1 X3 X4)) \Rightarrow (\forall X6. \\
& \quad (m1\_subset\_1 X6 (k4\_card\_3 (u3\_msualg\_1 X2 X5)))) \Rightarrow (\forall X7. \\
& \quad (m1\_subset\_1 X7 (k4\_card\_3 (u3\_msualg\_1 X0 X3)))) \Rightarrow ((X7 = k5\_relat\_1 \\
& \quad X6 (u1\_struct\_0 X0)) \Rightarrow (\forall X8.(v7\_ordinal1 X8) \Rightarrow (k5\_relat\_1 \\
& \quad (k5\_facirc\_1 X2 X5 X6 X8) (u1\_struct\_0 X0) = k5\_facirc\_1 X0 X3 X7 X8))))))))) \\
& \hspace{15em} (3)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. \forall X3. (((\neg v2\_struct\_0 \\
& \quad X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_msafree2 X0) \wedge (l1\_msualg\_1 X0)))) \wedge \\
& \quad (((v4\_msualg\_1 X1 X0) \wedge ((v4\_msafree2 X1 X0) \wedge (l3\_msualg\_1 X1 X0)))) \wedge \\
& \quad ((m1\_subset\_1 X2 (k4\_card\_3 (u3\_msualg\_1 X0 X1))) \wedge (v7\_ordinal1 \\
& \quad X3))) \Rightarrow (m1\_subset\_1 (k5\_facirc\_1 X0 X1 X2 X3) (k4\_card\_3 (u3\_msualg\_1 \\
& \quad X0 X1))) \\
& \hspace{15em} (4)
\end{aligned}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_msafree2 \\
& \quad X0) \wedge (l1\_msualg\_1 X0)))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((\neg \\
& \quad v11\_struct\_0 X1) \wedge ((v2\_msafree2 X1) \wedge (l1\_msualg\_1 X1)))) \Rightarrow (\forall X2. \\
& \quad ((\neg v2\_struct\_0 X2) \wedge ((\neg v11\_struct\_0 X2) \wedge ((v2\_msafree2 X2) \wedge ( \\
& \quad l1\_msualg\_1 X2)))) \Rightarrow (((r1\_xboole\_0 (k2\_msafree2 X0) (k3\_msafree2 \\
& \quad X1)) \wedge ((r1\_xboole\_0 (k2\_msafree2 X1) (k3\_msafree2 X0)) \wedge (X2 = k2\_circcomb \\
& \quad X0 X1))) \Rightarrow (\forall X3.((v4\_msualg\_1 X3 X0) \wedge ((v4\_msafree2 X3 X0) \wedge \\
& \quad (l3\_msualg\_1 X3 X0))) \Rightarrow (\forall X4.((v4\_msualg\_1 X4 X1) \wedge ((v4\_msafree2 \\
& \quad X4 X1) \wedge (l3\_msualg\_1 X4 X1))) \Rightarrow (\forall X5.((v4\_msualg\_1 X5 X2) \wedge \\
& \quad ((v4\_msafree2 X5 X2) \wedge (l3\_msualg\_1 X5 X2))) \Rightarrow (((r2\_circcomb X0 \\
& \quad X1 X3 X4) \wedge (X5 = k3\_circcomb X0 X1 X3 X4)) \Rightarrow (\forall X6.(v7\_ordinal1 \\
& \quad X6) \Rightarrow (\forall X7.(m1\_subset\_1 X7 (k4\_card\_3 (u3\_msualg\_1 X2 X5))) \Rightarrow \\
& \quad (\forall X8.(m1\_subset\_1 X8 (k4\_card\_3 (u3\_msualg\_1 X0 X3))) \Rightarrow \\
& \quad ((X8 = k5\_relat\_1 X7 (u1\_struct\_0 X0)) \Rightarrow (\forall X9.(m1\_subset\_1 \\
& \quad X9 (k4\_card\_3 (u3\_msualg\_1 X1 X4))) \Rightarrow (\neg (X9 = k5\_relat\_1 X7 (u1\_struct\_0 \\
& \quad X1)) \wedge ((\neg (v1\_circuit2 (k5\_facirc\_1 X0 X3 X8 X6) X0 X3) \wedge (v1\_circuit2 \\
& \quad (k5\_facirc\_1 X1 X4 X9 X6) X1 X4)) \wedge (v1\_circuit2 (k5\_facirc\_1 X2 X5 \\
& \quad X7 X6) X2 X5))))))))))))))
\end{aligned}$$