

t23\_facirc\_2 (TMJru-  
UPHbj1FuVKurGsR7jt66awQTtkDDLX)

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Let  $k3\_msafree2 : \iota \Rightarrow \iota$  be given. Let  $k19\_facirc\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_facirc\_1 : \iota$  be given. Let  $k9\_facirc\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_enumset1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_facirc\_1 : \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $k17\_facirc\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_finseq\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_2 : \iota$  be given. Let  $k6\_margrel1 : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_facirc\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_circcomb : \iota \Rightarrow o$  be given. Let  $v2\_circcomb : \iota \Rightarrow o$  be given. Let  $l1\_msualg\_1 : \iota \Rightarrow o$  be given. Let  $k2\_circcomb : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k15\_facirc\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_msualg\_1 : \iota \Rightarrow o$  be given. Let  $v3\_circcomb : \iota \Rightarrow o$  be given. Let  $k14\_facirc\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_circcomb : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_facirc\_1 : \iota$  be given. Let  $k11\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((v1\_funct\_1 X3) \wedge \\ & ((v1\_funct\_2 X3 (k4\_finseq\_2 np\_2 k6\_margrel1) k6\_margrel1) \wedge \\ & (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k4\_finseq\_2 np\_2 \\ & k6\_margrel1) k6\_margrel1)))) \Rightarrow (k3\_msafree2 (k8\_facirc\_1 X0 \\ & X1 X2 X3) = k2\_tarski (k4\_tarski (k10\_finseq\_1 X0 X1) X3) (k9\_facirc\_1 \\ & X0 X1 X2 X3)) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. k2\_xboole\_0 (k2\_xboole\_0 X0 \\ & X1) X2 = k2\_xboole\_0 X0 (k2\_xboole\_0 X1 X2) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v1\_circcomb X0) \wedge ((v2\_circcomb \\ & X0) \wedge (l1\_msualg\_1 X0)))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((v1\_circcomb \\ & X1) \wedge ((v2\_circcomb X1) \wedge (l1\_msualg\_1 X1)))) \Rightarrow (k3\_msafree2 (k2\_circcomb \\ & X0 X1) = k2\_xboole\_0 (k3\_msafree2 X0) (k3\_msafree2 X1))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. k3\_msafree2 (k15\_facirc\_1 X0 \\ & X1 X2) = k2\_xboole\_0 (k1\_enumset1 (k4\_tarski (k10\_finseq\_1 X0 X1) \\ & k3\_facirc\_1) (k4\_tarski (k10\_finseq\_1 X1 X2) k3\_facirc\_1) (k4\_tarski \\ & (k10\_finseq\_1 X2 X0) k3\_facirc\_1)) (k1\_tarski (k17\_facirc\_1 X0 \\ & X1 X2)) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((v1\_funct\_1 X3) \wedge \\ & ((v1\_funct\_2 X3 (k4\_finseq\_2 np\_2 k6\_margrel1) k6\_margrel1) \wedge \\ & (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k4\_finseq\_2 np\_2 \\ & k6\_margrel1) k6\_margrel1)))) \Rightarrow ((\neg v2\_struct\_0 (k8\_facirc\_1 \\ & X0 X1 X2 X3)) \wedge ((\neg v11\_struct\_0 (k8\_facirc\_1 X0 X1 X2 X3)) \wedge ((v1\_msualg\_1 \\ & (k8\_facirc\_1 X0 X1 X2 X3)) \wedge ((v1\_circcomb (k8\_facirc\_1 X0 X1 X2 X3)) \wedge \\ & ((v2\_circcomb (k8\_facirc\_1 X0 X1 X2 X3)) \wedge ((v3\_circcomb (k8\_facirc\_1 \\ & X0 X1 X2 X3)) \wedge (l1\_msualg\_1 (k8\_facirc\_1 X0 X1 X2 X3))))))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & (v1\_funct\_1 k1\_facirc\_1) \wedge ((v1\_funct\_2 k1\_facirc\_1 (k4\_finseq\_2 \\ & np\_2 k6\_margrel1) k6\_margrel1) \wedge (m1\_subset\_1 k1\_facirc\_1 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (k4\_finseq\_2 np\_2 k6\_margrel1) k6\_margrel1)))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (\neg v2\_struct\_0 (k15\_facirc\_1 \\ & X0 X1 X2)) \wedge ((\neg v11\_struct\_0 (k15\_facirc\_1 X0 X1 X2)) \wedge ((v1\_msualg\_1 \\ & (k15\_facirc\_1 X0 X1 X2)) \wedge ((v1\_circcomb (k15\_facirc\_1 X0 X1 X2)) \wedge \\ & ((v2\_circcomb (k15\_facirc\_1 X0 X1 X2)) \wedge ((v3\_circcomb (k15\_facirc\_1 \\ & X0 X1 X2)) \wedge (l1\_msualg\_1 (k15\_facirc\_1 X0 X1 X2))))))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. k19\_facirc\_1 X0 X1 X2 = k2\_circcomb \\ & (k8\_facirc\_1 X0 X1 X2 k1\_facirc\_1) (k15\_facirc\_1 X0 X1 X2) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.k15\_facirc.1 X0 X1 X2 = k2\_circcomb \\ & (k14\_facirc.1 X0 X1 X2) (k5\_circcomb k4\_facirc.1 (k11\_finseq.1 \\ & (k4\_tarski (k10\_finseq.1 X0 X1) k3\_facirc.1) (k4\_tarski (k10\_finseq.1 \\ & X1 X2) k3\_facirc.1) (k4\_tarski (k10\_finseq.1 X2 X0) k3\_facirc.1))) \end{aligned} \quad (9)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.k3\_msafree2 (k19\_facirc.1 X0 \\ & X1 X2) = k2\_xboole.0 (k2\_xboole.0 (k2\_tarski (k4\_tarski (k10\_finseq.1 \\ & X0 X1) k1\_facirc.1) (k9\_facirc.1 X0 X1 X2 k1\_facirc.1)) (k1\_enumset1 \\ & (k4\_tarski (k10\_finseq.1 X0 X1) k3\_facirc.1) (k4\_tarski (k10\_finseq.1 \\ & X1 X2) k3\_facirc.1) (k4\_tarski (k10\_finseq.1 X2 X0) k3\_facirc.1))) \\ & (k1\_tarski (k17\_facirc.1 X0 X1 X2)) \end{aligned}$$