t23_heyting2 (TMQQHSH2NNNWRtjphWwnp2m4nnmU635ipzr)

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Let $v1\_finset\_1 : \iota \Rightarrow o$ be given. Let $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k4\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $u1\_struct\_0 : \iota \Rightarrow \iota$ be given. Let $k5\_substlat : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k8\_heyting2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1\_tarski : \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall X0.\forall X1.(v1\_finset\_1\ X1) \Rightarrow (\forall X2.(m1\_subset\_1\ X2\ (k4\_partfun1\ X0\ X1)) \Rightarrow ((v1\_finset\_1\ X2) \Rightarrow (k3\_funct\_2\ (k4\_partfun1\ X0\ X1)\ (u1\_struct\_0\ (k5\_substlat\ X0\ X1))\ (k8\_heyting2\ X0\ X1)\ X2 = k1\_tarski\ X2))) \tag{1}$$

Assume the following.

$$\forall X0.\forall X1.(X1 = k1\_tarski\ X0) \Leftrightarrow (\forall X2.(X2 \in X1) \Leftrightarrow (X2 = X0)) \tag{2}$$

Theorem 1

$$\forall X0.\forall X1.(v1\_finset\_1\ X1) \Rightarrow (\forall X2.((v1\_finset\_1\ X2) \wedge (m1\_subset\_1\ X2\ (k4\_partfun1\ X0\ X1))) \Rightarrow (X2 \in k3\_funct\_2\ (k4\_partfun1\ X0\ X1)\ (u1\_struct\_0\ (k5\_substlat\ X0\ X1))\ (k8\_heyting2\ X0\ X1)\ X2))$$