

## t23\_isocat\_1

(TMFPnm64Gy9Eqc2G328nuTbo8BHP89b5z14)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v3\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v5\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v6\_cat\_1 : \iota \Rightarrow o$  be given. Let  $l1\_cat\_1 : \iota \Rightarrow o$  be given. Let  $m2\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_nattr\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m2\_nattr\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k4\_nattr\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_isocat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_cat\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_nattr\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_nattr\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_isocat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $m1\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\
 & X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\
 & X0) \wedge (l1\_cat\_1 X0))))))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((\neg \\
 & v11\_struct\_0 X1) \wedge ((v2\_cat\_1 X1) \wedge ((v3\_cat\_1 X1) \wedge ((v4\_cat\_1 \\
 & X1) \wedge ((v5\_cat\_1 X1) \wedge ((v6\_cat\_1 X1) \wedge (l1\_cat\_1 X1))))))) \Rightarrow (\forall X2. \\
 & ((\neg v2\_struct\_0 X2) \wedge ((\neg v11\_struct\_0 X2) \wedge ((v2\_cat\_1 X2) \wedge ((v3\_cat\_1 \\
 & X2) \wedge ((v4\_cat\_1 X2) \wedge ((v5\_cat\_1 X2) \wedge ((v6\_cat\_1 X2) \wedge (l1\_cat\_1 \\
 & X2))))))) \Rightarrow (\forall X3.(m2\_cat\_1 X3 X0 X1) \Rightarrow (\forall X4.(m2\_cat\_1 \\
 & X4 X0 X1) \Rightarrow ((r1\_nattr\_1 X0 X1 X3 X4) \Rightarrow (\forall X5.(m1\_nattr\_1 X5 \\
 & X0 X1 X3 X4) \Rightarrow (\forall X6.(m2\_cat\_1 X6 X1 X2) \Rightarrow (\forall X7.(m1\_subset\_1 \\
 & X7 (u1\_struct\_0 X0)) \Rightarrow (k4\_nattr\_1 X0 X2 (k9\_cat\_1 X0 X1 X2 X3 X6) \\
 & (k9\_cat\_1 X0 X1 X2 X4 X6) (k2\_isocat\_1 X0 X1 X2 X3 X4 X5 X6) X7 = k9\_cat\_3 \\
 & X1 (k8\_cat\_1 X0 X1 X3 X7) (k8\_cat\_1 X0 X1 X4 X7) X2 X6 (k4\_nattr\_1 X0 \\
 & X1 X3 X4 X5 X7))))))))))
 \end{aligned}$$

(1)

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((\neg v2\_struct\_0 \\ & X0)\wedge((\neg v11\_struct\_0 X0)\wedge((v2\_cat\_1 X0)\wedge((v3\_cat\_1 X0)\wedge((v4\_cat\_1 \\ & X0)\wedge((v5\_cat\_1 X0)\wedge((v6\_cat\_1 X0)\wedge(l1\_cat\_1 X0))))))))\wedge((( \\ & \neg v2\_struct\_0 X1)\wedge((\neg v11\_struct\_0 X1)\wedge((v2\_cat\_1 X1)\wedge((v3\_cat\_1 \\ & X1)\wedge((v4\_cat\_1 X1)\wedge((v5\_cat\_1 X1)\wedge((v6\_cat\_1 X1)\wedge(l1\_cat\_1 \\ & X1))))))))\wedge((m2\_cat\_1 X2 X0 X1)\wedge(m2\_cat\_1 X3 X0 X1)))\Rightarrow(\forall X4. \\ & (m2\_nattra\_1 X4 X0 X1 X2 X3)\Rightarrow(m1\_nattra\_1 X4 X0 X1 X2 X3)) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 X0)\wedge((v2\_cat\_1 \\ & X0)\wedge((v3\_cat\_1 X0)\wedge((v4\_cat\_1 X0)\wedge((v5\_cat\_1 X0)\wedge((v6\_cat\_1 \\ & X0)\wedge(l1\_cat\_1 X0))))))))\Rightarrow(\forall X1.((\neg v2\_struct\_0 X1)\wedge(( \\ & \neg v11\_struct\_0 X1)\wedge((v2\_cat\_1 X1)\wedge((v3\_cat\_1 X1)\wedge((v4\_cat\_1 \\ & X1)\wedge((v5\_cat\_1 X1)\wedge((v6\_cat\_1 X1)\wedge(l1\_cat\_1 X1))))))))\Rightarrow(\forall X2. \\ & (m2\_cat\_1 X2 X0 X1)\Rightarrow(\forall X3.(m2\_cat\_1 X3 X0 X1)\Rightarrow((r2\_nattra\_1 \\ & X0 X1 X2 X3)\Leftrightarrow((r1\_nattra\_1 X0 X1 X2 X3)\wedge(\exists X4.(m1\_nattra\_1 \\ & X4 X0 X1 X2 X3)\wedge(\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0))\Rightarrow( \\ & \forall X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0))\Rightarrow((k2\_cat\_1 X0 X5 \\ & X6\neq k1\_xboole\_0)\Rightarrow(\forall X7.(m1\_cat\_1 X7 X0 X5 X6)\Rightarrow(k5\_cat\_1 \\ & X1 (k8\_cat\_1 X0 X1 X2 X5) (k8\_cat\_1 X0 X1 X2 X6) (k8\_cat\_1 X0 X1 X3 X6) \\ & (k9\_cat\_3 X0 X5 X6 X1 X2 X7) (k4\_nattra\_1 X0 X1 X2 X3 X4 X6) = k5\_cat\_1 \\ & X1 (k8\_cat\_1 X0 X1 X2 X5) (k8\_cat\_1 X0 X1 X3 X5) (k8\_cat\_1 X0 X1 X3 X6) \\ & (k4\_nattra\_1 X0 X1 X2 X3 X4 X5) (k9\_cat\_3 X0 X5 X6 X1 X3 X7)))))))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 X0)\wedge((v2\_cat\_1 \\ & X0)\wedge((v3\_cat\_1 X0)\wedge((v4\_cat\_1 X0)\wedge((v5\_cat\_1 X0)\wedge((v6\_cat\_1 \\ & X0)\wedge(l1\_cat\_1 X0))))))))\Rightarrow(\forall X1.((\neg v2\_struct\_0 X1)\wedge(( \\ & \neg v11\_struct\_0 X1)\wedge((v2\_cat\_1 X1)\wedge((v3\_cat\_1 X1)\wedge((v4\_cat\_1 \\ & X1)\wedge((v5\_cat\_1 X1)\wedge((v6\_cat\_1 X1)\wedge(l1\_cat\_1 X1))))))))\Rightarrow(\forall X2. \\ & ((\neg v2\_struct\_0 X2)\wedge((\neg v11\_struct\_0 X2)\wedge((v2\_cat\_1 X2)\wedge((v3\_cat\_1 \\ & X2)\wedge((v4\_cat\_1 X2)\wedge((v5\_cat\_1 X2)\wedge((v6\_cat\_1 X2)\wedge(l1\_cat\_1 \\ & X2))))))))\Rightarrow(\forall X3.(m2\_cat\_1 X3 X0 X1)\Rightarrow(\forall X4.(m2\_cat\_1 \\ & X4 X0 X1)\Rightarrow((r2\_nattra\_1 X0 X1 X3 X4)\Rightarrow(\forall X5.(m2\_nattra\_1 X5 \\ & X0 X1 X3 X4)\Rightarrow(\forall X6.(m2\_cat\_1 X6 X1 X2)\Rightarrow(k4\_isocat\_1 X0 X1 X2 \\ & X3 X4 X5 X6 = k2\_isocat\_1 X0 X1 X2 X3 X4 X5 X6)))))) \end{aligned} \quad (4)$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\
& X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\
& X0) \wedge (l1\_cat\_1 X0)))))))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge (( \\
& \neg v11\_struct\_0 X1) \wedge ((v2\_cat\_1 X1) \wedge ((v3\_cat\_1 X1) \wedge ((v4\_cat\_1 \\
& X1) \wedge ((v5\_cat\_1 X1) \wedge ((v6\_cat\_1 X1) \wedge (l1\_cat\_1 X1)))))))) \Rightarrow (\forall X2. \\
& ((\neg v2\_struct\_0 X2) \wedge ((\neg v11\_struct\_0 X2) \wedge ((v2\_cat\_1 X2) \wedge ((v3\_cat\_1 \\
& X2) \wedge ((v4\_cat\_1 X2) \wedge ((v5\_cat\_1 X2) \wedge ((v6\_cat\_1 X2) \wedge (l1\_cat\_1 \\
& X2)))))))) \Rightarrow (\forall X3.(m2\_cat\_1 X3 X0 X1) \Rightarrow (\forall X4.(m2\_cat\_1 \\
& X4 X0 X1) \Rightarrow ((r2\_nattr\_1 X0 X1 X3 X4) \Rightarrow (\forall X5.(m2\_nattr\_1 X5 \\
& X0 X1 X3 X4) \Rightarrow (\forall X6.(m2\_cat\_1 X6 X1 X2) \Rightarrow (\forall X7.(m1\_subset\_1 \\
& X7 (u1\_struct\_0 X0)) \Rightarrow (k4\_nattr\_1 X0 X2 (k9\_cat\_1 X0 X1 X2 X3 X6) \\
& (k9\_cat\_1 X0 X1 X2 X4 X6) (k4\_isocat\_1 X0 X1 X2 X3 X4 X5 X6) X7 = k9\_cat\_3 \\
& X1 (k8\_cat\_1 X0 X1 X3 X7) (k8\_cat\_1 X0 X1 X4 X7) X2 X6 (k4\_nattr\_1 X0 \\
& X1 X3 X4 X5 X7))))))))))
\end{aligned}$$