

t23\_mssubfam (TMSHRvD-  
NPq1Yh7TvohJfbtQMxU8o1Wte5bD)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_finset\_1 : \iota \Rightarrow o$  be given. Let  $k2\_mboolean : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $k3\_tarski : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0.((v1\_finset\_1 X0) \wedge (\forall X1.(X1 \in X0) \Rightarrow (v1\_finset\_1 X1))) \Leftrightarrow (v1\_finset\_1 (k3\_tarski X0)) \quad (1)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge (v1\_funct\_1 X1) \wedge (v1\_partfun1 X1 X0))) \Rightarrow ((v1\_relat\_1 (k2\_mboolean X0 X1)) \wedge ((v4\_relat\_1 (k2\_mboolean X0 X1) X0) \wedge ((v1\_funct\_1 (k2\_mboolean X0 X1)) \wedge (v1\_partfun1 (k2\_mboolean X0 X1) X0)))) \quad (2)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge (v1\_funct\_1 X1))) \Rightarrow ((v2\_finset\_1 X1) \Leftrightarrow (\forall X2.(X2 \in X0) \Rightarrow (v1\_finset\_1 (k1\_funct\_1 X1 X2)))) \quad (3)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge (v1\_funct\_1 X1) \wedge (v1\_partfun1 X1 X0))) \Rightarrow (\forall X2.((v1\_relat\_1 X2) \wedge ((v4\_relat\_1 X2 X0) \wedge (v1\_funct\_1 X2) \wedge (v1\_partfun1 X2 X0)))) \Rightarrow ((X2 = k2\_mboolean X0 X1) \Leftrightarrow (\forall X3.(X3 \in X0) \Rightarrow (k1\_funct\_1 X2 X3 = k3\_tarski (k1\_funct\_1 X1 X3)))) \quad (4)$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge \\
& (v1\_funct\_1 X1) \wedge (v1\_partfun1 X1 X0))) \Rightarrow (\forall X2. ((v1\_relat\_1 \\
& X2) \wedge ((v4\_relat\_1 X2 X0) \wedge ((v1\_funct\_1 X2) \wedge (v1\_partfun1 X2 X0)))) \Rightarrow \\
& ((r1\_pboole X0 X1 X2) \Leftrightarrow (\forall X3. (X3 \in X0) \Rightarrow (k1\_funct\_1 X1 X3 \in k1\_funct\_1 \\
& X2 X3))))
\end{aligned} \tag{5}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge \\
& (v1\_funct\_1 X1) \wedge (v1\_partfun1 X1 X0))) \Rightarrow ((v2\_finset\_1 (k2\_mboolean \\
& X0 X1)) \Rightarrow ((v2\_finset\_1 X1) \wedge (\forall X2. ((v1\_relat\_1 X2) \wedge ((v4\_relat\_1 \\
& X2 X0) \wedge ((v1\_funct\_1 X2) \wedge (v1\_partfun1 X2 X0)))) \Rightarrow ((r1\_pboole X0 \\
& X2 X1) \Rightarrow (v2\_finset\_1 X2))))))
\end{aligned}$$