

t23\_ordinal2  
(TMXhYiadyiU4roCu1VwNwHqeC4Cp68jN7Zq)

October 27, 2020

Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k3\_ordinal2 : \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_ordinal1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. X0 \neq k1\_ordinal1 X0 \tag{1}$$

Assume the following.

$$\forall X0. \forall X1. (X0 \in k1\_ordinal1 X1) \Leftrightarrow ((X0 \in X1) \vee (X0 = X1)) \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. r1\_tarski X0 (k2\_xboole\_0 X0 X1) \tag{3}$$

Assume the following.

$$\forall X0. \forall X1. (r1\_tarski X0 X1) \Rightarrow (r1\_ordinal1 (k3\_ordinal2 X0) (k3\_ordinal2 X1)) \tag{4}$$

Assume the following.

$$\forall X0. (v3\_ordinal1 X0) \Rightarrow (\forall X1. (v3\_ordinal1 X1) \Rightarrow ((X0 \in k1\_ordinal1 X1) \Leftrightarrow (r1\_ordinal1 X0 X1))) \tag{5}$$

Assume the following.

$$\forall X0. (v3\_ordinal1 X0) \Rightarrow (\forall X1. \neg (X0 \in k3\_ordinal2 X1) \wedge (\forall X2. (v3\_ordinal1 X2) \Rightarrow (\neg (X2 \in X1) \wedge (r1\_ordinal1 X0 X2)))) \tag{6}$$

Assume the following.

$$\forall X0. (v3\_ordinal1 X0) \Rightarrow (\forall X1. (v3\_ordinal1 X1) \Rightarrow ((X0 \in X1) \Leftrightarrow (r1\_ordinal1 (k1\_ordinal1 X0) X1))) \tag{7}$$

Assume the following.

$$\forall X0.(v3\_ordinal1\ X0)\Rightarrow(\forall X1.(X0 \in X1)\Rightarrow(X0 \in k3\_ordinal2\ X1)) \quad (8)$$

Assume the following.

$$\forall X0.(v3\_ordinal1\ X0)\Rightarrow(k3\_ordinal2\ X0 = X0) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.(k4\_xboole\_0\ (k1\_tarski\ X0)\ (k1\_tarski\ X1) = k1\_tarski\ X0)\Leftrightarrow(X0\neq X1) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.((v3\_ordinal1\ X0)\wedge(v3\_ordinal1\ X1))\Rightarrow((r1\_ordinal1\ X0\ X1)\Leftrightarrow(r1\_tarski\ X0\ X1)) \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.k6\_subset\_1\ X0\ X1 = k4\_xboole\_0\ X0\ X1 \quad (12)$$

Assume the following.

$$\forall X0.(v3\_ordinal1\ X0)\Rightarrow((\neg v1\_xboole\_0\ (k1\_ordinal1\ X0))\wedge(v3\_ordinal1\ (k1\_ordinal1\ X0))) \quad (13)$$

Assume the following.

$$\forall X0.v3\_ordinal1\ (k3\_ordinal2\ X0) \quad (14)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(X2 = k4\_xboole\_0\ X0\ X1)\Leftrightarrow(\forall X3.(X3 \in X2)\Leftrightarrow((X3 \in X0)\wedge(\neg X3 \in X1))) \quad (15)$$

Assume the following.

$$\forall X0.\forall X1.(X1 = k1\_tarski\ X0)\Leftrightarrow(\forall X2.(X2 \in X1)\Leftrightarrow(X2 = X0)) \quad (16)$$

Assume the following.

$$\forall X0.k1\_ordinal1\ X0 = k2\_xboole\_0\ X0\ (k1\_tarski\ X0) \quad (17)$$

Assume the following.

$$\forall X0.\forall X1.(X0 = X1)\Leftrightarrow((r1\_tarski\ X0\ X1)\wedge(r1\_tarski\ X1\ X0)) \quad (18)$$

**Theorem 1**

$$\forall X0.(v3\_ordinal1\ X0)\Rightarrow(k3\_ordinal2\ (k1\_tarski\ X0) = k1\_ordinal1\ X0)$$