

# t23\_sublemma (TMPKTMCKRtvT- tkqD4v3D4VqcATj25Z3Dcwh)

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Let  $m1\_qc\_lang1 : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k16\_subst1 : \iota \Rightarrow \iota$  be given. Let  $k38\_subst1 : \iota \Rightarrow \iota$  be given. Let  $k19\_subst1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k39\_subst1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_sublemma : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_cqc\_lang : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k37\_subst1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k21\_subst1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k14\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k3\_cqc\_lang : \iota \Rightarrow \iota$  be given. Let  $k9\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k16\_subst1 \\ & X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k16\_subst1 X0)) \Rightarrow ((k19\_subst1 \\ & X0 X1 = k19\_subst1 X0 X2) \Rightarrow (k37\_subst1 X0 (k21\_subst1 X0 X1 \\ & X2) = k14\_qc\_lang1 X0 (k37\_subst1 X0 X1) (k37\_subst1 X0 X2)))))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))) \Rightarrow (\forall X2.(m2\_subset\_1 \\ & X2 X0 X1) \Leftrightarrow (m1\_subset\_1 X2 X1)) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.((m1\_qc\_lang1 X0) \wedge ((m1\_subset\_1 \\ & X1 (k3\_cqc\_lang X0)) \wedge (m1\_subset\_1 X2 (k3\_cqc\_lang X0)))) \Rightarrow (k7\_cqc\_lang \\ & X0 X1 X2 = k14\_qc\_lang1 X0 X1 X2) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((m1\_qc\_lang1 X0) \wedge (m1\_subset\_1 X1 (k38\_subst1 \\ & X0))) \Rightarrow (k39\_subst1 X0 X1 = k37\_subst1 X0 X1) \end{aligned} \quad (4)$$

Assume the following.

$$\forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\neg v1\_xboole\_0 (k38\_subst1 X0)) \quad (5)$$

Assume the following.

$$\forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\neg v1\_xboole\_0 (k3\_cqc\_lang X0)) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))) \Rightarrow (\forall X2.(m2\_subset\_1 X2 X0 X1) \Rightarrow (m1\_subset\_1 X2 X0)) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((m1\_qc\_lang1 X0) \wedge ((m1\_subset\_1 X1 (k38\_subst1 X0)) \wedge (m1\_subset\_1 X2 (k38\_subst1 X0)))) \Rightarrow (m2\_subset\_1 (k6\_sublemma X0 X1 X2) (k16\_subst1 X0) (k38\_subst1 X0)) \quad (8)$$

Assume the following.

$$\forall X0.(m1\_qc\_lang1 X0) \Rightarrow (m1\_subset\_1 (k3\_cqc\_lang X0) (k1\_zfmisc\_1 (k9\_qc\_lang1 X0))) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.((m1\_qc\_lang1 X0) \wedge (m1\_subset\_1 X1 (k38\_subst1 X0))) \Rightarrow (m2\_subset\_1 (k39\_subst1 X0 X1) (k9\_qc\_lang1 X0) (k3\_cqc\_lang X0)) \quad (10)$$

Assume the following.

$$\forall X0.(m1\_qc\_lang1 X0) \Rightarrow (m1\_subset\_1 (k38\_subst1 X0) (k1\_zfmisc\_1 (k16\_subst1 X0))) \quad (11)$$

Assume the following.

$$\forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\forall X1.(m2\_subset\_1 X1 (k16\_subst1 X0) (k38\_subst1 X0)) \Rightarrow (\forall X2.(m2\_subset\_1 X2 (k16\_subst1 X0) (k38\_subst1 X0)) \Rightarrow ((k19\_subst1 X0 X1 = k19\_subst1 X0 X2) \Rightarrow (k6\_sublemma X0 X1 X2 = k21\_subst1 X0 X1 X2)))) \quad (12)$$

Assume the following.

$$\forall X0.(v1\_xboole\_0 X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)) \Rightarrow (v1\_xboole\_0 X1)) \quad (13)$$

**Theorem 1**

$$\forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\forall X1.(m2\_subset\_1 X1 (k16\_subst1 X0) (k38\_subst1 X0)) \Rightarrow (\forall X2.(m2\_subset\_1 X2 (k16\_subst1 X0) (k38\_subst1 X0)) \Rightarrow ((k19\_subst1 X0 X1 = k19\_subst1 X0 X2) \Rightarrow (k39\_subst1 X0 (k6\_sublemma X0 X1 X2) = k7\_cqc\_lang X0 (k39\_subst1 X0 X1) (k39\_subst1 X0 X2))))))$$