

t24_borsuk_1

(TMbdTyjRKudvGJmChUZUnrL1pA7p1jnxupc)

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Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $v2_pre_topc : \iota \Rightarrow o$ be given. Let $l1_pre_topc : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $k3_borsuk_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_xboole_0 : \iota$ be given. Let $k3_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_borsuk_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k9_setfam_1 : \iota \Rightarrow \iota$ be given. Let $k8_borsuk_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k9_borsuk_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k8_mcart_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_funct_3 : \iota \Rightarrow \iota$ be given. Let $k9_funct_3 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k10_funct_3 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_funct_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v4_pre_topc : \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(m1_subset_1 X2 (k1_zfmisc_1 \\ & X0)) \Rightarrow (\forall X3.(m1_subset_1 X3 (k1_zfmisc_1 X1)) \Rightarrow ((k8_mcart_1 \\ & X0 X1 X2 X3 \neq k1_xboole_0) \Rightarrow ((k1_funct_1 (k1_funct_3 (k9_funct_3 \\ & X0 X1)) (k8_mcart_1 X0 X1 X2 X3) = X2) \wedge (k1_funct_1 (k1_funct_3 (k10_funct_3 \\ & X0 X1)) (k8_mcart_1 X0 X1 X2 X3) = X3)))) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0.k9_setfam_1 X0 = k1_zfmisc_1 X0 \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((m1_subset_1 X2 \\ & (k1_zfmisc_1 X0)) \wedge (m1_subset_1 X3 (k1_zfmisc_1 X1))) \Rightarrow (k8_mcart_1 \\ & X0 X1 X2 X3 = k2_zfmisc_1 X2 X3) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((\neg v1_xboole_0 X0) \wedge \\ & (((v1_funct_1 X2) \wedge ((v1_funct_2 X2 X0 X1) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\ & (k2_zfmisc_1 X0 X1)))))) \wedge (m1_subset_1 X3 X0))) \Rightarrow (k3_funct_2 X0 \\ & X1 X2 X3 = k1_funct_1 X2 X3) \end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((v2_pre_topc\ X0)\wedge \\ & (l1_pre_topc\ X0))\wedge(((v2_pre_topc\ X1)\wedge(l1_pre_topc\ X1))\wedge((m1_subset_1 \\ & X2\ (k1_zfmisc_1\ (u1_struct_0\ X0)))\wedge(m1_subset_1\ X3\ (k1_zfmisc_1 \\ & (u1_struct_0\ X1))))))\Rightarrow(k3_borsuk_1\ X0\ X1\ X2\ X3 = k2_zfmisc_1\ X2 \\ & X3) \end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.((\neg v1_xboole_0\ X1)\wedge((v1_funct_1 \\ & X2)\wedge((v1_funct_2\ X2\ X0\ X1)\wedge(m1_subset_1\ X2\ (k1_zfmisc_1\ (k2_zfmisc_1 \\ & X0\ X1))))))\Rightarrow(k2_funct_3\ X0\ X1\ X2 = k1_funct_3\ X2) \end{aligned} \tag{6}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0\ X0)\wedge((v2_pre_topc\ X0)\wedge(l1_pre_topc \\ & X0)))\Rightarrow(\exists X1.(m1_subset_1\ X1\ (k1_zfmisc_1\ (u1_struct_0 \\ & X0)))\wedge((\neg v1_xboole_0\ X1)\wedge(v4_pre_topc\ X1\ X0))) \end{aligned} \tag{7}$$

Assume the following.

$$\forall X0.\neg v1_xboole_0\ (k1_zfmisc_1\ X0) \tag{8}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(v1_funct_1\ (k9_funct_3\ X0\ X1))\wedge((v1_funct_2 \\ & (k9_funct_3\ X0\ X1)\ (k2_zfmisc_1\ X0\ X1)\ X0)\wedge(m1_subset_1\ (k9_funct_3 \\ & X0\ X1)\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k2_zfmisc_1\ X0\ X1)\ X0)))) \end{aligned} \tag{9}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2_struct_0\ X0)\wedge((v2_pre_topc\ X0)\wedge \\ & (l1_pre_topc\ X0)))\wedge((\neg v2_struct_0\ X1)\wedge((v2_pre_topc\ X1)\wedge(l1_pre_topc \\ & X1))))\Rightarrow((v1_funct_1\ (k9_borsuk_1\ X0\ X1))\wedge((v1_funct_2\ (k9_borsuk_1 \\ & X0\ X1)\ (k9_setfam_1\ (u1_struct_0\ (k2_borsuk_1\ X0\ X1)))\ (k9_setfam_1 \\ & (u1_struct_0\ X1)))\wedge(m1_subset_1\ (k9_borsuk_1\ X0\ X1)\ (k1_zfmisc_1 \\ & (k2_zfmisc_1\ (k9_setfam_1\ (u1_struct_0\ (k2_borsuk_1\ X0\ X1))) \\ & (k9_setfam_1\ (u1_struct_0\ X1)))))) \end{aligned} \tag{10}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2_struct_0\ X0)\wedge((v2_pre_topc\ X0)\wedge \\ & (l1_pre_topc\ X0)))\wedge((\neg v2_struct_0\ X1)\wedge((v2_pre_topc\ X1)\wedge(l1_pre_topc \\ & X1))))\Rightarrow((v1_funct_1\ (k8_borsuk_1\ X0\ X1))\wedge((v1_funct_2\ (k8_borsuk_1 \\ & X0\ X1)\ (k9_setfam_1\ (u1_struct_0\ (k2_borsuk_1\ X0\ X1)))\ (k9_setfam_1 \\ & (u1_struct_0\ X0)))\wedge(m1_subset_1\ (k8_borsuk_1\ X0\ X1)\ (k1_zfmisc_1 \\ & (k2_zfmisc_1\ (k9_setfam_1\ (u1_struct_0\ (k2_borsuk_1\ X0\ X1))) \\ & (k9_setfam_1\ (u1_struct_0\ X0)))))) \end{aligned} \tag{11}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((v2_pre_topc\ X0)\wedge \\ & (l1_pre_topc\ X0))\wedge(((v2_pre_topc\ X1)\wedge(l1_pre_topc\ X1))\wedge((m1_subset_1 \\ & X2\ (k1_zfmisc_1\ (u1_struct_0\ X0)))\wedge(m1_subset_1\ X3\ (k1_zfmisc_1 \\ & (u1_struct_0\ X1))))))\Rightarrow(m1_subset_1\ (k3_borsuk_1\ X0\ X1\ X2\ X3)\ (\\ & k1_zfmisc_1\ (u1_struct_0\ (k2_borsuk_1\ X0\ X1)))) \end{aligned} \quad (12)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(v1_funct_1\ (k10_funct_3\ X0\ X1))\wedge((v1_funct_2 \\ & (k10_funct_3\ X0\ X1)\ (k2_zfmisc_1\ X0\ X1\ X1))\wedge(m1_subset_1\ (k10_funct_3 \\ & X0\ X1)\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k2_zfmisc_1\ X0\ X1)\ X1)))) \end{aligned} \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0\ X0)\wedge((v2_pre_topc\ X0)\wedge(l1_pre_topc \\ & X0)))\Rightarrow(\forall X1.((\neg v2_struct_0\ X1)\wedge((v2_pre_topc\ X1)\wedge(l1_pre_topc \\ & X1))))\Rightarrow(k9_borsuk_1\ X0\ X1 = k2_funct_3\ (k2_zfmisc_1\ (u1_struct_0 \\ & X0)\ (u1_struct_0\ X1))\ (u1_struct_0\ X1)\ (k10_funct_3\ (u1_struct_0 \\ & X0)\ (u1_struct_0\ X1)))) \end{aligned} \quad (14)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0\ X0)\wedge((v2_pre_topc\ X0)\wedge(l1_pre_topc \\ & X0)))\Rightarrow(\forall X1.((\neg v2_struct_0\ X1)\wedge((v2_pre_topc\ X1)\wedge(l1_pre_topc \\ & X1))))\Rightarrow(k8_borsuk_1\ X0\ X1 = k2_funct_3\ (k2_zfmisc_1\ (u1_struct_0 \\ & X0)\ (u1_struct_0\ X1))\ (u1_struct_0\ X0)\ (k9_funct_3\ (u1_struct_0 \\ & X0)\ (u1_struct_0\ X1)))) \end{aligned} \quad (15)$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1_xboole_0\ X0)\Rightarrow(\forall X1.(m1_subset_1\ X1\ (k1_zfmisc_1 \\ & X0))\Rightarrow(v1_xboole_0\ X1)) \end{aligned} \quad (16)$$

Theorem 1

$$\begin{aligned} & \forall X0.((\neg v2_struct_0\ X0)\wedge((v2_pre_topc\ X0)\wedge(l1_pre_topc \\ & X0)))\Rightarrow(\forall X1.((\neg v2_struct_0\ X1)\wedge((v2_pre_topc\ X1)\wedge(l1_pre_topc \\ & X1))))\Rightarrow(\forall X2.(m1_subset_1\ X2\ (k1_zfmisc_1\ (u1_struct_0 \\ & X0)))\Rightarrow(\forall X3.(m1_subset_1\ X3\ (k1_zfmisc_1\ (u1_struct_0 \\ & X1))))\Rightarrow((k3_borsuk_1\ X0\ X1\ X2\ X3\neq k1_xboole_0)\Rightarrow((k3_funct_2\ (k1_zfmisc_1 \\ & (u1_struct_0\ (k2_borsuk_1\ X0\ X1)))\ (k9_setfam_1\ (u1_struct_0 \\ & X0))\ (k8_borsuk_1\ X0\ X1)\ (k3_borsuk_1\ X0\ X1\ X2\ X3) = X2)\wedge(k3_funct_2 \\ & (k1_zfmisc_1\ (u1_struct_0\ (k2_borsuk_1\ X0\ X1)))\ (k9_setfam_1 \\ & (u1_struct_0\ X1))\ (k9_borsuk_1\ X0\ X1)\ (k3_borsuk_1\ X0\ X1\ X2\ X3) = \\ & X3)))))) \end{aligned}$$