

t24_integr19

(TMZ9HL4cEfe4vETCJZFhcBWR4NVpUU2YEhM)

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Let $v1_xreal_0 : \iota \Rightarrow o$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $m2_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_numbers : \iota$ be given. Let $k5_numbers : \iota$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_euclid : \iota \Rightarrow \iota$ be given. Let $r1_xxreal_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_integr15 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k3_integra5 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_integra5 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_nfcont_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v3_integr15 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_relset_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k12_euclid : \iota \Rightarrow \iota$ be given. Let $k7_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k12_integr15 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k11_binop_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k10_binop_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned}
 & \forall X0.(v1_xreal_0 X0) \Rightarrow (\forall X1.(v1_xreal_0 X1) \Rightarrow (\forall X2. \\
 & (v1_xreal_0 X2) \Rightarrow (\forall X3.(v1_xreal_0 X3) \Rightarrow (\forall X4.(v1_xreal_0 \\
 & X4) \Rightarrow (\forall X5.((\neg v1_xboole_0 X5) \wedge (m2_subset_1 X5 k1_numbers \\
 & k5_numbers)) \Rightarrow (\forall X6.((v1_funct_1 X6) \wedge (m1_subset_1 X6 (\\
 & k1_zfmisc_1 (k2_zfmisc_1 k1_numbers (k1_euclid X5)))))) \Rightarrow (((r1_xxreal_0 \\
 & X0 X1) \wedge ((r1_xxreal_0 X2 X3) \wedge ((r1_integr15 X5 (k3_integra5 X0 X1) \\
 & X6) \wedge ((r1_integra5 (k3_integra5 X0 X1) (k1_nfcont_4 X5 k1_numbers \\
 & X6)) \wedge ((v3_integr15 (k2_partfun1 k1_numbers (k1_euclid X5) X6 \\
 & (k3_integra5 X0 X1)) X5) \wedge (r1_tarski (k3_integra5 X0 X1) (k1_relset_1 \\
 & k1_numbers X6)) \wedge ((X2 \in k3_integra5 X0 X1) \wedge ((X3 \in k3_integra5 X0 \\
 & X1) \wedge (\forall X7.(v1_xreal_0 X7) \Rightarrow ((X7 \in k3_integra5 X2 X3) \Rightarrow (r1_xxreal_0 \\
 & (k12_euclid (k7_partfun1 (k1_euclid X5) X6 X7)) X4)))))))))) \Rightarrow \\
 & (r1_xxreal_0 (k12_euclid (k12_integr15 X3 X2 X5 X6)) (k11_binop_2 \\
 & X4 (k10_binop_2 X3 X2)))))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v1_xreal_0 X0) \Rightarrow (\forall X1.(v1_xreal_0 X1) \Rightarrow (\forall X2. \\
& (v1_xreal_0 X2) \Rightarrow (\forall X3.(v1_xreal_0 X3) \Rightarrow (\forall X4.(v1_xreal_0 \\
& X4) \Rightarrow (\forall X5.((\neg v1_xboole_0 X5) \wedge (m2_subset_1 X5 k1_numbers \\
& k5_numbers)) \Rightarrow (\forall X6.((v1_funct_1 X6) \wedge (m1_subset_1 X6 (\\
& k1_zfmisc_1 (k2_zfmisc_1 k1_numbers (k1_euclid X5)))))) \Rightarrow (((r1_xxreal_0 \\
& X0 X1) \wedge ((r1_xxreal_0 X2 X3) \wedge ((r1_integr15 X5 (k3_integra5 X0 X1) \\
& X6) \wedge ((r1_integra5 (k3_integra5 X0 X1) (k1_nfcont_4 X5 k1_numbers \\
& X6)) \wedge ((v3_integr15 (k2_partfun1 k1_numbers (k1_euclid X5) X6 \\
& (k3_integra5 X0 X1)) X5) \wedge ((r1_tarski (k3_integra5 X0 X1) (k1_relset_1 \\
& k1_numbers X6)) \wedge ((X2 \in k3_integra5 X0 X1) \wedge ((X3 \in k3_integra5 X0 \\
& X1) \wedge (\forall X7.(v1_xreal_0 X7) \Rightarrow ((X7 \in k3_integra5 X2 X3) \Rightarrow (r1_xxreal_0 \\
& (k12_euclid (k7_partfun1 (k1_euclid X5) X6 X7)) X4)))))))))) \Rightarrow \\
& (r1_xxreal_0 (k12_euclid (k12_integr15 X2 X3 X5 X6)) (k11_binop_2 \\
& X4 (k10_binop_2 X3 X2)))))))))
\end{aligned} \tag{2}$$

Theorem 1

$$\begin{aligned}
& \forall X0.(v1_xreal_0 X0) \Rightarrow (\forall X1.(v1_xreal_0 X1) \Rightarrow (\forall X2. \\
& (v1_xreal_0 X2) \Rightarrow (\forall X3.(v1_xreal_0 X3) \Rightarrow (\forall X4.(v1_xreal_0 \\
& X4) \Rightarrow (\forall X5.((\neg v1_xboole_0 X5) \wedge (m2_subset_1 X5 k1_numbers \\
& k5_numbers)) \Rightarrow (\forall X6.((v1_funct_1 X6) \wedge (m1_subset_1 X6 (\\
& k1_zfmisc_1 (k2_zfmisc_1 k1_numbers (k1_euclid X5)))))) \Rightarrow (((r1_xxreal_0 \\
& X0 X1) \wedge ((r1_xxreal_0 X2 X3) \wedge ((r1_integr15 X5 (k3_integra5 X0 X1) \\
& X6) \wedge ((r1_integra5 (k3_integra5 X0 X1) (k1_nfcont_4 X5 k1_numbers \\
& X6)) \wedge ((v3_integr15 (k2_partfun1 k1_numbers (k1_euclid X5) X6 \\
& (k3_integra5 X0 X1)) X5) \wedge ((r1_tarski (k3_integra5 X0 X1) (k1_relset_1 \\
& k1_numbers X6)) \wedge ((X2 \in k3_integra5 X0 X1) \wedge ((X3 \in k3_integra5 X0 \\
& X1) \wedge (\forall X7.(v1_xreal_0 X7) \Rightarrow ((X7 \in k3_integra5 X2 X3) \Rightarrow (r1_xxreal_0 \\
& (k12_euclid (k7_partfun1 (k1_euclid X5) X6 X7)) X4)))))))))) \Rightarrow \\
& ((r1_xxreal_0 (k12_euclid (k12_integr15 X2 X3 X5 X6)) (k11_binop_2 \\
& X4 (k10_binop_2 X3 X2))) \wedge (r1_xxreal_0 (k12_euclid (k12_integr15 \\
& X3 X2 X5 X6)) (k11_binop_2 X4 (k10_binop_2 X3 X2)))))))))
\end{aligned}$$