## t24_member_1 <br> (TMPBz7PYjhUH2waSZjzvtK86SU18zJU19Vc)

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Let $v 2 \_$membered : $\iota \Rightarrow 0$ be given. Let $r 1 \_$tarski : $\iota \Rightarrow \iota \Rightarrow 0$ be given. Let $k 6 \_m e m b e r \_1: \iota \Rightarrow \iota$ be given. Let $k 3 \_x b o o l e \_0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 2 \_\right.$membered $\left.X 0\right) \Rightarrow(\forall X 1$. (v2_membered $X 1) \Rightarrow(($
$\left.\left.\left.r 1 \_t a r s k i X 0 X 1\right) \Rightarrow\left(r 1 \_t a r s k i\left(k 6 \_m e m b e r \_1 X 0\right)\left(k 6 \_m e m b e r \_1 X 1\right)\right)\right)\right)$
Assume the following.

$$
\begin{align*}
& \forall X 0 . \forall X 1 . \forall X 2 .\left(( r 1 \_ \text { tarski } X 0 X 1 ) \wedge \left(r 1 \_\right.\right. \text {tarski } \\
& X 0 X 2)) \Rightarrow\left(r 1 \_t a r s k i X 0\left(k 3 \_x b o o l e \_0 X 1 X 2\right)\right) \tag{2}
\end{align*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . r 1 \_t a r s k i\left(k 3 \_x b o o l e \_0 X 0 X 1\right) X 0 \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(v 2 \_m e m b e r e d X 0\right) \Rightarrow\left(v 2 \_ m e m b e r e d ~ \left(k 3 \_x b o o l e \_0\right.\right.  \tag{4}\\
X 0 X 1))
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . k 3 \_x b o o l e \_0 X 0 X 1=k 3 \_x b o o l e \_0 X 1 X 0 \tag{5}
\end{equation*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d X 1\right) \Rightarrow\left(r 1 \_t a r s k i\right.\right.$
$\left(k 6 \_m e m b e r \_1\left(k 3 \_x b o o l e \_0 X 0 X 1\right)\right)\left(k 3 \_x b o o l e \_0\left(k 6 \_m e m b e r \_1 X 0\right)\right.$
$\left.\left.\left.\left(k 6 \_m e m b e r \_1 X 1\right)\right)\right)\right)$

