

# t25\_facirc\_1 (TMMkoNXepXGsB- MXsyzyrEeZpU2SyKoGuQfr)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_circcomb : \iota \Rightarrow o$  be given. Let  $v2\_circcomb : \iota \Rightarrow o$  be given. Let  $v3\_circcomb : \iota \Rightarrow o$  be given. Let  $l1\_msualg\_1 : \iota \Rightarrow o$  be given. Let  $v4\_msafree2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v6\_circcomb : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_circcomb : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_circcomb : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v4\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_msualg\_1 X0)) \Rightarrow (\forall X1. \\ & ((\neg v2\_struct\_0 X1) \wedge (l1\_msualg\_1 X1)) \Rightarrow (\forall X2.(l3\_msualg\_1 \\ & X2 X0) \Rightarrow (\forall X3.(l3\_msualg\_1 X3 X1) \Rightarrow (((v6\_circcomb X2 X0) \wedge \\ & (v6\_circcomb X3 X1)) \Rightarrow (r1\_partfun1 (u3\_msualg\_1 X0 X2) (u3\_msualg\_1 \\ & X1 X3)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_msualg\_1 X0)) \Rightarrow (\forall X1. \\ & ((\neg v2\_struct\_0 X1) \wedge (l1\_msualg\_1 X1)) \Rightarrow (\forall X2.((\neg v2\_struct\_0 \\ & X2) \wedge (l1\_msualg\_1 X2)) \Rightarrow (\forall X3.((v4\_msualg\_1 X3 X0) \wedge (l3\_msualg\_1 \\ & X3 X0)) \Rightarrow (\forall X4.((v4\_msualg\_1 X4 X1) \wedge (l3\_msualg\_1 X4 X1)) \Rightarrow \\ & (\forall X5.((v4\_msualg\_1 X5 X2) \wedge (l3\_msualg\_1 X5 X2)) \Rightarrow (((r1\_partfun1 \\ & (u3\_msualg\_1 X0 X3) (u3\_msualg\_1 X1 X4)) \wedge ((r1\_partfun1 (u3\_msualg\_1 \\ & X1 X4) (u3\_msualg\_1 X2 X5)) \wedge (r1\_partfun1 (u3\_msualg\_1 X2 X5) (u3\_msualg\_1 \\ & X0 X3)))) \Rightarrow (k3\_circcomb (k2\_circcomb X0 X1) X2 (k3\_circcomb X0 X1 \\ & X3 X4) X5 = k3\_circcomb X0 (k2\_circcomb X1 X2) X3 (k3\_circcomb X1 X2 \\ & X4 X5)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_msualg\_1 X0)) \Rightarrow (\forall X1. \\ & (l3\_msualg\_1 X1 X0) \Rightarrow ((v6\_circcomb X1 X0) \Rightarrow ((v4\_msualg\_1 X1 X0) \wedge \\ & (v4\_msafree2 X1 X0)))) \end{aligned} \tag{3}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v1\_circcomb \\ & X0) \wedge ((v2\_circcomb X0) \wedge ((v3\_circcomb X0) \wedge (l1\_msualg\_1 X0)))))) \Rightarrow \\ & (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((\neg v11\_struct\_0 X1) \wedge ((v1\_circcomb \\ & X1) \wedge ((v2\_circcomb X1) \wedge ((v3\_circcomb X1) \wedge (l1\_msualg\_1 X1)))))) \Rightarrow \\ & (\forall X2.((\neg v2\_struct\_0 X2) \wedge ((\neg v11\_struct\_0 X2) \wedge ((v1\_circcomb \\ & X2) \wedge ((v2\_circcomb X2) \wedge ((v3\_circcomb X2) \wedge (l1\_msualg\_1 X2)))))) \Rightarrow \\ & (\forall X3.((v4\_msafree2 X3 X0) \wedge ((v6\_circcomb X3 X0) \wedge (l3\_msualg\_1 \\ & X3 X0))) \Rightarrow (\forall X4.((v4\_msafree2 X4 X1) \wedge ((v6\_circcomb X4 X1) \wedge \\ & (l3\_msualg\_1 X4 X1))) \Rightarrow (\forall X5.((v4\_msafree2 X5 X2) \wedge ((v6\_circcomb \\ & X5 X2) \wedge (l3\_msualg\_1 X5 X2)))) \Rightarrow (k3\_circcomb (k2\_circcomb X0 X1) \\ & X2 (k3\_circcomb X0 X1 X3 X4) X5 = k3\_circcomb X0 (k2\_circcomb X1 X2) \\ & X3 (k3\_circcomb X1 X2 X4 X5)))))) \end{aligned}$$