# t25_member_1 <br> (TMLiA2B2hTPn9nGvAj3zviNjuLTMHZjdkRW) 

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Let $v 2 \_$membered : $\iota \Rightarrow 0$ be given. Let $k 4 \_$member_1 : $\iota \Rightarrow \iota$ be given. Let $k 6 \_m e m b e r \_1: \iota \Rightarrow \iota$ be given. Let $v 1 \_x x r e a l \_0: \iota \Rightarrow o$ be given. Let $k 5 \_x x r e a l \_3$ : $\iota \Rightarrow \iota$ be given. Let $k 2 \_x$ xreal_3 : $\iota \Rightarrow \iota$ be given. Let $m 1 \_$subset $\_1: \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k 7$ _numbers : $\iota$ be given. Let $k 2$ _member_ $1: \iota \Rightarrow \iota$ be given. Let $k 1 \_m e m b e r \_1: \iota \Rightarrow \iota$ be given. Assume the following.

$$
\begin{align*}
\forall X 0 .\left(v 1 \_x x r e a l \_0 ~ X 0\right) \Rightarrow & \left(k 5 \_x x r e a l \_3\left(k 2 \_x x r e a l \_3 X 0\right)=k 2 \_x x r e a l \_3\right. \\
& \left.\left(k 5 \_x x r e a l \_3 X 0\right)\right) \tag{1}
\end{align*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x x r e a l \_0 X 1\right) \Rightarrow(( \right. \\
\left.\left.\left.k 2 \_x x r e a l \_3 X 1 \in X 0\right) \Leftrightarrow\left(X 1 \in k 4 \_m e m b e r \_1 X 0\right)\right)\right) \tag{2}
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(m 1 \_s u b s e t \_1 \quad X 0\right.$ $\left.k 7 \_n u m b e r s\right) \Rightarrow\left(k 2 \_m e m b e r \_1 X 0=k 5 \_x x r e a l \_3\right.$

$$
\begin{equation*}
X 0) \tag{3}
\end{equation*}
$$

Assume the following.
$\forall X 0 .\left(m 1 \_\right.$subset_1 $X 0$ k7_numbers $) \Rightarrow\left(k 1 \_m e m b e r \_1 X 0=k 2 \_x x r e a l \_3\right.$ X0)

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(k 4 \_m e m b e r \_1\left(k 4 \_m e m b e r \_1 X 0\right)=X 0\right) \tag{5}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x x r e a l \_0 X 0\right) \Rightarrow\left(k 2 \_x x r e a l \_3\left(k 2 \_x x r e a l \_3 X 0\right)=X 0\right) \tag{6}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(m 1 \_s u b s e t \_1 X 0 \text { k7_numbers }\right) \Rightarrow\left(k 1 \_ m e m b e r \_ 1 \left(k 1 \_m e m b e r \_1\right.\right.  \tag{7}\\
X 0)=X 0)
\end{gather*}
$$

Assume the following.

$$
v 2 \_m e m b e r e d ~ k 7 \_n u m b e r s
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d\left(k 6 \_m e m b e r \_1 X 0\right)\right) \tag{9}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d\left(k 4 \_m e m b e r \_1 X 0\right)\right) \tag{10}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(m 1 \_s u b s e t \_1 X 0 \text { k7_numbers }\right) \Rightarrow\left(m 1 \_ s u b s e t \_ 1 \left(k 1 \_m e m b e r \_1\right.\right. \\
\left.X 0) k 7 \_n u m b e r s\right) \tag{11}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .(v 2 \text { _membered X0 }) \Rightarrow(\text { k6_member_1 } X 0=\text { ReplSep (toset }( \\
\left.\left.\lambda X 1: \iota . m 1 \_ \text {subset_1 X1 k7_numbers }\right)\right)(\lambda X 1: \iota . X 1 \in X 0)(  \tag{12}\\
\left.\left.\lambda X 1: \iota . k 2 \_m e m b e r \_1 X 1\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(k 4 \_m e m b e r \_1 X 0=\text { ReplSep }(\text { toset }( \right. \\
\left.\left.\lambda X 1: \iota . m 1 \_ \text {subset_1 X1 k7_numbers }\right)\right)(\lambda X 1: \iota . X 1 \in X 0)(  \tag{13}\\
\left.\left.\lambda X 1: \iota . k 1 \_m e m b e r \_1 X 1\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow(( \right.  \tag{14}\\
\left.\left.X 0=X 1) \Leftrightarrow\left(\forall X 2 .\left(v 1 \_x x r e a l \_0 X 2\right) \Rightarrow((X 2 \in X 0) \Leftrightarrow(X 2 \in X 1))\right)\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(m 1 \_s u b s e t \_1 X 1 X 0\right) \Rightarrow\right. \\
\left.\left(v 1 \_x x r e a l \_0 X 1\right)\right) \tag{15}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(k 4 \_m e m b e r \_1\left(k 6 \_m e m b e r \_1 X 0\right)=k 6 \_m e m b e r \_1\right.$

