

t25_rfunct_2 (TMWQbzbvtd- drum13yYXCHBA2NLVrGPKmBfkg)

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Let $v1_funct.1 : \iota \Rightarrow o$ be given. Let $m1_subset.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc.1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_numbers : \iota$ be given. Let $v8_valued.0 : \iota \Rightarrow o$ be given. Let $k2_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k9_subset.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_relset.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_xxreal.0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_seq.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_xxreal.0 : \iota \Rightarrow o$ be given. Let $v1_relat.1 : \iota \Rightarrow o$ be given. Let $v3_valued.0 : \iota \Rightarrow o$ be given. Let $k1_funct.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v2_valued.0 : \iota \Rightarrow o$ be given. Let $v3_membered : \iota \Rightarrow o$ be given. Let $v2_membered : \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1_funct.1 X1) \wedge (m1_subset.1 X1 (k1_zfmisc.1 \\ & (k2_zfmisc.1 k1_numbers k1_numbers)))) \Rightarrow ((v8_valued.0 (k2_partfun1 \\ & k1_numbers k1_numbers X1 X0)) \Leftrightarrow (\forall X2. (m1_subset.1 X2 k1_numbers) \Rightarrow \\ & (\forall X3. (m1_subset.1 X3 k1_numbers) \Rightarrow (((X2 \in k9_subset.1 k1_numbers \\ & X0 (k1_relset.1 k1_numbers X1)) \wedge (X3 \in k9_subset.1 k1_numbers X0 \\ & (k1_relset.1 k1_numbers X1))) \Rightarrow ((r1_xxreal.0 X3 X2) \vee (r1_xxreal.0 \\ & (k1_seq.1 X1 X3) (k1_seq.1 X1 X2)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. (v1_xxreal.0 X0) \Rightarrow (\forall X1. (v1_xxreal.0 X1) \Rightarrow ((r1_xxreal.0 X0 X1) \wedge (r1_xxreal.0 X1 X0)) \Rightarrow (X0 = X1)) \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. ((v1_xxreal.0 X0) \wedge (v1_xxreal.0 X1)) \Rightarrow (r1_xxreal.0 X0 X0) \tag{3}$$

Assume the following.

$$\forall X0. \forall X1. ((v1_relat.1 X0) \wedge ((v1_funct.1 X0) \wedge (v3_valued.0 X0))) \Rightarrow (k1_seq.1 X0 X1 = k1_funct.1 X0 X1) \tag{4}$$

Assume the following.

$$\forall X0. \forall X1. ((v1_relat.1 X0) \wedge ((v1_funct.1 X0) \wedge (v2_valued.0 X0))) \Rightarrow (v1_xxreal.0 (k1_funct.1 X0 X1)) \tag{5}$$

Assume the following.

$$v3_membered\ k1_numbers \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.((v1_xxreal_0\ X0)\wedge(v1_xxreal_0\ X1))\Rightarrow((r1_xxreal_0\ X0\ X1)\vee(r1_xxreal_0\ X1\ X0)) \quad (7)$$

Assume the following.

$$\forall X0.(v3_membered\ X0)\Rightarrow(v2_membered\ X0) \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1_subset_1\ X2\ (k1_zfmisc_1\ (k2_zfmisc_1\ X0\ X1)))\Rightarrow(v1_relat_1\ X2) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.(v3_membered\ X1)\Rightarrow(\forall X2.(m1_subset_1\ X2\ (k1_zfmisc_1\ (k2_zfmisc_1\ X0\ X1)))\Rightarrow(v3_valued_0\ X2)) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.(v2_membered\ X1)\Rightarrow(\forall X2.(m1_subset_1\ X2\ (k1_zfmisc_1\ (k2_zfmisc_1\ X0\ X1)))\Rightarrow(v2_valued_0\ X2)) \quad (11)$$

Assume the following.

$$\forall X0.(v2_membered\ X0)\Rightarrow(\forall X1.(m1_subset_1\ X1\ X0)\Rightarrow(v1_xxreal_0\ X1)) \quad (12)$$

Theorem 1

$$\begin{aligned} & \forall X0.\forall X1.((v1_funct_1\ X1)\wedge(m1_subset_1\ X1\ (k1_zfmisc_1\ (k2_zfmisc_1\ k1_numbers\ k1_numbers))))\Rightarrow((v8_valued_0\ (k2_partfun1\ k1_numbers\ k1_numbers\ X1\ X0))\Leftrightarrow(\forall X2.(m1_subset_1\ X2\ k1_numbers)\Rightarrow \\ & (\forall X3.(m1_subset_1\ X3\ k1_numbers)\Rightarrow(((X2 \in k9_subset_1\ k1_numbers\ X0\ (k1_relset_1\ k1_numbers\ X1))\wedge((X3 \in k9_subset_1\ k1_numbers\ X0\ (k1_relset_1\ k1_numbers\ X1))\wedge(r1_xxreal_0\ X2\ X3))\Rightarrow(r1_xxreal_0\ (k1_seq_1\ X1\ X3)\ (k1_seq_1\ X1\ X2)))))) \end{aligned}$$