

t25\_substlat  
(TMR7sCPW6VMHRNaAqgYbK2F1HSey6Xkb2D4)

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Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_finsub\_1 : \iota \Rightarrow \iota$  be given. Let  $k4\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_substlat : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_substlat : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_substlat : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (m1\_subset\_1 X2 (k5\_finsub\_1 \\ & (k4\_partfun1 X0 X1))) \Rightarrow (k3\_substlat X0 X1 (k4\_substlat X0 X1 X2 X2) = \\ & \quad k3\_substlat X0 X1 X2) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (m2\_subset\_1 X2 (k5\_finsub\_1 \\ & (k4\_partfun1 X0 X1)) (k1\_substlat X0 X1)) \Rightarrow (k3\_substlat X0 X1 X2 = \\ & \quad X2) \end{aligned} \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. \neg v1\_xboole\_0 (k1\_substlat X0 X1) \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))) \Rightarrow (\forall X2. (m2\_subset\_1 \\ & \quad X2 X0 X1) \Rightarrow (m1\_subset\_1 X2 X0)) \end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. m1\_subset\_1 (k1\_substlat X0 X1) (k1\_zfmisc\_1 \\ & \quad (k5\_finsub\_1 (k4\_partfun1 X0 X1))) \end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned} & \forall X0. (v1\_xboole\_0 X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & \quad X0)) \Rightarrow (v1\_xboole\_0 X1)) \end{aligned} \tag{6}$$

**Theorem 1**

$$\forall X0.\forall X1.\forall X2.(m2\_subset\_1 X2 (k5\_finsub\_1 (k4\_partfun1 X0 X1)) (k1\_substlat X0 X1)) \Rightarrow (k3\_substlat X0 X1 (k4\_substlat X0 X1 X2 X2) = X2)$$