

t26\_midsp\_2 (TMZc-  
QAMqvfgv2mADEBUtKpDuYoT2oxQdmC8)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v2\_midsp\_2 : \iota \Rightarrow o$  be given. Let  $l2\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $r1\_midsp\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_midsp\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k7\_midsp\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $g1\_midsp\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_midsp\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_binop\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_binop\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_midsp\_1 : \iota \Rightarrow o$  be given. Let  $l1\_midsp\_1 : \iota \Rightarrow o$  be given. Let  $k1\_midsp\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_midsp\_1 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. ((\neg v2\_struct\_0 X1) \wedge \\
 & ((v13\_algstr\_0 X1) \wedge ((v2\_rlvect\_1 X1) \wedge ((v3\_rlvect\_1 X1) \wedge ((v4\_rlvect\_1 \\
 & X1) \wedge ((v2\_midsp\_2 X1) \wedge (l2\_algstr\_0 X1))))))) \Rightarrow (\forall X2. (( \\
 & v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k2\_zfmisc\_1 X0 X0) (u1\_struct\_0 \\
 & X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 \\
 & X0 X0) (u1\_struct\_0 X1)))))) \Rightarrow ((r1\_midsp\_2 X0 X1 X2) \Rightarrow (\forall X3. \\
 & (m1\_subset\_1 X3 X0) \Rightarrow (\forall X4. (m1\_subset\_1 X4 X0) \Rightarrow (\forall X5. \\
 & (m1\_subset\_1 X5 X0) \Rightarrow ((k5\_binop\_1 X0 (k6\_midsp\_2 X0 X1 X2) X3 X4 = \\
 & X5) \Leftrightarrow (k2\_binop\_1 X0 X0 (u1\_struct\_0 X1) X2 X3 X5 = k2\_binop\_1 X0 X0 \\
 & (u1\_struct\_0 X1) X2 X5 X4))))))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
 & \forall X0. \forall X1. ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 (k2\_zfmisc\_1 \\
 & X0 X0) X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 \\
 & X0 X0) X0)))) \Rightarrow (\forall X2. \forall X3. (g1\_midsp\_1 X0 X1 = g1\_midsp\_1 \\
 & X2 X3) \Rightarrow ((X0 = X2) \wedge (X1 = X3)))
 \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v1\_xboole\_0 X0) \wedge ((v1\_funct\_1 X1) \wedge \\ & (v1\_funct\_2 X1 (k2\_zfmisc\_1 X0 X0) X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0) X0)))))) \Rightarrow ((\neg v2\_struct\_0 (g1\_midsp\_1 \\ & X0 X1)) \wedge (v1\_midsp\_1 (g1\_midsp\_1 X0 X1))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((\neg v1\_xboole\_0 X0) \wedge (((\neg v2\_struct\_0 \\ & X1) \wedge ((v13\_algstr\_0 X1) \wedge ((v2\_rlvect\_1 X1) \wedge ((v3\_rlvect\_1 X1) \wedge \\ & ((v4\_rlvect\_1 X1) \wedge ((v2\_midsp\_2 X1) \wedge (l2\_algstr\_0 X1)))))) \wedge \\ & ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k2\_zfmisc\_1 X0 X0) (u1\_struct\_0 \\ & X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X0) (u1\_struct\_0 X1)))))) \Rightarrow ((v1\_funct\_1 (k7\_midsp\_2 X0 X1 \\ & X2)) \wedge ((v1\_funct\_2 (k7\_midsp\_2 X0 X1 X2) (k2\_zfmisc\_1 (u1\_struct\_0 \\ & (g1\_midsp\_1 X0 (k6\_midsp\_2 X0 X1 X2))) (u1\_struct\_0 (g1\_midsp\_1 \\ & X0 (k6\_midsp\_2 X0 X1 X2))) (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 (k7\_midsp\_2 \\ & X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 \\ & (g1\_midsp\_1 X0 (k6\_midsp\_2 X0 X1 X2))) (u1\_struct\_0 (g1\_midsp\_1 \\ & X0 (k6\_midsp\_2 X0 X1 X2))) (u1\_struct\_0 X1)))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((\neg v1\_xboole\_0 X0) \wedge (((\neg v2\_struct\_0 \\ & X1) \wedge ((v13\_algstr\_0 X1) \wedge ((v2\_rlvect\_1 X1) \wedge ((v3\_rlvect\_1 X1) \wedge \\ & ((v4\_rlvect\_1 X1) \wedge ((v2\_midsp\_2 X1) \wedge (l2\_algstr\_0 X1)))))) \wedge \\ & ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k2\_zfmisc\_1 X0 X0) (u1\_struct\_0 \\ & X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X0) (u1\_struct\_0 X1)))))) \Rightarrow ((v1\_funct\_1 (k6\_midsp\_2 X0 X1 \\ & X2)) \wedge ((v1\_funct\_2 (k6\_midsp\_2 X0 X1 X2) (k2\_zfmisc\_1 X0 X0) X0) \wedge \\ & (m1\_subset\_1 (k6\_midsp\_2 X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 ( \\ & k2\_zfmisc\_1 X0 X0) X0)))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 (k2\_zfmisc\_1 \\ & X0 X0) X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X0) X0)))) \Rightarrow ((v1\_midsp\_1 (g1\_midsp\_1 X0 X1)) \wedge (l1\_midsp\_1 ( \\ & g1\_midsp\_1 X0 X1))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_midsp\_1 X0)) \Rightarrow (\forall X1. \\
& ((\neg v2\_struct\_0 X1) \wedge (l2\_algstr\_0 X1)) \Rightarrow (\forall X2.((v1\_funct\_1 \\
& X2) \wedge ((v1\_funct\_2 X2 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0)) (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0)) (u1\_struct\_0 \\
& X1)))))) \Rightarrow ((v1\_midsp\_2 X2 X0 X1) \Leftrightarrow (\forall X3.(m1\_subset\_1 X3 ( \\
& u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow ((k1\_midsp\_1 X0 \\
& X3 X4 = X5) \Leftrightarrow (k2\_binop\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X1) X2 X3 X5 = k2\_binop\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X1) X2 X5 X4)))))))))
\end{aligned} \tag{7}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_midsp\_1 X0)) \Rightarrow (\forall X1. \\
& (m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 \\
& (u1\_struct\_0 X0)) \Rightarrow (k1\_midsp\_1 X0 X1 X2 = k5\_binop\_1 (u1\_struct\_0 \\
& X0) (u1\_midsp\_1 X0) X1 X2)))
\end{aligned} \tag{8}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge \\
& ((v13\_algstr\_0 X1) \wedge ((v2\_rlvect\_1 X1) \wedge ((v3\_rlvect\_1 X1) \wedge ((v4\_rlvect\_1 \\
& X1) \wedge ((v2\_midsp\_2 X1) \wedge (l2\_algstr\_0 X1)))))) \Rightarrow (\forall X2.(( \\
& v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k2\_zfmisc\_1 X0 X0) (u1\_struct\_0 \\
& X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 \\
& X0 X0) (u1\_struct\_0 X1)))))) \Rightarrow (k7\_midsp\_2 X0 X1 X2 = X2)))
\end{aligned} \tag{9}$$

Assume the following.

$$\forall X0.(l1\_midsp\_1 X0) \Rightarrow ((v1\_midsp\_1 X0) \Rightarrow (X0 = g1\_midsp\_1 (u1\_struct\_0 X0) (u1\_midsp\_1 X0))) \tag{10}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge \\
& ((v13\_algstr\_0 X1) \wedge ((v2\_rlvect\_1 X1) \wedge ((v3\_rlvect\_1 X1) \wedge ((v4\_rlvect\_1 \\
& X1) \wedge ((v2\_midsp\_2 X1) \wedge (l2\_algstr\_0 X1)))))) \Rightarrow (\forall X2.(( \\
& v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k2\_zfmisc\_1 X0 X0) (u1\_struct\_0 \\
& X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 \\
& X0 X0) (u1\_struct\_0 X1)))))) \Rightarrow ((r1\_midsp\_2 X0 X1 X2) \Rightarrow (v1\_midsp\_2 \\
& (k7\_midsp\_2 X0 X1 X2) (g1\_midsp\_1 X0 (k6\_midsp\_2 X0 X1 X2)) X1)))
\end{aligned}$$