

t26\_qc\_lang3  
(TMccexr3GaHybHa5r2YsJuRwrhqtuUiCZBD)

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Let  $m1\_qc\_lang1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k9\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Let  $v6\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_qc\_lang2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k14\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k13\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k9\_qc\_lang1 \\ X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k9\_qc\_lang1 X0)) \Rightarrow (((v6\_qc\_lang1 \\ X1 X0) \wedge (v6\_qc\_lang1 X2 X0)) \Leftrightarrow (v6\_qc\_lang1 (k14\_qc\_lang1 X0 X1 X2) \\ X0)))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k9\_qc\_lang1 \\ X0)) \Rightarrow ((v6\_qc\_lang1 X1 X0) \Leftrightarrow (v6\_qc\_lang1 (k13\_qc\_lang1 X0 X1) X0))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.((m1\_qc\_lang1 X0) \wedge ((m1\_subset\_1 \\ X1 (k9\_qc\_lang1 X0)) \wedge (m1\_subset\_1 X2 (k9\_qc\_lang1 X0)))) \Rightarrow (m1\_subset\_1 \\ (k14\_qc\_lang1 X0 X1 X2) (k9\_qc\_lang1 X0)) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((m1\_qc\_lang1 X0) \wedge (m1\_subset\_1 X1 (k9\_qc\_lang1 \\ X0))) \Rightarrow (m1\_subset\_1 (k13\_qc\_lang1 X0 X1) (k9\_qc\_lang1 X0)) \end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k9\_qc\_lang1 \\ X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k9\_qc\_lang1 X0)) \Rightarrow (k2\_qc\_lang2 \\ X0 X1 X2 = k13\_qc\_lang1 X0 (k14\_qc\_lang1 X0 X1 (k13\_qc\_lang1 X0 X2)))))) \end{aligned} \tag{5}$$

**Theorem 1**

$$\begin{aligned} \forall X0.(m1\_qc\_lang1\ X0) \Rightarrow (\forall X1.(m1\_subset\_1\ X1\ (k9\_qc\_lang1 \\ X0)) \Rightarrow (\forall X2.(m1\_subset\_1\ X2\ (k9\_qc\_lang1\ X0)) \Rightarrow (((v6\_qc\_lang1 \\ X1\ X0) \wedge (v6\_qc\_lang1\ X2\ X0)) \Leftrightarrow (v6\_qc\_lang1\ (k2\_qc\_lang2\ X0\ X1\ X2) \\ X0)))) \end{aligned}$$