

## t26\_sin\_cos4

(TMcvSyhPg65ZCg1T316UaGDU279hGgJtxuN)

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Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $k6\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k17\_sin\_cos : \iota \Rightarrow \iota$  be given. Let  $k2\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_2 : \iota$  be given. Let  $k20\_sin\_cos : \iota \Rightarrow \iota$  be given. Let  $v1\_xcmplx\_0 : \iota \Rightarrow o$  be given. Let  $k7\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_xcmplx\_0 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xcmplx\_0 X0) \Rightarrow (\forall X1.(v1\_xcmplx\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xcmplx\_0 X2) \Rightarrow (k2\_xcmplx\_0 X0 X1 = k2\_xcmplx\_0 (k2\_xcmplx\_0 \\ & X0 X2) (k6\_xcmplx\_0 X1 X2)))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xreal\_0 X0) \Rightarrow (\forall X1.(v1\_xreal\_0 X1) \Rightarrow (k2\_xcmplx\_0 \\ & (k17\_sin\_cos (k2\_xcmplx\_0 X0 X1)) (k17\_sin\_cos (k6\_xcmplx\_0 X0 \\ & X1)) = k3\_xcmplx\_0 np\_2 (k3\_xcmplx\_0 (k17\_sin\_cos X0) (k20\_sin\_cos \\ & X1)))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xcmplx\_0 X0) \Rightarrow (\forall X1.(v1\_xcmplx\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xcmplx\_0 X2) \Rightarrow (k6\_xcmplx\_0 (k6\_xcmplx\_0 X0 X1) (k6\_xcmplx\_0 \\ & X0 X2) = k6\_xcmplx\_0 X2 X1))) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xreal\_0 X0) \Rightarrow (\forall X1.(v1\_xreal\_0 X1) \Rightarrow (k6\_xcmplx\_0 \\ & (k17\_sin\_cos X0) (k17\_sin\_cos X1) = k3\_xcmplx\_0 np\_2 (k3\_xcmplx\_0 \\ & (k20\_sin\_cos (k7\_xcmplx\_0 (k2\_xcmplx\_0 X0 X1) np\_2)) (k17\_sin\_cos \\ & (k7\_xcmplx\_0 (k6\_xcmplx\_0 X0 X1) np\_2)))) \end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned} \forall X0.(v1\_xreal\_0 X0) \Rightarrow (\forall X1.(v1\_xreal\_0 X1) \Rightarrow (k2\_xcmplx\_0 \\ (k17\_sin\_cos X0) (k17\_sin\_cos X1) = k3\_xcmplx\_0 \text{ np\_2} (k3\_xcmplx\_0 \\ (k20\_sin\_cos (k7\_xcmplx\_0 (k6\_xcmplx\_0 X0 X1) \text{ np\_2})) (k17\_sin\_cos \\ (k7\_xcmplx\_0 (k2\_xcmplx\_0 X0 X1) \text{ np\_2})))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1\_xcmplx\_0 X0) \wedge (v1\_xcmplx\_0 X1)) \Rightarrow ( \\ k6\_xcmplx\_0 (k4\_xcmplx\_0 X0) (k4\_xcmplx\_0 X1) = k6\_xcmplx\_0 X1 \\ X0) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1\_xcmplx\_0 X0) \wedge (v1\_xcmplx\_0 X1)) \Rightarrow ( \\ k2\_xcmplx\_0 X0 (k4\_xcmplx\_0 X1) = k6\_xcmplx\_0 X0 X1) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0.(v1\_xcmplx\_0 X0) \Rightarrow (k4\_xcmplx\_0 (k4\_xcmplx\_0 X0) = X0) \quad (8)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1\_xreal\_0 X0) \wedge (v1\_xreal\_0 X1)) \Rightarrow (v1\_xreal\_0 \\ (k6\_xcmplx\_0 X0 X1)) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1\_xreal\_0 X0) \wedge (v1\_xreal\_0 X1)) \Rightarrow (v1\_xreal\_0 \\ (k2\_xcmplx\_0 X0 X1)) \end{aligned} \quad (10)$$

Assume the following.

$$\forall X0.(v1\_xreal\_0 X0) \Rightarrow (v1\_xreal\_0 (k20\_sin\_cos X0)) \quad (11)$$

Assume the following.

$$\begin{aligned} \forall X0.(v1\_xreal\_0 X0) \Rightarrow ((v1\_xcmplx\_0 (k4\_xcmplx\_0 X0)) \wedge \\ (v1\_xreal\_0 (k4\_xcmplx\_0 X0))) \end{aligned} \quad (12)$$

Assume the following.

$$\forall X0.(v1\_xreal\_0 X0) \Rightarrow (v1\_xreal\_0 (k17\_sin\_cos X0)) \quad (13)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1\_xcmplx\_0 X0) \wedge (v1\_xcmplx\_0 X1)) \Rightarrow ( \\ k3\_xcmplx\_0 X0 X1 = k3\_xcmplx\_0 X1 X0) \end{aligned} \quad (14)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xcmplx\_0 X0)\wedge(v1\_xcmplx\_0 X1))\Rightarrow( k2\_xcmplx\_0 X0 X1 = k2\_xcmplx\_0 X1 X0) \quad (15)$$

Assume the following.

$$\forall X0.(v1\_xreal\_0 X0)\Rightarrow(v1\_xcmplx\_0 X0) \quad (16)$$

**Theorem 1**

$$\forall X0.(v1\_xreal\_0 X0)\Rightarrow(\forall X1.(v1\_xreal\_0 X1)\Rightarrow(k6\_xcmplx\_0 (k17\_sin\_cos (k2\_xcmplx\_0 X0 X1)) (k17\_sin\_cos (k6\_xcmplx\_0 X0 X1)) = k3\_xcmplx\_0 np\_2 (k3\_xcmplx\_0 (k20\_sin\_cos X0) (k17\_sin\_cos X1))))$$