

## t27\_scmfsa8b

(TMXVCbxae4WWAGLHwuXXz2pvm1riHFDsmkM)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_compos\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_scmfsa\_2 : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v5\_funct\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_3 : \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $v1\_afinsq\_1 : \iota \Rightarrow o$  be given. Let  $v1\_ami\_2 : \iota \Rightarrow o$  be given. Let  $v1\_scmfsa\_m : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_numbers : \iota$  be given. Let  $r5\_scmfsa7b : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r6\_scmfsa7b : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_scmfsa8b : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_scmfsa8b : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_scmfsa8b : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v5\_relat\_1 \\
 & X0 (u1\_compos\_1 k1\_scmfsa\_2)) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 \\
 & X0 k5\_numbers)))))) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 \\
 & X1 (u1\_struct\_0 k1\_scmfsa\_2)) \wedge ((v1\_funct\_1 X1) \wedge ((v5\_funct\_1 \\
 & X1 (k2\_memstr\_0 np\_3 k1\_scmfsa\_2)) \wedge (v1\_partfun1 X1 (u1\_struct\_0 \\
 & k1\_scmfsa\_2)))))) \Rightarrow (\forall X2.((\neg v1\_xboole\_0 X2) \wedge ((v1\_relat\_1 \\
 & X2) \wedge ((v4\_relat\_1 X2 k5\_numbers) \wedge ((v5\_relat\_1 X2 (u1\_compos\_1 \\
 & k1\_scmfsa\_2)) \wedge ((v1\_funct\_1 X2) \wedge ((v1\_finset\_1 X2) \wedge (v1\_afinsq\_1 \\
 & X2)))))) \Rightarrow (\forall X3.((\neg v1\_xboole\_0 X3) \wedge ((v1\_relat\_1 X3) \wedge \\
 & ((v4\_relat\_1 X3 k5\_numbers) \wedge ((v5\_relat\_1 X3 (u1\_compos\_1 k1\_scmfsa\_2)) \wedge \\
 & ((v1\_funct\_1 X3) \wedge ((v1\_finset\_1 X3) \wedge (v1\_afinsq\_1 X3)))))) \Rightarrow \\
 & (\forall X4.((v1\_ami\_2 X4) \wedge ((\neg v1\_scmfsa\_m X4) \wedge (m1\_subset\_1 \\
 & X4 (u1\_struct\_0 k1\_scmfsa\_2)))) \Rightarrow (((k1\_funct\_1 X1 X4 = k6\_numbers) \wedge \\
 & ((r5\_scmfsa7b X2 X1 X0) \wedge (r6\_scmfsa7b X2 X1 X0)) \Rightarrow ((r5\_scmfsa7b \\
 & (k1\_scmfsa8b X4 X2 X3) X1 X0) \wedge (r6\_scmfsa7b (k1\_scmfsa8b X4 X2 X3) \\
 & X1 X0))))))
 \end{aligned}
 \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. (((v1\_ami\_2 X0) \wedge (m1\_subset\_1 \\
& X0 (u1\_struct\_0 k1\_scmfsa\_2))) \wedge (((\neg v1\_xboole\_0 X1) \wedge ((v1\_relat\_1 \\
& X1) \wedge ((v4\_relat\_1 X1 k5\_numbers) \wedge ((v5\_relat\_1 X1 (u1\_compos\_1 \\
& k1\_scmfsa\_2)) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_finset\_1 X1) \wedge (v1\_afinsq\_1 \\
& X1)))))) \wedge ((\neg v1\_xboole\_0 X2) \wedge ((v1\_relat\_1 X2) \wedge ((v4\_relat\_1 \\
& X2 k5\_numbers) \wedge ((v5\_relat\_1 X2 (u1\_compos\_1 k1\_scmfsa\_2)) \wedge \\
& (v1\_funct\_1 X2) \wedge ((v1\_finset\_1 X2) \wedge (v1\_afinsq\_1 X2)))))) \Rightarrow \\
& ((\neg v1\_xboole\_0 (k2\_scmfsa8b X0 X1 X2)) \wedge ((v1\_relat\_1 (k2\_scmfsa8b \\
& X0 X1 X2)) \wedge ((v4\_relat\_1 (k2\_scmfsa8b X0 X1 X2) k5\_numbers) \wedge ((v5\_relat\_1 \\
& (k2\_scmfsa8b X0 X1 X2) (u1\_compos\_1 k1\_scmfsa\_2)) \wedge ((v1\_funct\_1 \\
& (k2\_scmfsa8b X0 X1 X2)) \wedge ((v1\_finset\_1 (k2\_scmfsa8b X0 X1 X2)) \wedge \\
& (v1\_afinsq\_1 (k2\_scmfsa8b X0 X1 X2))))))))) \Rightarrow \\
& \hspace{15em} (2)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0. ((v1\_ami\_2 X0) \wedge (m1\_subset\_1 X0 (u1\_struct\_0 k1\_scmfsa\_2))) \Rightarrow \\
& (\forall X1. ((\neg v1\_xboole\_0 X1) \wedge ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 \\
& X1 k5\_numbers) \wedge ((v5\_relat\_1 X1 (u1\_compos\_1 k1\_scmfsa\_2)) \wedge \\
& (v1\_funct\_1 X1) \wedge ((v1\_finset\_1 X1) \wedge (v1\_afinsq\_1 X1)))))) \Rightarrow ( \\
& \quad \forall X2. ((\neg v1\_xboole\_0 X2) \wedge ((v1\_relat\_1 X2) \wedge ((v4\_relat\_1 \\
& X2 k5\_numbers) \wedge ((v5\_relat\_1 X2 (u1\_compos\_1 k1\_scmfsa\_2)) \wedge \\
& (v1\_funct\_1 X2) \wedge ((v1\_finset\_1 X2) \wedge (v1\_afinsq\_1 X2)))))) \Rightarrow ( \\
& k3\_scmfsa8b X0 X1 X2 = k1\_scmfsa8b X0 X2 (k2\_scmfsa8b X0 X2 X1))) \Rightarrow \\
& \hspace{15em} (3)
\end{aligned}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0. ((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v5\_relat\_1 \\
& X0 (u1\_compos\_1 k1\_scmfsa\_2)) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 \\
& X0 k5\_numbers)))) \Rightarrow (\forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 \\
& X1 (u1\_struct\_0 k1\_scmfsa\_2)) \wedge ((v1\_funct\_1 X1) \wedge ((v5\_funct\_1 \\
& X1 (k2\_memstr\_0 np\_3 k1\_scmfsa\_2)) \wedge (v1\_partfun1 X1 (u1\_struct\_0 \\
& k1\_scmfsa\_2)))))) \Rightarrow (\forall X2. ((\neg v1\_xboole\_0 X2) \wedge ((v1\_relat\_1 \\
& X2) \wedge ((v4\_relat\_1 X2 k5\_numbers) \wedge ((v5\_relat\_1 X2 (u1\_compos\_1 \\
& k1\_scmfsa\_2)) \wedge ((v1\_funct\_1 X2) \wedge ((v1\_finset\_1 X2) \wedge (v1\_afinsq\_1 \\
& X2)))))) \Rightarrow (\forall X3. ((\neg v1\_xboole\_0 X3) \wedge ((v1\_relat\_1 X3) \wedge \\
& ((v4\_relat\_1 X3 k5\_numbers) \wedge ((v5\_relat\_1 X3 (u1\_compos\_1 k1\_scmfsa\_2)) \wedge \\
& ((v1\_funct\_1 X3) \wedge ((v1\_finset\_1 X3) \wedge (v1\_afinsq\_1 X3)))))) \Rightarrow \\
& (\forall X4. ((v1\_ami\_2 X4) \wedge ((\neg v1\_scmfsa\_m X4) \wedge (m1\_subset\_1 \\
& X4 (u1\_struct\_0 k1\_scmfsa\_2)))) \Rightarrow (((k1\_funct\_1 X1 X4 = k6\_numbers) \wedge \\
& ((r5\_scmfsa7b X3 X1 X0) \wedge (r6\_scmfsa7b X3 X1 X0)) \Rightarrow ((r5\_scmfsa7b \\
& (k3\_scmfsa8b X4 X2 X3) X1 X0) \wedge (r6\_scmfsa7b (k3\_scmfsa8b X4 X2 X3) \\
& X1 X0))))))
\end{aligned}$$