

# t27\_waybel17 (TMLHRNZZs- bcgW31Gt8s2iuab2AWUtMUpCu6)

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Let  $v2\_pre\_topc : \iota \Rightarrow o$  be given. Let  $v3\_orders\_2 : \iota \Rightarrow o$  be given. Let  $v4\_orders\_2 : \iota \Rightarrow o$  be given. Let  $v5\_orders\_2 : \iota \Rightarrow o$  be given. Let  $v1\_lattice3 : \iota \Rightarrow o$  be given. Let  $v2\_lattice3 : \iota \Rightarrow o$  be given. Let  $v3\_lattice3 : \iota \Rightarrow o$  be given. Let  $v4\_waybel11 : \iota \Rightarrow o$  be given. Let  $l1\_waybel\_9 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_waybel\_8 : \iota \Rightarrow o$  be given. Let  $v5\_pre\_topc : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_waybel\_8 : \iota \Rightarrow \iota$  be given. Let  $r3\_orders\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_orders\_2 : \iota \Rightarrow o$  be given. Let  $v3\_waybel\_3 : \iota \Rightarrow o$  be given. Let  $r1\_waybel\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. ((v3\_orders\_2 X0) \wedge ((v4\_orders\_2 X0) \wedge ((v5\_orders\_2 \\
& X0) \wedge ((v1\_lattice3 X0) \wedge ((v2\_lattice3 X0) \wedge (l1\_orders\_2 X0)))))) \Rightarrow \\
& ((v2\_waybel\_8 X0) \Leftrightarrow ((v3\_waybel\_3 X0) \wedge (\forall X1. (m1\_subset\_1 \\
& X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (u1\_struct\_0 \\
& X0)) \Rightarrow (\neg (r1\_waybel\_3 X0 X1 X2) \wedge (\forall X3. (m1\_subset\_1 X3 (u1\_struct\_0 \\
& X0)) \Rightarrow (\neg (X3 \in u1\_struct\_0 (k1\_waybel\_8 X0)) \wedge ((r3\_orders\_2 X0 X1 \\
& X3) \wedge (r3\_orders\_2 X0 X3 X2))))))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v2\_pre\_topc\ X0)\wedge((v3\_orders\_2\ X0)\wedge((v4\_orders\_2 \\
& X0)\wedge((v5\_orders\_2\ X0)\wedge((v1\_lattice3\ X0)\wedge((v2\_lattice3\ X0)\wedge \\
& ((v3\_lattice3\ X0)\wedge((v3\_waybel\_3\ X0)\wedge((v4\_waybel11\ X0)\wedge(l1\_waybel\_9 \\
& X0))))))))\Rightarrow(\forall X1.((v2\_pre\_topc\ X1)\wedge((v3\_orders\_2\ X1)\wedge \\
& ((v4\_orders\_2\ X1)\wedge((v5\_orders\_2\ X1)\wedge((v1\_lattice3\ X1)\wedge((v2\_lattice3 \\
& X1)\wedge((v3\_lattice3\ X1)\wedge((v3\_waybel\_3\ X1)\wedge((v4\_waybel11\ X1)\wedge \\
& (l1\_waybel\_9\ X1))))))))\Rightarrow(\forall X2.((v1\_funct\_1\ X2)\wedge((v1\_funct\_2 \\
& X2\ (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1))\wedge(m1\_subset\_1\ X2\ (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1\ (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1))))))\Rightarrow((v5\_pre\_topc \\
& X2\ X0\ X1)\Leftrightarrow(\forall X3.(m1\_subset\_1\ X3\ (u1\_struct\_0\ X0))\Rightarrow(\forall X4. \\
& (m1\_subset\_1\ X4\ (u1\_struct\_0\ X1))\Rightarrow((r1\_waybel\_3\ X1\ X4\ (k3\_funct\_2 \\
& (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1)\ X2\ X3))\Leftrightarrow(\exists X5.(m1\_subset\_1 \\
& X5\ (u1\_struct\_0\ X0))\wedge((r1\_waybel\_3\ X0\ X5\ X3)\wedge(r1\_waybel\_3\ X1\ X4 \\
& (k3\_funct\_2\ (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1)\ X2\ X5))))))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v2\_pre\_topc\ X0)\wedge((v3\_orders\_2\ X0)\wedge((v4\_orders\_2 \\
& X0)\wedge((v5\_orders\_2\ X0)\wedge((v1\_lattice3\ X0)\wedge((v2\_lattice3\ X0)\wedge \\
& ((v3\_lattice3\ X0)\wedge((v4\_waybel11\ X0)\wedge(l1\_waybel\_9\ X0))))))))\Rightarrow \\
& (\forall X1.((v2\_pre\_topc\ X1)\wedge((v3\_orders\_2\ X1)\wedge((v4\_orders\_2 \\
& X1)\wedge((v5\_orders\_2\ X1)\wedge((v1\_lattice3\ X1)\wedge((v2\_lattice3\ X1)\wedge \\
& ((v3\_lattice3\ X1)\wedge((v4\_waybel11\ X1)\wedge(l1\_waybel\_9\ X1))))))))\Rightarrow \\
& (\forall X2.((v1\_funct\_1\ X2)\wedge((v1\_funct\_2\ X2\ (u1\_struct\_0\ X0) \\
& (u1\_struct\_0\ X1))\wedge(m1\_subset\_1\ X2\ (k1\_zfmisc\_1\ (k2\_zfmisc\_1 \\
& (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1))))))\Rightarrow(((v2\_waybel\_8\ X1)\wedge \\
& \forall X3.(m1\_subset\_1\ X3\ (u1\_struct\_0\ X0))\Rightarrow(\forall X4.(m1\_subset\_1 \\
& X4\ (u1\_struct\_0\ X1))\Rightarrow((X4 \in u1\_struct\_0\ (k1\_waybel\_8\ X1))\Rightarrow((r3\_orders\_2 \\
& X1\ X4\ (k3\_funct\_2\ (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1)\ X2\ X3))\Leftrightarrow(\exists X5. \\
& (m1\_subset\_1\ X5\ (u1\_struct\_0\ X0))\wedge((X5 \in u1\_struct\_0\ (k1\_waybel\_8 \\
& X0))\wedge((r3\_orders\_2\ X0\ X5\ X3)\wedge(r3\_orders\_2\ X1\ X4\ (k3\_funct\_2\ (u1\_struct\_0 \\
& X0)\ (u1\_struct\_0\ X1)\ X2\ X5))))))))))\Rightarrow(\forall X3.(m1\_subset\_1 \\
& X3\ (u1\_struct\_0\ X0))\Rightarrow(\forall X4.(m1\_subset\_1\ X4\ (u1\_struct\_0 \\
& X1))\Rightarrow((r1\_waybel\_3\ X1\ X4\ (k3\_funct\_2\ (u1\_struct\_0\ X0)\ (u1\_struct\_0 \\
& X1)\ X2\ X3))\Leftrightarrow(\exists X5.(m1\_subset\_1\ X5\ (u1\_struct\_0\ X0))\wedge((r1\_waybel\_3 \\
& X0\ X5\ X3)\wedge(r1\_waybel\_3\ X1\ X4\ (k3\_funct\_2\ (u1\_struct\_0\ X0)\ (u1\_struct\_0 \\
& X1)\ X2\ X5))))))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v2\_pre\_topc\ X0)\wedge((v3\_orders\_2\ X0)\wedge((v4\_orders\_2 \\
& \quad X0)\wedge((v5\_orders\_2\ X0)\wedge((v1\_lattice3\ X0)\wedge((v2\_lattice3\ X0)\wedge \\
& \quad ((v3\_lattice3\ X0)\wedge((v4\_waybel11\ X0)\wedge(l1\_waybel\_9\ X0)))))))\Rightarrow \\
& \quad (\forall X1.((v2\_pre\_topc\ X1)\wedge((v3\_orders\_2\ X1)\wedge((v4\_orders\_2 \\
& \quad X1)\wedge((v5\_orders\_2\ X1)\wedge((v1\_lattice3\ X1)\wedge((v2\_lattice3\ X1)\wedge \\
& \quad ((v3\_lattice3\ X1)\wedge((v4\_waybel11\ X1)\wedge(l1\_waybel\_9\ X1)))))))\Rightarrow \\
& \quad (\forall X2.((v1\_funct\_1\ X2)\wedge((v1\_funct\_2\ X2\ (u1\_struct\_0\ X0) \\
& \quad (u1\_struct\_0\ X1))\wedge(m1\_subset\_1\ X2\ (k1\_zfmisc\_1\ (k2\_zfmisc\_1 \\
& \quad (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1))))))\Rightarrow(((v2\_waybel\_8\ X0)\wedge( \\
& \quad (v2\_waybel\_8\ X1)\wedge(\forall X3.(m1\_subset\_1\ X3\ (u1\_struct\_0\ X0))\Rightarrow \\
& \quad (\forall X4.(m1\_subset\_1\ X4\ (u1\_struct\_0\ X1))\Rightarrow((r1\_waybel\_3 \\
& \quad X1\ X4\ (k3\_funct\_2\ (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1)\ X2\ X3))\Leftrightarrow(\exists X5. \\
& \quad (m1\_subset\_1\ X5\ (u1\_struct\_0\ X0))\wedge((r1\_waybel\_3\ X0\ X5\ X3)\wedge(r1\_waybel\_3 \\
& \quad X1\ X4\ (k3\_funct\_2\ (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1)\ X2\ X5))))))\Rightarrow \\
& \quad (\forall X3.(m1\_subset\_1\ X3\ (u1\_struct\_0\ X0))\Rightarrow(\forall X4.(m1\_subset\_1 \\
& \quad X4\ (u1\_struct\_0\ X1))\Rightarrow((X4\ \in\ u1\_struct\_0\ (k1\_waybel\_8\ X1))\Rightarrow((r3\_orders\_2 \\
& \quad X1\ X4\ (k3\_funct\_2\ (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1)\ X2\ X3))\Leftrightarrow(\exists X5. \\
& \quad (m1\_subset\_1\ X5\ (u1\_struct\_0\ X0))\wedge((X5\ \in\ u1\_struct\_0\ (k1\_waybel\_8 \\
& \quad X0))\wedge((r3\_orders\_2\ X0\ X5\ X3)\wedge(r3\_orders\_2\ X1\ X4\ (k3\_funct\_2\ (u1\_struct\_0 \\
& \quad X0)\ (u1\_struct\_0\ X1)\ X2\ X5))))))))))
\end{aligned} \tag{4}$$

Assume the following.

$$\forall X0.(l1\_waybel\_9\ X0)\Rightarrow((l1\_pre\_topc\ X0)\wedge(l1\_orders\_2\ X0)) \tag{5}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((v2\_pre\_topc\ X0)\wedge((v3\_orders\_2\ X0)\wedge((v4\_orders\_2 \\
& \quad X0)\wedge((v5\_orders\_2\ X0)\wedge((v1\_lattice3\ X0)\wedge((v2\_lattice3\ X0)\wedge \\
& \quad ((v3\_lattice3\ X0)\wedge((v4\_waybel11\ X0)\wedge(l1\_waybel\_9\ X0)))))))\Rightarrow \\
& \quad (\forall X1.((v2\_pre\_topc\ X1)\wedge((v3\_orders\_2\ X1)\wedge((v4\_orders\_2 \\
& \quad X1)\wedge((v5\_orders\_2\ X1)\wedge((v1\_lattice3\ X1)\wedge((v2\_lattice3\ X1)\wedge \\
& \quad ((v3\_lattice3\ X1)\wedge((v4\_waybel11\ X1)\wedge(l1\_waybel\_9\ X1)))))))\Rightarrow \\
& \quad (\forall X2.((v1\_funct\_1\ X2)\wedge((v1\_funct\_2\ X2\ (u1\_struct\_0\ X0) \\
& \quad (u1\_struct\_0\ X1))\wedge(m1\_subset\_1\ X2\ (k1\_zfmisc\_1\ (k2\_zfmisc\_1 \\
& \quad (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1))))))\Rightarrow(((v2\_waybel\_8\ X0)\wedge( \\
& \quad v2\_waybel\_8\ X1))\Rightarrow((v5\_pre\_topc\ X2\ X0\ X1)\Leftrightarrow(\forall X3.(m1\_subset\_1 \\
& \quad X3\ (u1\_struct\_0\ X0))\Rightarrow(\forall X4.(m1\_subset\_1\ X4\ (u1\_struct\_0 \\
& \quad X1))\Rightarrow((X4\ \in\ u1\_struct\_0\ (k1\_waybel\_8\ X1))\Rightarrow((r3\_orders\_2\ X1\ X4 \\
& \quad (k3\_funct\_2\ (u1\_struct\_0\ X0)\ (u1\_struct\_0\ X1)\ X2\ X3))\Leftrightarrow(\exists X5. \\
& \quad (m1\_subset\_1\ X5\ (u1\_struct\_0\ X0))\wedge((X5\ \in\ u1\_struct\_0\ (k1\_waybel\_8 \\
& \quad X0))\wedge((r3\_orders\_2\ X0\ X5\ X3)\wedge(r3\_orders\_2\ X1\ X4\ (k3\_funct\_2\ (u1\_struct\_0 \\
& \quad X0)\ (u1\_struct\_0\ X1)\ X2\ X5))))))))))
\end{aligned}$$