

t29_circcomb
(TMYsQscDDcRH4U1sKyvom32qbesq7E9xfnb)

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Let $v2_struct.0 : \iota \Rightarrow o$ be given. Let $v11_struct.0 : \iota \Rightarrow o$ be given. Let $v2_msafree2 : \iota \Rightarrow o$ be given. Let $l1_msualg.1 : \iota \Rightarrow o$ be given. Let $k2_circcomb : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v4_msualg.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v4_msafree2 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $l3_msualg.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k4_card.3 : \iota \Rightarrow \iota$ be given. Let $u3_msualg.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k11_card.3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $u1_struct.0 : \iota \Rightarrow \iota$ be given. Let $u4_struct.0 : \iota \Rightarrow \iota$ be given. Let $k3_circuit1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_relat.1 : \iota \Rightarrow o$ be given. Let $v1_funct.1 : \iota \Rightarrow o$ be given. Let $k3_relat.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k5_relat.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_relat.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_msualg.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_msualg.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $m2_finseq.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_finseq.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v2_relat.1 : \iota \Rightarrow o$ be given. Let $v5_relat.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v4_funct.1 : \iota \Rightarrow o$ be given. Let $l1_struct.0 : \iota \Rightarrow o$ be given. Let $l2_msualg.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v4_relat.1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_finseq.2 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m2_finseq.2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_finseq.1 : \iota \Rightarrow o$ be given. Let $k1_zfmisc.1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc.1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k5_numbers : \iota$ be given. Let $l5_struct.0 : \iota \Rightarrow o$ be given. Let $k3_finseq.2 : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0.((v1_relat.1 X0) \wedge (v1_funct.1 X0)) \Rightarrow (\forall X1.((\\ & v1_relat.1 X1) \wedge (v1_funct.1 X1)) \Rightarrow (\forall X2.k3_relat.1 X1 (k5_relat.1 \\ & X0 X2) = k3_relat.1 (k6_relat.1 X2 X1) X0)) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct.0 X0) \wedge (l1_msualg.1 X0)) \Rightarrow (\forall X1. \\ & ((\neg v2_struct.0 X1) \wedge ((\neg v11_struct.0 X1) \wedge (l1_msualg.1 X1))) \Rightarrow \\ & (\forall X2.(m1_subset.1 X2 (u4_struct.0 X1)) \Rightarrow (\forall X3.(m1_subset.1 \\ & X3 (u4_struct.0 (k2_circcomb X0 X1))) \Rightarrow ((X2 = X3) \Rightarrow ((k1_msualg.1 \\ & (k2_circcomb X0 X1) X3 = k1_msualg.1 X1 X2) \wedge (k2_msualg.1 (k2_circcomb \\ & X0 X1) X3 = k2_msualg.1 X1 X2)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\forall X0.\forall X1.(m2_finseq.1 X1 X0) \Leftrightarrow (m1_finseq.1 X1 X0) \quad (3)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(((v1_relat_1 X0)\wedge((v2_relat_1 X0)\wedge(v1_funct_1 X0)))\wedge(m1_subset_1 X1 (k4_card_3 X0)))\Rightarrow(k11_card_3 X0 X1 X2 = k5_relat_1 X1 X2) \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.((v1_relat_1 X1)\wedge(v5_relat_1 X1 X0))\Rightarrow(k6_relat_1 X0 X1 = X1) \quad (5)$$

Assume the following.

$$\forall X0.((v1_relat_1 X0)\wedge(v1_funct_1 X0))\Rightarrow(v4_funct_1 (k4_card_3 X0)) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.(((l1_struct_0 X0)\wedge((v4_msualg_1 X1 X0)\wedge(l2_msualg_1 X1 X0)))\Rightarrow((v1_relat_1 (u3_msualg_1 X0 X1))\wedge((v2_relat_1 (u3_msualg_1 X0 X1))\wedge((v4_relat_1 (u3_msualg_1 X0 X1) (u1_struct_0 X0))\wedge((v1_funct_1 (u3_msualg_1 X0 X1))\wedge(v1_partfun1 (u3_msualg_1 X0 X1) (u1_struct_0 X0)))))))) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.(((l1_struct_0 X0)\wedge(l2_msualg_1 X1 X0))\Rightarrow((v1_relat_1 (u3_msualg_1 X0 X1))\wedge((v4_relat_1 (u3_msualg_1 X0 X1) (u1_struct_0 X0))\wedge((v1_funct_1 (u3_msualg_1 X0 X1))\wedge(v1_partfun1 (u3_msualg_1 X0 X1) (u1_struct_0 X0)))))) \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.(m1_finseq_2 X1 X0)\Rightarrow(\forall X2.(m2_finseq_2 X2 X0 X1)\Rightarrow(m2_finseq_1 X2 X0)) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.(m2_finseq_1 X1 X0)\Rightarrow((v1_funct_1 X1)\wedge((v1_finseq_1 X1)\wedge(m1_subset_1 X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers X0)))))) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.(m1_finseq_1 X1 X0)\Rightarrow((v1_relat_1 X1)\wedge((v1_funct_1 X1)\wedge(v1_finseq_1 X1))) \quad (11)$$

Assume the following.

$$\forall X0.(l5_struct_0 X0)\Rightarrow(l1_struct_0 X0) \quad (12)$$

Assume the following.

$$\forall X0.((\neg v2_struct_0 X0) \wedge (l1_msualg_1 X0)) \Rightarrow (\forall X1. (l3_msualg_1 X1 X0) \Rightarrow (l2_msualg_1 X1 X0)) \quad (13)$$

Assume the following.

$$\forall X0.(l1_msualg_1 X0) \Rightarrow (l5_struct_0 X0) \quad (14)$$

Assume the following.

$$\forall X0.m1_finseq_2 (k3_finseq_2 X0) X0 \quad (15)$$

Assume the following.

$$\forall X0.\forall X1.(((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge (l1_msualg_1 X0))) \wedge (m1_subset_1 X1 (u4_struct_0 X0))) \Rightarrow (m2_finseq_2 (k1_msualg_1 X0 X1) (u1_struct_0 X0) (k3_finseq_2 (u1_struct_0 X0)))) \quad (16)$$

Assume the following.

$$\forall X0.(((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge ((v2_msafree2 X0) \wedge (l1_msualg_1 X0)))) \Rightarrow (\forall X1.(((v4_msualg_1 X1 X0) \wedge ((v4_msafree2 X1 X0) \wedge (l3_msualg_1 X1 X0))) \Rightarrow (\forall X2.(m1_subset_1 X2 (k4_card_3 (u3_msualg_1 X0 X1))) \Rightarrow (\forall X3.(m1_subset_1 X3 (u4_struct_0 X0)) \Rightarrow (k3_circuit1 X0 X1 X2 X3 = k3_relat_1 (k1_msualg_1 X0 X3) X2)))))) \quad (17)$$

Assume the following.

$$\forall X0.(v4_funct_1 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 X0) \Rightarrow ((v1_relat_1 X1) \wedge (v1_funct_1 X1))) \quad (18)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1))) \Rightarrow ((v4_relat_1 X2 X0) \wedge (v5_relat_1 X2 X1)) \quad (19)$$

Theorem 1

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge ((v2_msafree2 \\ & \quad X0) \wedge (l1_msualg_1 X0)))) \Rightarrow (\forall X1.((\neg v2_struct_0 X1) \wedge ((\neg \\ & \quad v11_struct_0 X1) \wedge ((v2_msafree2 X1) \wedge (l1_msualg_1 X1)))) \Rightarrow (\forall X2. \\ & \quad ((\neg v2_struct_0 X2) \wedge ((\neg v11_struct_0 X2) \wedge ((v2_msafree2 X2) \wedge (\\ & \quad l1_msualg_1 X2)))) \Rightarrow ((X2 = k2_circcomb X0 X1) \Rightarrow (\forall X3.((v4_msualg_1 \\ & \quad X3 X0) \wedge ((v4_msafree2 X3 X0) \wedge (l3_msualg_1 X3 X0))) \Rightarrow (\forall X4. \\ & \quad ((v4_msualg_1 X4 X1) \wedge ((v4_msafree2 X4 X1) \wedge (l3_msualg_1 X4 X1))) \Rightarrow \\ & \quad (\forall X5.((v4_msualg_1 X5 X2) \wedge ((v4_msafree2 X5 X2) \wedge (l3_msualg_1 \\ & \quad X5 X2))) \Rightarrow (\forall X6.(m1_subset_1 X6 (k4_card_3 (u3_msualg_1 \\ & \quad X2 X5))) \Rightarrow (\forall X7.(m1_subset_1 X7 (k4_card_3 (u3_msualg_1 \\ & \quad X1 X4))) \Rightarrow ((X7 = k11_card_3 (u3_msualg_1 X2 X5) X6 (u1_struct_0 X1)) \Rightarrow \\ & \quad (\forall X8.(m1_subset_1 X8 (u4_struct_0 X2)) \Rightarrow (\forall X9.(m1_subset_1 \\ & \quad X9 (u4_struct_0 X1)) \Rightarrow ((X8 = X9) \Rightarrow (k3_circuit1 X2 X5 X6 X8 = k3_circuit1 \\ & \quad X1 X4 X7 X9)))))))))))))) \end{aligned}$$