

t2\_glib\_002 (TM-  
RvXGTG8uQyJLAcujdbBsXHmH3PhEP6ahS)

October 27, 2020

Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $v1\_glib\_000 : \iota \Rightarrow o$  be given. Let  $v4\_glib\_000 : \iota \Rightarrow o$  be given. Let  $v1\_glib\_002 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_glib\_000 : \iota \Rightarrow \iota$  be given. Let  $v10\_glib\_000 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m3\_glib\_001 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_glib\_001 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k13\_glib\_001 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_glib\_001 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_glib\_001 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_glib\_001 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v1\_funct\_1 \\ X0) \wedge ((v1\_finset\_1 X0) \wedge (v1\_glib\_000 X0)))))) \Rightarrow (\forall X1.(m3\_glib\_001 \\ X1 X0) \Rightarrow ((k3\_glib\_001 X0 X1 \in k13\_glib\_001 X0 X1) \wedge (k4\_glib\_001 X0 \\ X1 \in k13\_glib\_001 X0 X1))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v1\_funct\_1 \\ X0) \wedge ((v1\_finset\_1 X0) \wedge ((v1\_glib\_000 X0) \wedge (\neg v4\_glib\_000 X0)))))) \Rightarrow \\ (\neg \forall X1.(m1\_subset\_1 X1 (k6\_glib\_000 X0)) \Rightarrow (\forall X2.( \\ m1\_subset\_1 X2 (k6\_glib\_000 X0)) \Rightarrow (X1 = X2))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v1\_funct\_1 \\ X0) \wedge ((v1\_finset\_1 X0) \wedge (v1\_glib\_000 X0)))))) \Rightarrow (\forall X1.(m3\_glib\_001 \\ X1 X0) \Rightarrow ((\neg v3\_glib\_001 X1 X0) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k6\_glib\_000 \\ X0)) \Rightarrow (\neg (X2 \in k13\_glib\_001 X0 X1) \wedge (v10\_glib\_000 X2 X0)))))) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v1\_funct\_1 \\ X0) \wedge ((v1\_finset\_1 X0) \wedge (v1\_glib\_000 X0)))))) \Rightarrow (\forall X1.(m3\_glib\_001 \\ X1 X0) \Rightarrow (\neg (k3\_glib\_001 X0 X1 \neq k4\_glib\_001 X0 X1) \wedge (v3\_glib\_001 X1 \\ X0))) \end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v1\_funct\_1 \\ & \quad X0) \wedge ((v1\_finset\_1 X0) \wedge (v1\_glib\_000 X0)))))) \Rightarrow (\forall X1. \forall X2. \\ \forall X3. (m3\_glib\_001 X3 X0) \Rightarrow ((r1\_glib\_001 X0 X1 X2 X3) \Leftrightarrow ((k3\_glib\_001 \\ & \quad X0 X3 = X1) \wedge (k4\_glib\_001 X0 X3 = X2)))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v1\_funct\_1 \\ & \quad X0) \wedge ((v1\_finset\_1 X0) \wedge (v1\_glib\_000 X0)))))) \Rightarrow ((v1\_glib\_002 X0) \Leftrightarrow \\ & \quad (\forall X1. (m1\_subset\_1 X1 (k6\_glib\_000 X0)) \Rightarrow (\forall X2. (m1\_subset\_1 \\ & \quad X2 (k6\_glib\_000 X0)) \Rightarrow (\exists X3. (m3\_glib\_001 X3 X0) \wedge (r1\_glib\_001 \\ & \quad X0 X1 X2 X3)))))) \end{aligned} \quad (6)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v1\_funct\_1 \\ & \quad X0) \wedge ((v1\_finset\_1 X0) \wedge ((v1\_glib\_000 X0) \wedge ((\neg v4\_glib\_000 X0) \wedge \\ & \quad (v1\_glib\_002 X0))))))) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (k6\_glib\_000 \\ & \quad X0)) \Rightarrow (\neg v10\_glib\_000 X1 X0)) \end{aligned}$$