

t30_tops_2

(TMYy5TtBBZwCZQ9uFnvsLBjJaHssCDM7Bq3)

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Let $l1_pre_topc : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_tops_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_pre_topc : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k9_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall X0. \forall X1. \forall X2. ((X0 \in X1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 X2))) \Rightarrow (m1_subset_1 X0 X2) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((l1_pre_topc X0) \wedge ((m1_subset_1 X1 (k1_zfmisc_1 (u1_struct_0 X0))) \wedge (m1_subset_1 X2 (k1_zfmisc_1 (k1_zfmisc_1 (u1_struct_0 X0)))))) \Rightarrow (m1_subset_1 (k1_tops_2 X0 X1 X2) (k1_zfmisc_1 (k1_zfmisc_1 (u1_struct_0 (k1_pre_topc X0 X1)))))) \quad (2)$$

Assume the following.

$$\forall X0. (l1_pre_topc X0) \Rightarrow (\forall X1. (m1_subset_1 X1 (k1_zfmisc_1 (u1_struct_0 X0))) \Rightarrow (\forall X2. (m1_subset_1 X2 (k1_zfmisc_1 (k1_zfmisc_1 (u1_struct_0 X0)))) \Rightarrow (\forall X3. (m1_subset_1 X3 (k1_zfmisc_1 (k1_zfmisc_1 (u1_struct_0 (k1_pre_topc X0 X1)))))) \Rightarrow ((X3 = k1_tops_2 X0 X1 X2) \Leftrightarrow (\forall X4. (m1_subset_1 X4 (k1_zfmisc_1 (u1_struct_0 (k1_pre_topc X0 X1)))) \Rightarrow ((X4 \in X3) \Leftrightarrow (\exists X5. (m1_subset_1 X5 (k1_zfmisc_1 (u1_struct_0 X0))) \wedge ((X5 \in X2) \wedge (k9_subset_1 (u1_struct_0 X0) X5 X1 = X4)))))))))) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. (r1_tarski X0 X1) \Leftrightarrow (\forall X2. (X2 \in X0) \Rightarrow (X2 \in X1)) \quad (4)$$

Theorem 1

$$\begin{aligned} \forall X0.(l1_pre_topc\ X0) \Rightarrow & (\forall X1.(m1_subset_1\ X1\ (k1_zfmisc_1 \\ & (u1_struct_0\ X0))) \Rightarrow (\forall X2.(m1_subset_1\ X2\ (k1_zfmisc_1 \\ & (k1_zfmisc_1\ (u1_struct_0\ X0)))) \Rightarrow (\forall X3.(m1_subset_1\ X3 \\ & (k1_zfmisc_1\ (k1_zfmisc_1\ (u1_struct_0\ X0)))) \Rightarrow ((r1_tarski\ X2 \\ & X3) \Rightarrow (r1_tarski\ (k1_tops_2\ X0\ X1\ X2)\ (k1_tops_2\ X0\ X1\ X3)))))) \end{aligned}$$