

## t31\_catalg\_1

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v3\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v5\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v6\_cat\_1 : \iota \Rightarrow o$  be given. Let  $l1\_cat\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $u4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k2\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_catalg\_1 : \iota \Rightarrow \iota$  be given. Let  $k10\_catalg\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k13\_catalg\_1 : \iota \Rightarrow \iota$  be given. Let  $k10\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_finseq\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_graph\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_graph\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $l5\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_graph\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\
 & X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\
 & X0) \wedge (l1\_cat\_1 X0))))))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\
 & X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
 & (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\
 & (u4\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 X5 (u4\_struct\_0 X0)) \Rightarrow \\
 & (((X4 \in k2\_cat\_1 X0 X1 X2) \wedge (X5 \in k2\_cat\_1 X0 X2 X3)) \Rightarrow (k1\_funct\_1 ( \\
 & k5\_msualg\_1 (k3\_catalg\_1 (u1\_struct\_0 X0)) (k10\_catalg\_1 (u1\_struct\_0 \\
 & X0) X1 X2 X3) (k13\_catalg\_1 X0)) (k2\_finseq\_4 (u4\_struct\_0 X0) X5 \\
 & X4) = k1\_cat\_1 X0 X4 X5)))))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
 & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge (l1\_cat\_1 \\
 & X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u4\_struct\_0 X0)) \Rightarrow (\forall X2. \\
 & (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\
 & (u1\_struct\_0 X0)) \Rightarrow (((X1 \in k2\_cat\_1 X0 X2 X3) \Leftrightarrow ((k3\_graph\_1 X0 X1 = \\
 & X2) \wedge (k4\_graph\_1 X0 X1 = X3))))))
 \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\ X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\ X0) \wedge (l1\_cat\_1 X0)))))))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u4\_struct\_0 \\ X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u4\_struct\_0 X0)) \Rightarrow (\forall X3. \\ (m1\_subset\_1 X3 (u4\_struct\_0 X0)) \Rightarrow (((k3\_graph\_1 X0 X3 = k4\_graph\_1 \\ X0 X2) \wedge (k3\_graph\_1 X0 X2 = k4\_graph\_1 X0 X1)) \Rightarrow (k1\_cat\_1 X0 (k1\_cat\_1 \\ X0 X1 X2) X3 = k1\_cat\_1 X0 X1 (k1\_cat\_1 X0 X2 X3)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\ X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\ X0) \wedge (l1\_cat\_1 X0)))))))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u4\_struct\_0 \\ X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u4\_struct\_0 X0)) \Rightarrow ((k3\_graph\_1 \\ X0 X2 = k4\_graph\_1 X0 X1) \Rightarrow ((k3\_graph\_1 X0 (k1\_cat\_1 X0 X1 X2) = k3\_graph\_1 \\ X0 X1) \wedge (k4\_graph\_1 X0 (k1\_cat\_1 X0 X1 X2) = k4\_graph\_1 X0 X2)))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. \forall X2. ((\neg v1\_xboole\_0 X0) \wedge ((m1\_subset\_1 \\ X1 X0) \wedge (m1\_subset\_1 X2 X0))) \Rightarrow (k2\_finseq\_4 X0 X1 X2 = k10\_finseq\_1 \\ X1 X2) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0. ((\neg v11\_struct\_0 X0) \wedge (l5\_struct\_0 X0)) \Rightarrow (\neg v1\_xboole\_0 \\ (u4\_struct\_0 X0)) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0. (l1\_graph\_1 X0) \Rightarrow (l5\_struct\_0 X0) \quad (7)$$

Assume the following.

$$\forall X0. (l1\_cat\_1 X0) \Rightarrow (l1\_graph\_1 X0) \quad (8)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. \forall X2. ((l1\_cat\_1 X0) \wedge ((m1\_subset\_1 \\ X1 (u4\_struct\_0 X0)) \wedge (m1\_subset\_1 X2 (u4\_struct\_0 X0)))) \Rightarrow (m1\_subset\_1 \\ (k1\_cat\_1 X0 X1 X2) (u4\_struct\_0 X0)) \end{aligned} \quad (9)$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\
& X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\
& X0) \wedge (l1\_cat\_1 X0))))))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
& (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 X5 (u4\_struct\_0 X0)) \Rightarrow \\
& (\forall X6.(m1\_subset\_1 X6 (u4\_struct\_0 X0)) \Rightarrow (\forall X7.(m1\_subset\_1 \\
& X7 (u4\_struct\_0 X0)) \Rightarrow (((X5 \in k2\_cat\_1 X0 X1 X2) \wedge ((X6 \in k2\_cat\_1 X0 \\
& X2 X3) \wedge (X7 \in k2\_cat\_1 X0 X3 X4))) \Rightarrow (k1\_funct\_1 (k5\_msualg\_1 (k3\_catalg\_1 \\
& (u1\_struct\_0 X0)) (k10\_catalg\_1 (u1\_struct\_0 X0) X1 X3 X4) (k13\_catalg\_1 \\
& X0)) (k10\_finseq\_1 X7 (k1\_funct\_1 (k5\_msualg\_1 (k3\_catalg\_1 ( \\
& u1\_struct\_0 X0)) (k10\_catalg\_1 (u1\_struct\_0 X0) X1 X2 X3) (k13\_catalg\_1 \\
& X0)) (k2\_finseq\_4 (u4\_struct\_0 X0) X6 X5))) = k1\_funct\_1 (k5\_msualg\_1 \\
& (k3\_catalg\_1 (u1\_struct\_0 X0)) (k10\_catalg\_1 (u1\_struct\_0 X0) \\
& X1 X2 X4) (k13\_catalg\_1 X0)) (k10\_finseq\_1 (k1\_funct\_1 (k5\_msualg\_1 \\
& (k3\_catalg\_1 (u1\_struct\_0 X0)) (k10\_catalg\_1 (u1\_struct\_0 X0) \\
& X2 X3 X4) (k13\_catalg\_1 X0)) (k2\_finseq\_4 (u4\_struct\_0 X0) X7 X6)) \\
& X5))))))))))
\end{aligned}$$