

## t31\_hilbert3

(TMN458d3EkmizQjCFVyLKPtzecULW76scT7)

October 27, 2020

Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_hilbert1 : \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v2\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_hilbert3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_hilbert1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_hilbert3 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_hilbert1 : \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k1\_hilbert2 : \iota \Rightarrow \iota$  be given. Let  $k3\_hilbert1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. ((m1\_subset\_1 X0 k1\_hilbert1) \wedge (m1\_subset\_1 X1 k1\_hilbert1)) \Rightarrow (m1\_subset\_1 (k4\_hilbert1 X0 X1) k1\_hilbert1) \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0. ((v1\_relat\_1 X0) \wedge ((v2\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 \\ k5\_numbers) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 X0 k5\_numbers)))))) \Rightarrow \\ ((v1\_relat\_1 (k2\_hilbert3 X0)) \wedge ((v4\_relat\_1 (k2\_hilbert3 X0) \\ k1\_hilbert1) \wedge ((v1\_funct\_1 (k2\_hilbert3 X0)) \wedge (v1\_partfun1 ( \\ k2\_hilbert3 X0) k1\_hilbert1)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0. ((v1\_relat\_1 X0) \wedge ((v2\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 \\ k5\_numbers) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 X0 k5\_numbers)))))) \Rightarrow \\ (\forall X1. (m1\_subset\_1 X1 k1\_hilbert1) \Rightarrow (k3\_hilbert3 X0 X1 = \\ k1\_funct\_1 (k2\_hilbert3 X0) X1)) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v2\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 \\
& k5\_numbers) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 X0 k5\_numbers)))))) \Rightarrow \\
& (\forall X1.((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 k1\_hilbert1) \wedge ( \\
& (v1\_funct\_1 X1) \wedge (v1\_partfun1 X1 k1\_hilbert1)))))) \Rightarrow ((X1 = k2\_hilbert3 \\
& X0) \Leftrightarrow ((k1\_funct\_1 X1 k2\_hilbert1 = np\_1) \wedge ((\forall X2.(m2\_subset\_1 \\
& X2 k1\_numbers k5\_numbers) \Rightarrow (k1\_funct\_1 X1 (k1\_hilbert2 X2) = k1\_funct\_1 \\
& X0 X2)) \wedge (\forall X2.(m1\_subset\_1 X2 k1\_hilbert1) \Rightarrow (\forall X3. \\
& (m1\_subset\_1 X3 k1\_hilbert1) \Rightarrow ((k1\_funct\_1 X1 (k4\_hilbert1 X2 \\
& X3) = k2\_zfmisc\_1 (k1\_funct\_1 X1 X2) (k1\_funct\_1 X1 X3)) \wedge (k1\_funct\_1 \\
& X1 (k3\_hilbert1 X2 X3) = k1\_funct\_2 (k1\_funct\_1 X1 X2) (k1\_funct\_1 \\
& X1 X3))))))))))
\end{aligned} \tag{4}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& X1 k1\_hilbert1) \Rightarrow (\forall X2.((v1\_relat\_1 X2) \wedge ((v2\_relat\_1 X2) \wedge \\
& ((v4\_relat\_1 X2 k5\_numbers) \wedge ((v1\_funct\_1 X2) \wedge (v1\_partfun1 X2 \\
& k5\_numbers)))))) \Rightarrow (k3\_hilbert3 X2 (k4\_hilbert1 X0 X1) = k2\_zfmisc\_1 \\
& (k3\_hilbert3 X2 X0) (k3\_hilbert3 X2 X1))))
\end{aligned}$$