

t31_semi_af1 (TMcTp-
WUg2e44DxWKCHaJNC2J85uUDG8b37)

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Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $v1_semi_af1 : \iota \Rightarrow o$ be given. Let $l1_analoaf : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $r1_semi_af1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r2_analoaf : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0) \wedge ((v1_semi_af1 X0) \wedge (l1_analoaf X0))) \Rightarrow (\forall X1.(m1_subset_1 X1 (u1_struct_0 X0)) \Rightarrow (\forall X2. \\ & (m1_subset_1 X2 (u1_struct_0 X0)) \Rightarrow (\forall X3.(m1_subset_1 X3 (u1_struct_0 X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 (u1_struct_0 X0)) \Rightarrow \\ & ((r2_analoaf X0 X1 X2 X3 X4) \Rightarrow ((r2_analoaf X0 X2 X1 X3 X4) \wedge ((r2_analoaf X0 X1 X2 X4 X3) \wedge ((r2_analoaf X0 X2 X1 X3 X4 X1 X2) \wedge ((r2_analoaf X0 X4 X3 X1 X2) \wedge ((r2_analoaf X0 X3 X4 X2 X1) \wedge (r2_analoaf X0 X4 X3 X2 X1)))))))))) \\ & \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0) \wedge ((v1_semi_af1 X0) \wedge (l1_analoaf X0))) \Rightarrow (\forall X1.(m1_subset_1 X1 (u1_struct_0 X0)) \Rightarrow (\forall X2. \\ & (m1_subset_1 X2 (u1_struct_0 X0)) \Rightarrow (\forall X3.(m1_subset_1 X3 (u1_struct_0 X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 (u1_struct_0 X0)) \Rightarrow \\ & (((r1_semi_af1 X0 X1 X2 X3) \wedge (r1_semi_af1 X0 X1 X2 X4)) \Rightarrow (r2_analoaf X0 X1 X2 X3 X4)))))) \\ & \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned}
& \forall X_0. ((\neg v_{2_struct_0} X_0) \wedge (l_{1_analoaf} X_0)) \Rightarrow ((v_{1_semi_af} \\
& X_0) \Leftrightarrow ((\forall X_1. (m_{1_subset_1} X_1 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_2. \\
& (m_{1_subset_1} X_2 (u_{1_struct_0} X_0)) \Rightarrow (r_{2_analoaf} X_0 X_1 X_2 X_2 X_1))) \wedge \\
& ((\forall X_1. (m_{1_subset_1} X_1 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_2. (\\
& m_{1_subset_1} X_2 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_3. (m_{1_subset_1} X_3 \\
& (u_{1_struct_0} X_0)) \Rightarrow (r_{2_analoaf} X_0 X_1 X_2 X_3 X_3)))) \wedge ((\forall X_1. \\
& (m_{1_subset_1} X_1 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_2. (m_{1_subset_1} X_2 \\
& (u_{1_struct_0} X_0)) \Rightarrow (\forall X_3. (m_{1_subset_1} X_3 (u_{1_struct_0} X_0)) \Rightarrow \\
& (\forall X_4. (m_{1_subset_1} X_4 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_5. (m_{1_subset_1} \\
& X_5 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_6. (m_{1_subset_1} X_6 (u_{1_struct_0} \\
& X_0)) \Rightarrow (((r_{2_analoaf} X_0 X_1 X_2 X_3 X_4) \wedge (r_{2_analoaf} X_0 X_1 X_2 X_5 X_6)) \Rightarrow \\
& (X_1 = X_2) \vee (r_{2_analoaf} X_0 X_3 X_4 X_5 X_6))))))) \wedge ((\forall X_1. (m_{1_subset_1} \\
& X_1 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_2. (m_{1_subset_1} X_2 (u_{1_struct_0} \\
& X_0)) \Rightarrow (\forall X_3. (m_{1_subset_1} X_3 (u_{1_struct_0} X_0)) \Rightarrow ((r_{2_analoaf} \\
& X_0 X_1 X_2 X_1 X_3) \Rightarrow (r_{2_analoaf} X_0 X_2 X_1 X_2 X_3)))))) \wedge ((\neg \forall X_1. (m_{1_subset_1} \\
& X_1 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_2. (m_{1_subset_1} X_2 (u_{1_struct_0} \\
& X_0)) \Rightarrow (\forall X_3. (m_{1_subset_1} X_3 (u_{1_struct_0} X_0)) \Rightarrow (r_{2_analoaf} \\
& X_0 X_1 X_2 X_1 X_3)) \wedge ((\forall X_1. (m_{1_subset_1} X_1 (u_{1_struct_0} X_0)) \Rightarrow \\
& (\forall X_2. (m_{1_subset_1} X_2 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_3. (m_{1_subset_1} \\
& X_3 (u_{1_struct_0} X_0)) \Rightarrow (\exists X_4. (m_{1_subset_1} X_4 (u_{1_struct_0} \\
& X_0)) \wedge ((r_{2_analoaf} X_0 X_1 X_2 X_3 X_4) \wedge (r_{2_analoaf} X_0 X_1 X_3 X_2 X_4)))))) \wedge \\
& ((\forall X_1. (m_{1_subset_1} X_1 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_2. (\\
& m_{1_subset_1} X_2 (u_{1_struct_0} X_0)) \Rightarrow (\exists X_3. (m_{1_subset_1} X_3 \\
& (u_{1_struct_0} X_0)) \wedge (\forall X_4. (m_{1_subset_1} X_4 (u_{1_struct_0} X_0)) \Rightarrow \\
& (\forall X_5. (m_{1_subset_1} X_5 (u_{1_struct_0} X_0)) \Rightarrow ((r_{2_analoaf} X_0 \\
& X_1 X_2 X_1 X_3) \wedge (\neg \forall X_6. (m_{1_subset_1} X_6 (u_{1_struct_0} X_0)) \Rightarrow ((\\
& r_{2_analoaf} X_0 X_1 X_3 X_1 X_4) \wedge (\neg (r_{2_analoaf} X_0 X_1 X_5 X_1 X_6) \wedge (r_{2_analoaf} \\
& X_0 X_3 X_5 X_4 X_6)))))))) \wedge ((\forall X_1. (m_{1_subset_1} X_1 (u_{1_struct_0} \\
& X_0)) \Rightarrow (\forall X_2. (m_{1_subset_1} X_2 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_3. \\
& (m_{1_subset_1} X_3 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_4. (m_{1_subset_1} X_4 \\
& (u_{1_struct_0} X_0)) \Rightarrow (\forall X_5. (m_{1_subset_1} X_5 (u_{1_struct_0} X_0)) \Rightarrow \\
& (\forall X_6. (m_{1_subset_1} X_6 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_7. (m_{1_subset_1} \\
& X_7 (u_{1_struct_0} X_0)) \Rightarrow (((r_{2_analoaf} X_0 X_1 X_2 X_1 X_3) \wedge ((r_{2_analoaf} \\
& X_0 X_1 X_4 X_1 X_5) \wedge ((r_{2_analoaf} X_0 X_1 X_6 X_1 X_7) \wedge ((r_{2_analoaf} X_0 X_2 X_4 X_3 \\
& X_5) \wedge (r_{2_analoaf} X_0 X_2 X_6 X_3 X_7)))))) \Rightarrow ((r_{2_analoaf} X_0 X_1 X_2 X_1 X_4) \vee \\
& ((r_{2_analoaf} X_0 X_1 X_2 X_1 X_6) \vee (r_{2_analoaf} X_0 X_4 X_6 X_5 X_7))))))) \wedge \\
& ((\forall X_1. (m_{1_subset_1} X_1 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_2. (\\
& m_{1_subset_1} X_2 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_3. (m_{1_subset_1} X_3 \\
& (u_{1_struct_0} X_0)) \Rightarrow (\forall X_4. (m_{1_subset_1} X_4 (u_{1_struct_0} X_0)) \Rightarrow \\
& (\forall X_5. (m_{1_subset_1} X_5 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_6. (m_{1_subset_1} \\
& X_6 (u_{1_struct_0} X_0)) \Rightarrow (((r_{2_analoaf} X_0 X_1 X_2 X_3 X_4) \wedge ((r_{2_analoaf} \\
& X_0 X_1 X_2 X_5 X_6) \wedge ((r_{2_analoaf} X_0 X_1 X_3 X_2 X_4) \wedge (r_{2_analoaf} X_0 X_1 X_5 X_2 \\
& X_6)))))) \Rightarrow ((r_{2_analoaf} X_0 X_1 X_2 X_1 X_3) \vee ((r_{2_analoaf} X_0 X_1 X_2 X_1 X_5) \vee \\
& (r_{2_analoaf} X_0 X_3 X_5 X_4 X_6))))))) \wedge ((\forall X_1. (m_{1_subset_1} \\
& X_1 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_2. (m_{1_subset_1} X_2 (u_{1_struct_0} \\
& X_0)) \Rightarrow (\forall X_3. (m_{1_subset_1} X_3 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_4. \\
& (m_{1_subset_1} X_4 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_5. (m_{1_subset_1} X_5 \\
& (u_{1_struct_0} X_0)) \Rightarrow (\forall X_6. (m_{1_subset_1} X_6 (u_{1_struct_0} X_0)) \Rightarrow \\
& (((r_{2_analoaf} X_0 X_1 X_2 X_1 X_3) \wedge ((r_{2_analoaf} X_0 X_4 X_5 X_4 X_6) \wedge ((r_{2_analoaf} \\
& X_0 X_1 X_5 X_2 X_4) \wedge (r_{2_analoaf} X_0 X_2 X_6 X_3 X_5)))))) \Rightarrow ((r_{2_analoaf} X_0 X_3 X_4 \\
& X_1 X_6))))))) \wedge ((\forall X_1. (m_{1_subset_1} X_1 (u_{1_struct_0} X_0)) \Rightarrow \\
& (\forall X_2. (m_{1_subset_1} X_2 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_3. (m_{1_subset_1} \\
& X_3 (u_{1_struct_0} X_0)) \Rightarrow (\forall X_4. (m_{1_subset_1} X_4 (u_{1_struct_0} \\
& X_0)) \Rightarrow (\neg (\neg (r_{2_analoaf} X_0 X_1 X_2 X_1 X_3) \wedge ((r_{2_analoaf} X_0 X_1 X_2 X_3 X_4) \wedge \\
& ((r_{2_analoaf} X_0 X_1 X_3 X_2 X_4) \wedge (r_{2_analoaf} X_0 X_1 X_4 X_2 X_3))))))))))) \\
& (3)
\end{aligned}$$

Theorem 1

$$\begin{aligned} \forall X0.((\neg v2_struct_0 X0) \wedge ((v1_semi_af1 X0) \wedge (l1_analoaf X0))) \Rightarrow (\forall X1.(m1_subset_1 X1 (u1_struct_0 X0)) \Rightarrow (\forall X2. \\ (m1_subset_1 X2 (u1_struct_0 X0)) \Rightarrow (\forall X3.(m1_subset_1 X3 (u1_struct_0 X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 (u1_struct_0 X0)) \Rightarrow \\ (\forall X5.(m1_subset_1 X5 (u1_struct_0 X0)) \Rightarrow (\forall X6.(m1_subset_1 X6 (u1_struct_0 X0)) \Rightarrow (((r1_semi_af1 X0 X1 X2 X5) \wedge ((r1_semi_af1 \\ X0 X1 X2 X6) \wedge ((r1_semi_af1 X0 X3 X4 X5) \wedge (r1_semi_af1 X0 X3 X4 X6)))) \Rightarrow \\ ((r2_analoaf X0 X1 X2 X3 X4) \vee (X5 = X6)))))))) \end{aligned}$$