

# t31\_tops\_2 (TMTqQFXqfUn- Ngw8Y7TaN4G8rm9yoQoqjGu8)

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Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k9\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tops\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_pre\_topc : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. \forall X2. ((X0 \in X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X2))) \Rightarrow (m1\_subset\_1 X0 X2) \quad (1)$$

Assume the following.

$$\forall X0. (l1\_pre\_topc X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (m1\_subset\_1 (k9\_subset\_1 (u1\_struct\_0 X0) X1 X2) (k1\_zfmisc\_1 (u1\_struct\_0 (k1\_pre\_topc X0 X2)))))) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((l1\_pre\_topc X0) \wedge ((m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))))) \Rightarrow (m1\_subset\_1 (k1\_tops\_2 X0 X1 X2) (k1\_zfmisc\_1 (k1\_zfmisc\_1 (u1\_struct\_0 (k1\_pre\_topc X0 X1)))))) \quad (3)$$

Assume the following.

$$\forall X0. (l1\_pre\_topc X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow (\forall X3. (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k1\_zfmisc\_1 (u1\_struct\_0 (k1\_pre\_topc X0 X1)))))) \Rightarrow ((X3 = k1\_tops\_2 X0 X1 X2) \Leftrightarrow (\forall X4. (m1\_subset\_1 X4 (k1\_zfmisc\_1 (u1\_struct\_0 (k1\_pre\_topc X0 X1)))) \Rightarrow ((X4 \in X3) \Leftrightarrow (\exists X5. (m1\_subset\_1 X5 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \wedge ((X5 \in X2) \wedge (k9\_subset\_1 (u1\_struct\_0 X0) X5 X1 = X4)))))))))) \quad (4)$$

**Theorem 1**

$$\begin{aligned} \forall X0.(l1\_pre\_topc\ X0) \Rightarrow (\forall X1.(m1\_subset\_1\ X1\ (k1\_zfmisc\_1 \\ (u1\_struct\_0\ X0))) \Rightarrow (\forall X2.(m1\_subset\_1\ X2\ (k1\_zfmisc\_1 \\ (u1\_struct\_0\ X0))) \Rightarrow (\forall X3.(m1\_subset\_1\ X3\ (k1\_zfmisc\_1 \\ (k1\_zfmisc\_1\ (u1\_struct\_0\ X0)))) \Rightarrow ((X1 \in X3) \Rightarrow (k9\_subset\_1\ (u1\_struct\_0 \\ X0)\ X1\ X2 \in k1\_tops\_2\ X0\ X2\ X3)))))) \end{aligned}$$