

t31\_tsp\_2  
(TMFRv7StskgFMVo8FbPgvS3P1N3FxdjsSCY)

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Let  $v2\_struct.0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_topc : \iota \Rightarrow o$  be given. Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $v2\_tsp.2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_pre\_topc : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset.1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc.1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct.0 : \iota \Rightarrow \iota$  be given. Let  $k7\_relset.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tsp.2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_subset.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_tex.4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_xboole.0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_xboole.0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_subset.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc.1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_funct.1 : \iota \Rightarrow o$  be given. Let  $v1\_funct.2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v5\_pre\_topc : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct.0 X0) \wedge (l1\_pre\_topc X0)) \Rightarrow (\forall X1. \\ & (m1\_subset.1 X1 (k1\_zfmisc.1 (u1\_struct.0 X0))) \Rightarrow (\forall X2. \\ & (m1\_subset.1 X2 (k1\_zfmisc.1 (u1\_struct.0 X0))) \Rightarrow (k3\_tex.4 X0 \\ & (k4\_subset.1 (u1\_struct.0 X0) X1 X2) = k4\_subset.1 (u1\_struct.0 \\ & X0) (k3\_tex.4 X0 X1) (k3\_tex.4 X0 X2)))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. k3\_xboole.0 X0 (k2\_xboole.0 \\ & X1 X2) = k2\_xboole.0 (k3\_xboole.0 X0 X1) (k3\_xboole.0 X0 X2) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. (l1\_pre\_topc X0) \Rightarrow (\forall X1. (m1\_pre\_topc X1 X0) \Rightarrow \\ & (m1\_subset.1 (u1\_struct.0 X1) (k1\_zfmisc.1 (u1\_struct.0 X0)))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (m1\_subset.1 X2 (k1\_zfmisc.1 \\ & X0)) \Rightarrow (k9\_subset.1 X0 X1 X2 = k3\_xboole.0 X1 X2) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((m1\_subset.1 X1 (k1\_zfmisc.1 \\ & X0)) \wedge (m1\_subset.1 X2 (k1\_zfmisc.1 X0))) \Rightarrow (k4\_subset.1 X0 X1 X2 = \\ & k2\_xboole.0 X1 X2) \end{aligned} \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.\forall X3.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))\Rightarrow(m1\_subset\_1 (k7\_relset\_1 X0 X1 X2 X3) (k1\_zfmisc\_1 X1)) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 X0)))\Rightarrow(m1\_subset\_1 (k4\_subset\_1 X0 X1 X2) (k1\_zfmisc\_1 X0)) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.(((\neg v2\_struct\_0 X0)\wedge(l1\_pre\_topc X0))\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))))\Rightarrow(m1\_subset\_1 (k3\_tex\_4 X0 X1) (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.(((\neg v2\_struct\_0 X0)\wedge((v2\_pre\_topc X0)\wedge(l1\_pre\_topc X0)))\wedge((\neg v2\_struct\_0 X1)\wedge((v2\_tsp\_2 X1 X0)\wedge(m1\_pre\_topc X1 X0))))\Rightarrow((v1\_funct\_1 (k1\_tsp\_2 X0 X1))\wedge((v1\_funct\_2 (k1\_tsp\_2 X0 X1) (u1\_struct\_0 X0) (u1\_struct\_0 X1))\wedge((v5\_pre\_topc (k1\_tsp\_2 X0 X1) X0 X1)\wedge(m1\_subset\_1 (k1\_tsp\_2 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1)))))))) \quad (9)$$

Assume the following.

$$\forall X0.((\neg v2\_struct\_0 X0)\wedge((v2\_pre\_topc X0)\wedge(l1\_pre\_topc X0)))\Rightarrow(\forall X1.((\neg v2\_struct\_0 X1)\wedge((v2\_tsp\_2 X1 X0)\wedge(m1\_pre\_topc X1 X0))))\Rightarrow(\forall X2.((v1\_funct\_1 X2)\wedge((v1\_funct\_2 X2 (u1\_struct\_0 X0) (u1\_struct\_0 X1))\wedge((v5\_pre\_topc X2 X0 X1)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1))))))))\Rightarrow((X2 = k1\_tsp\_2 X0 X1)\Leftrightarrow(\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))\Rightarrow((X3 = u1\_struct\_0 X1)\Rightarrow(\forall X4.(m1\_subset\_1 X4 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))\Rightarrow(k9\_subset\_1 (u1\_struct\_0 X0) X3 (k3\_tex\_4 X0 X4) = k7\_relset\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1) X2 X4)))))) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 X0))\Rightarrow(k9\_subset\_1 X0 X1 X2 = k9\_subset\_1 X0 X2 X1) \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.k3\_xboole\_0 X0 X1 = k3\_xboole\_0 X1 X0 \quad (12)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc \\ & X0))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((v2\_tsp\_2 X1 X0) \wedge (m1\_pre\_topc \\ & X1 X0))) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0))) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0))) \Rightarrow (k7\_relset\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1) (k1\_tsp\_2 \\ & X0 X1) (k4\_subset\_1 (u1\_struct\_0 X0) X2 X3) = k4\_subset\_1 (u1\_struct\_0 \\ & X1) (k7\_relset\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1) (k1\_tsp\_2 X0 \\ & X1) X2) (k7\_relset\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1) (k1\_tsp\_2 \\ & X0 X1) X3)))))) \end{aligned}$$