

# t31\_waybel20 (TMaEnm- CyYJqw73vBsPk4QFQL4BryAPYtwcD)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_yellow\_1 : \iota \Rightarrow o$  be given. Let  $v4\_waybel\_3 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v5\_orders\_2 : \iota \Rightarrow o$  be given. Let  $k3\_waybel\_3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_yellow\_0 : \iota \Rightarrow o$  be given. Let  $l1\_orders\_2 : \iota \Rightarrow o$  be given. Let  $k4\_waybel\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_yellow\_0 : \iota \Rightarrow \iota$  be given. Let  $k5\_yellow\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $r1\_orders\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_orders\_2 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v5\_orders\_2 X0) \wedge ((v1\_yellow\_0 \\ X0) \wedge (l1\_orders\_2 X0)))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\ X0)) \Rightarrow (r1\_orders\_2 X0 (k3\_yellow\_0 X0) X1)) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge ( \\ (v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge ((v1\_yellow\_1 \\ X1) \wedge (v4\_waybel\_3 X1)))))) \Rightarrow ((\forall X2.(m1\_subset\_1 X2 X0) \Rightarrow \\ (v5\_orders\_2 (k3\_waybel\_3 X0 X1 X2))) \Rightarrow (v5\_orders\_2 (k5\_yellow\_1 \\ X0 X1)))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge ( \\ (v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge ((v1\_yellow\_1 \\ X1) \wedge (v4\_waybel\_3 X1)))))) \Rightarrow ((\forall X2.(m1\_subset\_1 X2 X0) \Rightarrow \\ ((v5\_orders\_2 (k3\_waybel\_3 X0 X1 X2)) \wedge ((v1\_yellow\_0 (k3\_waybel\_3 \\ X0 X1 X2)) \wedge (l1\_orders\_2 (k3\_waybel\_3 X0 X1 X2)))))) \Rightarrow (v1\_yellow\_0 \\ (k5\_yellow\_1 X0 X1)))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge \\ & (v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge ((v1\_yellow\_1 \\ & X1) \wedge (v4\_waybel\_3 X1)))))) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\ & (k5\_yellow\_1 X0 X1))) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\ & (k5\_yellow\_1 X0 X1))) \Rightarrow ((r1\_orders\_2 (k5\_yellow\_1 X0 X1) X2 X3) \Leftrightarrow \\ & (\forall X4.(m1\_subset\_1 X4 X0) \Rightarrow (r1\_orders\_2 (k3\_waybel\_3 X0 \\ & X1 X4) (k4\_waybel\_3 X0 X1 X2 X4) (k4\_waybel\_3 X0 X1 X3 X4)))))) \\ & \hspace{15em} (4) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge \\ & (v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge ((v1\_yellow\_1 \\ & X1) \wedge (v4\_waybel\_3 X1)))))) \Rightarrow (\forall X2.((v1\_relat\_1 X2) \wedge (v1\_funct\_1 \\ & X2)) \Rightarrow ((m1\_subset\_1 X2 (u1\_struct\_0 (k5\_yellow\_1 X0 X1))) \Leftrightarrow ((k9\_xtuple\_0 \\ & X2 = X0) \wedge (\forall X3.(m1\_subset\_1 X3 X0) \Rightarrow (m1\_subset\_1 (k1\_funct\_1 \\ & X2 X3) (u1\_struct\_0 (k3\_waybel\_3 X0 X1 X3)))))) \\ & \hspace{15em} (5) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v5\_orders\_2 X0) \wedge ((v1\_yellow\_0 \\ & X0) \wedge (l1\_orders\_2 X0)))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0)) \Rightarrow ((r1\_orders\_2 X0 X1 (k3\_yellow\_0 X0)) \Rightarrow (X1 = k3\_yellow\_0 X0))) \\ & \hspace{15em} (6) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0 : \iota \Rightarrow \iota. \forall X1. \exists X2. ((v1\_relat\_1 X2) \wedge \\ & (v4\_relat\_1 X2 X1) \wedge ((v1\_funct\_1 X2) \wedge (v1\_partfun1 X2 X1))) \wedge \\ & \forall X3.(m1\_subset\_1 X3 X1) \Rightarrow (k1\_funct\_1 X2 X3 = X0 X3) \\ & \hspace{15em} (7) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1\_xboole\_0 X0) \wedge \\ & (((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_partfun1 \\ & X1 X0) \wedge ((v1\_yellow\_1 X1) \wedge (v4\_waybel\_3 X1)))))) \wedge ((m1\_subset\_1 \\ & X2 (u1\_struct\_0 (k5\_yellow\_1 X0 X1))) \wedge (m1\_subset\_1 X3 X0))) \Rightarrow \\ & (k4\_waybel\_3 X0 X1 X2 X3 = k1\_funct\_1 X2 X3) \\ & \hspace{15em} (8) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((\neg v1\_xboole\_0 X0) \wedge ((v1\_relat\_1 \\ & X1) \wedge ((v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge \\ & (v1\_yellow\_1 X1)))))) \wedge (m1\_subset\_1 X2 X0)) \Rightarrow (k3\_waybel\_3 X0 X1 \\ & X2 = k1\_funct\_1 X1 X2) \\ & \hspace{15em} (9) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge (v4\_relat\_1 X1 X0)) \Rightarrow ( \\ & k1\_relset\_1 X0 X1 = k9\_xtuple\_0 X1) \\ & \hspace{15em} (10) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((\neg v1\_xboole\_0 X0) \wedge (((v1\_relat\_1 \\ & X1) \wedge ((v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge \\ & ((v1\_yellow\_1 X1) \wedge (v4\_waybel\_3 X1)))))) \wedge (m1\_subset\_1 X2 X0))) \Rightarrow \\ & (\neg v2\_struct\_0 (k1\_funct\_1 X1 X2)) \end{aligned} \quad (11)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge \\ & (v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge ((v1\_yellow\_1 X1) \wedge (v4\_waybel\_3 \\ & X1)))))) \Rightarrow ((\neg v2\_struct\_0 (k5\_yellow\_1 X0 X1)) \wedge (v1\_orders\_2 ( \\ & k5\_yellow\_1 X0 X1))) \end{aligned} \quad (12)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge \\ & (v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge (v1\_yellow\_1 X1)))) \Rightarrow ( \\ & (v1\_orders\_2 (k5\_yellow\_1 X0 X1)) \wedge (l1\_orders\_2 (k5\_yellow\_1 \\ & X0 X1))) \end{aligned} \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1\_xboole\_0 X0) \wedge \\ & (((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_partfun1 \\ & X1 X0) \wedge ((v1\_yellow\_1 X1) \wedge (v4\_waybel\_3 X1)))))) \wedge ((m1\_subset\_1 \\ & X2 (u1\_struct\_0 (k5\_yellow\_1 X0 X1)) \wedge (m1\_subset\_1 X3 X0)))) \Rightarrow \\ & (m1\_subset\_1 (k4\_waybel\_3 X0 X1 X2 X3) (u1\_struct\_0 (k3\_waybel\_3 \\ & X0 X1 X3))) \end{aligned} \quad (14)$$

Assume the following.

$$\forall X0. (l1\_orders\_2 X0) \Rightarrow (m1\_subset\_1 (k3\_yellow\_0 X0) (u1\_struct\_0 X0)) \quad (15)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge (v4\_relat\_1 X1 X0)) \Rightarrow ( \\ & (v1\_partfun1 X1 X0) \Leftrightarrow (k1\_relset\_1 X0 X1 = X0)) \end{aligned} \quad (16)$$

**Theorem 1**

$$\begin{aligned} & \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. ((v1\_relat\_1 X1) \wedge \\ & (v4\_relat\_1 X1 X0) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge ((v1\_yellow\_1 \\ & X1) \wedge (v4\_waybel\_3 X1)))))) \Rightarrow ((\forall X2. (m1\_subset\_1 X2 X0) \Rightarrow \\ & ((v5\_orders\_2 (k3\_waybel\_3 X0 X1 X2)) \wedge ((v1\_yellow\_0 (k3\_waybel\_3 \\ & X0 X1 X2)) \wedge (l1\_orders\_2 (k3\_waybel\_3 X0 X1 X2)))))) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 X0) \Rightarrow (k4\_waybel\_3 X0 X1 (k3\_yellow\_0 (k5\_yellow\_1 \\ & X0 X1)) X2 = k3\_yellow\_0 (k3\_waybel\_3 X0 X1 X2)))) \end{aligned}$$