

## t32\_morph\_01

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Let  $v2\_struct.0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr.0 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect.1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect.1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect.1 : \iota \Rightarrow o$  be given. Let  $v5\_rlvect.1 : \iota \Rightarrow o$  be given. Let  $v6\_rlvect.1 : \iota \Rightarrow o$  be given. Let  $v7\_rlvect.1 : \iota \Rightarrow o$  be given. Let  $v8\_rlvect.1 : \iota \Rightarrow o$  be given. Let  $l1\_rlvect.1 : \iota \Rightarrow o$  be given. Let  $v1\_xboole.0 : \iota \Rightarrow o$  be given. Let  $m1\_subset.1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc.1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct.0 : \iota \Rightarrow \iota$  be given. Let  $k3\_funct.2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_setfam.1 : \iota \Rightarrow \iota$  be given. Let  $k3\_morph.01 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_subset.1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_morph.01 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_rusub.4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_morph.01 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_xboole.0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l2\_algstr.0 : \iota \Rightarrow o$  be given. Let  $k2\_morph.01 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_funct.1 : \iota \Rightarrow o$  be given. Let  $v1\_funct.2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc.1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct.0 X0) \wedge ((v13\_algstr.0 X0) \wedge ((v2\_rlvect.1 \\ & X0) \wedge ((v3\_rlvect.1 X0) \wedge ((v4\_rlvect.1 X0) \wedge ((v5\_rlvect.1 X0) \wedge \\ & ((v6\_rlvect.1 X0) \wedge ((v7\_rlvect.1 X0) \wedge ((v8\_rlvect.1 X0) \wedge (l1\_rlvect.1 \\ & X0)))))))))) \Rightarrow (\forall X1.((\neg v1\_xboole.0 X1) \wedge (m1\_subset.1 X1 \\ & (k1\_zfmisc.1 (u1\_struct.0 X0)))) \Rightarrow (\forall X2.((\neg v1\_xboole.0 \\ & X2) \wedge (m1\_subset.1 X2 (k1\_zfmisc.1 (u1\_struct.0 X0)))) \Rightarrow ((k6\_rusub.4 \\ & X0 (k6\_subset.1 (u1\_struct.0 X0) X1) X2 = k6\_subset.1 (u1\_struct.0 \\ & X0) (k1\_morph.01 X0 X1 X2)) \wedge (k1\_morph.01 X0 (k6\_subset.1 (u1\_struct.0 \\ & X0) X1) X2 = k6\_subset.1 (u1\_struct.0 X0) (k6\_rusub.4 X0 X1 X2)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. \forall X1. k6\_subset.1 X0 X1 = k4\_xboole.0 X0 X1 \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2\_struct.0 X0) \wedge ((v2\_rlvect.1 \\ & X0) \wedge (l2\_algstr.0 X0))) \wedge ((m1\_subset.1 X1 (k1\_zfmisc.1 (u1\_struct.0 \\ & X0))) \wedge (m1\_subset.1 X2 (k1\_zfmisc.1 (u1\_struct.0 X0)))))) \Rightarrow (k2\_morph.01 \\ & X0 X1 X2 = k6\_rusub.4 X0 X1 X2) \end{aligned} \tag{3}$$

Assume the following.

$$\forall X0.(l1\_rlvect\_1 X0)\Rightarrow(l2\_algstr\_0 X0) \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.m1\_subset\_1 (k6\_subset\_1 X0 X1) (k1\_zfmisc\_1 X0) \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2\_struct\_0 X0)\wedge((v13\_algstr\_0 X0)\wedge \\ & ((v2\_rlvect\_1 X0)\wedge((v3\_rlvect\_1 X0)\wedge((v4\_rlvect\_1 X0)\wedge((v5\_rlvect\_1 \\ & X0)\wedge((v6\_rlvect\_1 X0)\wedge((v7\_rlvect\_1 X0)\wedge((v8\_rlvect\_1 X0)\wedge \\ & (l1\_rlvect\_1 X0))))))))))\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ X0)))\Rightarrow((v1\_funct\_1 (k4\_morph\_01 X0 X1))\wedge((v1\_funct\_2 (k4\_morph\_01 \\ X0 X1) (k9\_setfam\_1 (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 \\ X0)))\wedge(m1\_subset\_1 (k4\_morph\_01 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ (k9\_setfam\_1 (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 X0))))))) \quad (6) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2\_struct\_0 X0)\wedge((v13\_algstr\_0 X0)\wedge \\ & ((v2\_rlvect\_1 X0)\wedge((v3\_rlvect\_1 X0)\wedge((v4\_rlvect\_1 X0)\wedge((v5\_rlvect\_1 \\ & X0)\wedge((v6\_rlvect\_1 X0)\wedge((v7\_rlvect\_1 X0)\wedge((v8\_rlvect\_1 X0)\wedge \\ & (l1\_rlvect\_1 X0))))))))))\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ X0)))\Rightarrow((v1\_funct\_1 (k3\_morph\_01 X0 X1))\wedge((v1\_funct\_2 (k3\_morph\_01 \\ X0 X1) (k9\_setfam\_1 (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 \\ X0)))\wedge(m1\_subset\_1 (k3\_morph\_01 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ (k9\_setfam\_1 (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 X0))))))) \quad (7) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0)\wedge((v13\_algstr\_0 X0)\wedge((v2\_rlvect\_1 \\ X0)\wedge((v3\_rlvect\_1 X0)\wedge((v4\_rlvect\_1 X0)\wedge((v5\_rlvect\_1 X0)\wedge \\ & ((v6\_rlvect\_1 X0)\wedge((v7\_rlvect\_1 X0)\wedge((v8\_rlvect\_1 X0)\wedge(l1\_rlvect\_1 \\ X0))))))))))\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ X0)))\Rightarrow(\forall X2.((v1\_funct\_1 X2)\wedge((v1\_funct\_2 X2 (k9\_setfam\_1 \\ (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 X0)))\wedge(m1\_subset\_1 \\ X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k9\_setfam\_1 (u1\_struct\_0 X0)) ( \\ k9\_setfam\_1 (u1\_struct\_0 X0))))))\Rightarrow((X2 = k4\_morph\_01 X0 X1)\Leftrightarrow \\ & (\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))\Rightarrow \\ & (k3\_funct\_2 (k1\_zfmisc\_1 (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 \\ X0)) X2 X3 = k1\_morph\_01 X0 X3 X1)))))) \quad (8) \end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v5\_rlvect\_1 X0) \wedge \\
& ((v6\_rlvect\_1 X0) \wedge ((v7\_rlvect\_1 X0) \wedge ((v8\_rlvect\_1 X0) \wedge (l1\_rlvect\_1 \\
& X0)))))))))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\
& X0))) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k9\_setfam\_1 \\
& (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 X0))) \wedge (m1\_subset\_1 \\
& X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k9\_setfam\_1 (u1\_struct\_0 X0)) ( \\
& k9\_setfam\_1 (u1\_struct\_0 X0)))))) \Rightarrow ((X2 = k3\_morph\_01 X0 X1) \Leftrightarrow \\
& (\forall X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow \\
& (k3\_funct\_2 (k1\_zfmisc\_1 (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 \\
& X0)) X2 X3 = k2\_morph\_01 X0 X3 X1))))))
\end{aligned} \tag{9}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v5\_rlvect\_1 X0) \wedge \\
& ((v6\_rlvect\_1 X0) \wedge ((v7\_rlvect\_1 X0) \wedge ((v8\_rlvect\_1 X0) \wedge (l1\_rlvect\_1 \\
& X0)))))))))) \Rightarrow (\forall X1.((\neg v1\_xboole\_0 X1) \wedge (m1\_subset\_1 X1 \\
& (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow (\forall X2.((\neg v1\_xboole\_0 \\
& X2) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow ((k3\_funct\_2 \\
& (k1\_zfmisc\_1 (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 X0)) \\
& (k3\_morph\_01 X0 X1) (k6\_subset\_1 (u1\_struct\_0 X0) X2) = k6\_subset\_1 \\
& (u1\_struct\_0 X0) (k3\_funct\_2 (k1\_zfmisc\_1 (u1\_struct\_0 X0)) ( \\
& k9\_setfam\_1 (u1\_struct\_0 X0)) (k4\_morph\_01 X0 X1) X2)) \wedge (k3\_funct\_2 \\
& (k1\_zfmisc\_1 (u1\_struct\_0 X0)) (k9\_setfam\_1 (u1\_struct\_0 X0)) \\
& (k4\_morph\_01 X0 X1) (k6\_subset\_1 (u1\_struct\_0 X0) X2) = k6\_subset\_1 \\
& (u1\_struct\_0 X0) (k3\_funct\_2 (k1\_zfmisc\_1 (u1\_struct\_0 X0)) ( \\
& k9\_setfam\_1 (u1\_struct\_0 X0)) (k3\_morph\_01 X0 X1) X2))))))
\end{aligned}$$