

t32_sublemma (TMVMeucre4f4BTSc31fZktEpfsvcfCSytem)

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Let $m1_qc_lang1 : \iota \Rightarrow o$ be given. Let $m2_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_qc_lang1 : \iota \Rightarrow \iota$ be given. Let $k3_qc_lang1 : \iota \Rightarrow \iota$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $m2_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_valuat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k16_subst1 : \iota \Rightarrow \iota$ be given. Let $k38_subst1 : \iota \Rightarrow \iota$ be given. Let $k9_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $k19_subst1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_subst1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_sublemma : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_sublemma : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $k3_relat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_relset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $m1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_subst1 : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1_relat_1 X1) \wedge (v1_funct_1 X1)) \Rightarrow (\forall X2. \\ & ((v1_relat_1 X2) \wedge (v1_funct_1 X2)) \Rightarrow ((X0 \in k9_xtuple_0 X1) \Rightarrow (k1_funct_1 \\ & (k3_relat_1 X1 X2) X0 = k1_funct_1 X2 (k1_funct_1 X1 X0)))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. (m1_qc_lang1 X0) \Rightarrow (\forall X1. (m2_subset_1 X1 (k2_qc_lang1 \\ & X0) (k3_qc_lang1 X0)) \Rightarrow (\forall X2. (\neg v1_xboole_0 X2) \Rightarrow (\forall X3. \\ & (m2_funct_2 X3 (k3_qc_lang1 X0) X2 (k2_valuat_1 X0 X2)) \Rightarrow (\forall X4. \\ & (m2_subset_1 X4 (k16_subst1 X0) (k38_subst1 X0)) \Rightarrow ((X1 \in k9_xtuple_0 \\ & (k19_subst1 X0 X4)) \Rightarrow (k3_funct_2 (k3_qc_lang1 X0) X2 (k1_sublemma \\ & X0 X2 X3 (k3_sublemma X0 X4 X2 X3)) X1 = k1_funct_1 (k3_sublemma X0 \\ & X4 X2 X3) X1)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. \forall X4. \forall X5. \\ & (((m1_subset_1 X4 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1))) \wedge (m1_subset_1 \\ & X5 (k1_zfmisc_1 (k2_zfmisc_1 X2 X3)))) \Rightarrow (k4_relset_1 X0 X1 X2 X3 \\ & X4 X5 = k3_relat_1 X4 X5)) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0.\forall X1.((m1_qc_lang1\ X0)\wedge(m1_subset_1\ X1\ (k16_subst1\ X0)))\Rightarrow(k19_subst1\ X0\ X1 = k2_xtuple_0\ X1) \quad (4)$$

Assume the following.

$$\forall X0.(m1_qc_lang1\ X0)\Rightarrow(\neg v1_xboole_0\ (k38_subst1\ X0)) \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1_xboole_0\ X0)\wedge((\neg v1_xboole_0\ X1)\wedge(m1_subset_1\ X1\ (k1_zfmisc_1\ X0))))\Rightarrow(\forall X2.(m2_subset_1\ X2\ X0\ X1)\Rightarrow(m1_subset_1\ X2\ X0)) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((\neg v1_xboole_0\ X1)\wedge(m1_funct_2\ X2\ X0\ X1))\Rightarrow(\forall X3.(m2_funct_2\ X3\ X0\ X1\ X2)\Rightarrow((v1_funct_1\ X3)\wedge((v1_funct_2\ X3\ X0\ X1)\wedge(m1_subset_1\ X3\ (k1_zfmisc_1\ (k2_zfmisc_1\ X0\ X1)))))) \quad (7)$$

Assume the following.

$$\forall X0.(m1_qc_lang1\ X0)\Rightarrow(m1_subset_1\ (k38_subst1\ X0)\ (k1_zfmisc_1\ (k16_subst1\ X0))) \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.((m1_qc_lang1\ X0)\wedge(\neg v1_xboole_0\ X1))\Rightarrow(m1_funct_2\ (k2_valuat_1\ X0\ X1)\ (k3_qc_lang1\ X0\ X1)) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.((m1_qc_lang1\ X0)\wedge(m1_subset_1\ X1\ (k1_subst1\ X0)))\Rightarrow((v1_funct_1\ (k2_subst1\ X0\ X1))\wedge(m1_subset_1\ (k2_subst1\ X0\ X1)\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k3_qc_lang1\ X0)\ (k3_qc_lang1\ X0)))))) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.((m1_qc_lang1\ X0)\wedge(m1_subset_1\ X1\ (k16_subst1\ X0)))\Rightarrow(m1_subset_1\ (k19_subst1\ X0\ X1)\ (k1_subst1\ X0)) \quad (11)$$

Assume the following.

$$\forall X0.(m1_qc_lang1\ X0)\Rightarrow(\forall X1.(m1_subset_1\ X1\ (k1_subst1\ X0))\Rightarrow(k2_subst1\ X0\ X1 = X1)) \quad (12)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1\ X0) \Rightarrow (\forall X1.(m2_subset_1\ X1\ (k16_subst1 \\ X0)\ (k38_subst1\ X0)) \Rightarrow (\forall X2.(\neg v1_xboole_0\ X2) \Rightarrow (\forall X3. \\ (m2_funct_2\ X3\ (k3_qc_lang1\ X0)\ X2\ (k2_valuat_1\ X0\ X2)) \Rightarrow (k3_sublemma \\ X0\ X1\ X2\ X3 = k4_relset_1\ (k3_qc_lang1\ X0)\ (k3_qc_lang1\ X0)\ (k3_qc_lang1 \\ X0)\ X2\ (k2_subst1\ X0\ (k19_subst1\ X0\ X1))\ X3)))) \end{aligned} \quad (13)$$

Assume the following.

$$\forall X0.(v1_xboole_0\ X0) \Rightarrow (\forall X1.(m1_subset_1\ X1\ (k1_zfmisc_1 \\ X0)) \Rightarrow (v1_xboole_0\ X1)) \quad (14)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1_subset_1\ X2\ (k1_zfmisc_1 \\ (k2_zfmisc_1\ X0\ X1))) \Rightarrow (v1_relat_1\ X2) \quad (15)$$

Theorem 1

$$\begin{aligned} \forall X0.(m1_qc_lang1\ X0) \Rightarrow (\forall X1.(m2_subset_1\ X1\ (k2_qc_lang1 \\ X0)\ (k3_qc_lang1\ X0)) \Rightarrow (\forall X2.(\neg v1_xboole_0\ X2) \Rightarrow (\forall X3. \\ (m2_funct_2\ X3\ (k3_qc_lang1\ X0)\ X2\ (k2_valuat_1\ X0\ X2)) \Rightarrow (\forall X4. \\ (m2_subset_1\ X4\ (k16_subst1\ X0)\ (k38_subst1\ X0)) \Rightarrow ((X1 \in k9_xtuple_0 \\ (k19_subst1\ X0\ X4)) \Rightarrow (k1_funct_1\ X3\ (k1_funct_1\ (k2_subst1 \\ X0\ (k19_subst1\ X0\ X4))\ X1) = k3_funct_2\ (k3_qc_lang1\ X0)\ X2\ (k1_sublemma \\ X0\ X2\ X3\ (k3_sublemma\ X0\ X4\ X2\ X3))\ X1)))))) \end{aligned}$$