

t33\_arytm\_3  
(TMZhiWbJpoiX75nyXduW1TLs6uZZLutj3Gf)

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Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_arytm\_3 : \iota$  be given. Let  $r1\_arytm\_3 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k6\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $c2\_arytm\_3 : \iota$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. \neg k4\_tarski X0 X1 \in k4\_ordinal1 \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. \forall X3. (k4\_tarski X0 X1 = k4\_tarski X2 X3) \Rightarrow ((X0 = X2) \wedge (X1 = X3)) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. k6\_subset\_1 X0 X1 = k4\_xboole\_0 X0 X1 \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((v3\_ordinal1 X0) \wedge (v7\_ordinal1 X0)) \Rightarrow (\forall X1. \\ & ((v3\_ordinal1 X1) \wedge (v7\_ordinal1 X1)) \Rightarrow ((k4\_tarski X0 X1 \in c2\_arytm\_3) \Rightarrow \\ & ((r1\_arytm\_3 X0 X1) \wedge (X1 \neq k1\_xboole\_0)))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} c2\_arytm\_3 = & ReplSep2 (toset (\lambda X0 : \iota. m1\_subset\_1 X0 k4\_ordinal1)) \\ & (\lambda X0 : \iota. toset (\lambda X1 : \iota. m1\_subset\_1 X1 k4\_ordinal1)) \\ & (\lambda X0 : \iota. \lambda X1 : \iota. (r1\_arytm\_3 X0 X1) \wedge (X1 \neq k1\_xboole\_0)) \\ & (\lambda X0 : \iota. \lambda X1 : \iota. k4\_tarski X0 X1) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned}
& k5\_arytm\_3 = k2\_xboole\_0 (k6\_subset\_1 (ReplSep2 (toset (\lambda X0 : \\
& \quad \iota.m1\_subset\_1 X0 k4\_ordinal1)) (\lambda X0 : \iota.toset (\lambda X1 : \\
& \quad \iota.m1\_subset\_1 X1 k4\_ordinal1)) (\lambda X0 : \iota.\lambda X1 : \iota.(r1\_arytm\_3 \\
& \quad X0 X1) \wedge (X1 \neq k1\_xboole\_0)) (\lambda X0 : \iota.\lambda X1 : \iota.k4\_tarski \\
& X0 X1)) (ReplSep (toset (\lambda X0 : \iota.m1\_subset\_1 X0 k4\_ordinal1)) \\
& (\lambda X0 : \iota.True) (\lambda X0 : \iota.k4\_tarski X0 np\_1))) k4\_ordinal1
\end{aligned} \tag{6}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.(X2 = k4\_xboole\_0 X0 X1) \Leftrightarrow (\forall X3. \\
& (X3 \in X2) \Leftrightarrow ((X3 \in X0) \wedge (\neg X3 \in X1)))
\end{aligned} \tag{7}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.k4\_tarski X0 X1 = k2\_tarski (k2\_tarski X0 \\
& X1) (k1\_tarski X0)
\end{aligned} \tag{8}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.(X2 = k2\_xboole\_0 X0 X1) \Leftrightarrow (\forall X3. \\
& (X3 \in X2) \Leftrightarrow ((X3 \in X0) \vee (X3 \in X1)))
\end{aligned} \tag{9}$$

Assume the following.

$$\forall X0.\forall X1.k2\_xboole\_0 X0 X1 = k2\_xboole\_0 X1 X0 \tag{10}$$

Assume the following.

$$\forall X0.\forall X1.k2\_tarski X0 X1 = k2\_tarski X1 X0 \tag{11}$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k4\_ordinal1) \Rightarrow (v7\_ordinal1 X0) \tag{12}$$

Assume the following.

$$\forall X0.(v7\_ordinal1 X0) \Rightarrow (v3\_ordinal1 X0) \tag{13}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k4\_ordinal1) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& X1 k4\_ordinal1) \Rightarrow ((k4\_tarski X0 X1 \in k5\_arytm\_3) \Leftrightarrow ((r1\_arytm\_3 \\
& X0 X1) \wedge ((X1 \neq k1\_xboole\_0) \wedge (X1 \neq np\_1))))))
\end{aligned}$$