

# t33\_hilbert3

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v2\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_hilbert3 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_hilbert3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_hilbert1 : \iota$  be given. Let  $k5\_hilbert3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_partfun1 : \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_relat\_1 : \iota \Rightarrow \iota$  be given. Let  $m2\_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_hilbert3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_hilbert1 : \iota$  be given. Let  $k2\_hilbert3 : \iota \Rightarrow \iota$  be given. Let  $k1\_msualg\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k1\_hilbert2 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_hilbert1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k16\_funct\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_hilbert1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_hilbert3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. (((v1\_funct\_1 X2) \wedge \\ & ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X1)))))) \wedge ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 X0 X1) \wedge (m1\_subset\_1 \\ & X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \Rightarrow ((r2\_funct\_2 X0 X1 X2 \\ & X3) \Leftrightarrow (X2 = X3)) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. k6\_partfun1 X0 = k4\_relat\_1 X0 \tag{2}$$

Assume the following.

$$\forall X0. (v1\_relat\_1 (k4\_relat\_1 X0)) \wedge (v1\_funct\_1 (k4\_relat\_1 X0)) \tag{3}$$

Assume the following.

$$\forall X0. (v1\_partfun1 (k6\_partfun1 X0) X0) \wedge (m1\_subset\_1 (k6\_partfun1 X0) (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0))) \tag{4}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v2\_relat\_1 X0)\wedge(( \\ & v4\_relat\_1 X0 k5\_numbers)\wedge((v1\_funct\_1 X0)\wedge(v1\_partfun1 X0 k5\_numbers))))))\wedge \\ & (m1\_hilbert3 X1 X0))\Rightarrow(m2\_pboole (k4\_hilbert3 X0 X1) k1\_hilbert1 \\ & (k2\_hilbert3 X0) (k2\_hilbert3 X0)) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0)\wedge((v2\_relat\_1 X0)\wedge((v4\_relat\_1 X0 \\ & k5\_numbers)\wedge((v1\_funct\_1 X0)\wedge(v1\_partfun1 X0 k5\_numbers))))))\Rightarrow \\ & ((v1\_relat\_1 (k2\_hilbert3 X0))\wedge((v4\_relat\_1 (k2\_hilbert3 X0) \\ & k1\_hilbert1)\wedge((v1\_funct\_1 (k2\_hilbert3 X0))\wedge(v1\_partfun1 ( \\ & k2\_hilbert3 X0) k1\_hilbert1)))) \end{aligned} \quad (6)$$

Assume the following.

$$m1\_subset\_1 k2\_hilbert1 k1\_hilbert1 \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0)\wedge((v2\_relat\_1 X0)\wedge((v4\_relat\_1 X0 \\ & k5\_numbers)\wedge((v1\_funct\_1 X0)\wedge(v1\_partfun1 X0 k5\_numbers))))))\Rightarrow \\ & (\forall X1.(m1\_hilbert3 X1 X0)\Rightarrow(\forall X2.(m1\_subset\_1 X2 k1\_hilbert1)\Rightarrow \\ & (k5\_hilbert3 X0 X1 X2 = k1\_msualg\_3 k1\_hilbert1 (k2\_hilbert3 X0) \\ & (k2\_hilbert3 X0) (k4\_hilbert3 X0 X1) X2))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v2\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 \\
& k5\_numbers) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 X0 k5\_numbers)))))) \Rightarrow \\
& (\forall X1.(m1\_hilbert3 X1 X0) \Rightarrow (\forall X2.(m2\_pboole X2 k1\_hilbert1 \\
& (k2\_hilbert3 X0) (k2\_hilbert3 X0)) \Rightarrow ((X2 = k4\_hilbert3 X0 X1) \Leftrightarrow ( \\
& (k1\_msualg\_3 k1\_hilbert1 (k2\_hilbert3 X0) (k2\_hilbert3 X0) X2 \\
& k2\_hilbert1 = k6\_partfun1 np\_1) \wedge ((\forall X3.(m2\_subset\_1 X3 \\
& k1\_numbers k5\_numbers) \Rightarrow (k1\_msualg\_3 k1\_hilbert1 (k2\_hilbert3 \\
& X0) (k2\_hilbert3 X0) X2 (k1\_hilbert2 X3) = k1\_funct\_1 X1 X3)) \wedge (\forall X3. \\
& (m1\_subset\_1 X3 k1\_hilbert1) \Rightarrow (\forall X4.(m1\_subset\_1 X4 k1\_hilbert1) \Rightarrow \\
& (\exists X5.((v1\_funct\_1 X5) \wedge ((v1\_funct\_2 X5 (k3\_hilbert3 X0 \\
& X3) (k3\_hilbert3 X0 X3)) \wedge ((v3\_funct\_2 X5 (k3\_hilbert3 X0 X3) (k3\_hilbert3 \\
& X0 X3)) \wedge (m1\_subset\_1 X5 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k3\_hilbert3 \\
& X0 X3) (k3\_hilbert3 X0 X3)))))))))) \wedge (\exists X6.((v1\_funct\_1 X6) \wedge \\
& ((v1\_funct\_2 X6 (k3\_hilbert3 X0 X4) (k3\_hilbert3 X0 X4)) \wedge ((v3\_funct\_2 \\
& X6 (k3\_hilbert3 X0 X4) (k3\_hilbert3 X0 X4)) \wedge (m1\_subset\_1 X6 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 (k3\_hilbert3 X0 X4) (k3\_hilbert3 X0 X4)))))))))) \wedge (( \\
& X5 = k1\_msualg\_3 k1\_hilbert1 (k2\_hilbert3 X0) (k2\_hilbert3 X0) \\
& X2 X3) \wedge ((X6 = k1\_msualg\_3 k1\_hilbert1 (k2\_hilbert3 X0) (k2\_hilbert3 \\
& X0) X2 X4) \wedge ((k1\_msualg\_3 k1\_hilbert1 (k2\_hilbert3 X0) (k2\_hilbert3 \\
& X0) X2 (k4\_hilbert1 X3 X4) = k16\_funct\_3 (k3\_hilbert3 X0 X3) (k3\_hilbert3 \\
& X0 X4) (k3\_hilbert3 X0 X3) (k3\_hilbert3 X0 X4) X5 X6) \wedge (k1\_msualg\_3 \\
& k1\_hilbert1 (k2\_hilbert3 X0) (k2\_hilbert3 X0) X2 (k3\_hilbert1 \\
& X3 X4) = k1\_hilbert3 (k3\_hilbert3 X0 X3) (k3\_hilbert3 X0 X4) X5 X6))))))))))))) \\
& \tag{9}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v2\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 \\
& k5\_numbers) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 X0 k5\_numbers)))))) \Rightarrow \\
& (\forall X1.(m1\_subset\_1 X1 k1\_hilbert1) \Rightarrow (k3\_hilbert3 X0 X1 = \\
& k1\_funct\_1 (k2\_hilbert3 X0) X1)) \\
& \tag{10}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v2\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 \\
& k5\_numbers) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 X0 k5\_numbers)))))) \Rightarrow \\
& (\forall X1.((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 k1\_hilbert1) \wedge ( \\
& (v1\_funct\_1 X1) \wedge (v1\_partfun1 X1 k1\_hilbert1)))))) \Rightarrow ((X1 = k2\_hilbert3 \\
& X0) \Leftrightarrow ((k1\_funct\_1 X1 k2\_hilbert1 = np\_1) \wedge ((\forall X2.(m2\_subset\_1 \\
& X2 k1\_numbers k5\_numbers) \Rightarrow (k1\_funct\_1 X1 (k1\_hilbert2 X2) = k1\_funct\_1 \\
& X0 X2)) \wedge (\forall X2.(m1\_subset\_1 X2 k1\_hilbert1) \Rightarrow (\forall X3. \\
& (m1\_subset\_1 X3 k1\_hilbert1) \Rightarrow ((k1\_funct\_1 X1 (k4\_hilbert1 X2 \\
& X3) = k2\_zfmisc\_1 (k1\_funct\_1 X1 X2) (k1\_funct\_1 X1 X3)) \wedge (k1\_funct\_1 \\
& X1 (k3\_hilbert1 X2 X3) = k1\_funct\_2 (k1\_funct\_1 X1 X2) (k1\_funct\_1 \\
& X1 X3)))))))))) \\
& \tag{11}
\end{aligned}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v2\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 \\ & k5\_numbers) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 X0 k5\_numbers)))))) \Rightarrow \\ & (\forall X1.(m1\_hilbert3 X1 X0) \Rightarrow (r2\_funct\_2 (k3\_hilbert3 X0 k2\_hilbert1) \\ & (k3\_hilbert3 X0 k2\_hilbert1) (k5\_hilbert3 X0 X1 k2\_hilbert1) ( \\ & k6\_partfun1 (k3\_hilbert3 X0 k2\_hilbert1)))) \end{aligned}$$