t33_member_1 (TMb1EqXfvs5ooVMj6AJdS4dcYEdf68aenLw)

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Let $v1_membered : \iota \Rightarrow o$ be given. Let $k7_member_1 : \iota \Rightarrow \iota$ be given. Let $k3_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

 $\forall X0.(v1_membered \ X0) \Rightarrow (\forall X1.(v1_membered \ X1) \Rightarrow ((r1_tarski \ X0 \ X1) \Leftrightarrow (r1_tarski \ (k7_member_1 \ X0) \ (k7_member_1 \ X1))))$ (1)

Assume the following.

$$\forall X0.\forall X1.(r1_tarski X0 X1) \Rightarrow (k3_xboole_0 X0 X1 = X0)$$
⁽²⁾

Assume the following.

$$\forall X0.\forall X1.r1_tarski \ (k3_xboole_0 \ X0 \ X1) \ X0 \tag{3}$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.k3_xboole_0 \ (k3_xboole_0 \ X0 \\ X1) \ X2 = k3_xboole_0 \ X0 \ (k3_xboole_0 \ X1 \ X2)$$

$$(4)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(r1_tarski \ X0 \ X1) \Rightarrow (r1_tarski \ (5)$$

$$(k3_xboole_0 \ X0 \ X2) \ X1)$$

Assume the following.

 $\forall X0.(v1_membered \ X0) \Rightarrow (\forall X1.(v1_membered \ X1) \Rightarrow ((r1_tarski \ X0 \ X1) \Rightarrow (r1_tarski \ (k7_member_1 \ X0) \ (k7_member_1 \ X1))))$ (6)

Assume the following.

$$\forall X0.(v1_membered \ X0) \Rightarrow (k7_member_1 \ (k7_member_1 \ X0) = X0)$$
(7)

Assume the following.

$$\forall X0.\forall X1.(v1_membered \ X0) \Rightarrow (v1_membered \ (k3_xboole_0 X1 \ X0))$$
(8)

Assume the following.

$$\forall X0.\forall X1.(v1_membered \ X0) \Rightarrow (v1_membered \ (k3_xboole_0 X0 \ X1))$$
(9)

Assume the following.

$$\forall X0.(v1_membered \ X0) \Rightarrow (v1_membered \ (k7_member_1 \ X0))$$
(10)

Assume the following.

$$\forall X0.\forall X1.k3_xboole_0 \ X0 \ X1 = k3_xboole_0 \ X1 \ X0 \tag{11}$$

Theorem 1

$$\begin{array}{l} \forall X0.(v1_membered \ X0) \Rightarrow (\forall X1.(v1_membered \ X1) \Rightarrow (k7_member_1 \ (k3_xboole_0 \ X0 \ X1) = k3_xboole_0 \ (k7_member_1 \ X0) \ (k7_member_1 \ X1))) \end{array}$$