# t33_member_1 <br> (TMb1EqXfvs5ooVMj6AJdS4dcYEdf68aenLw) 

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Let $v 1 \_$membered : $\iota \Rightarrow 0$ be given. Let $k 7$ _member_1 : $\iota \Rightarrow \iota$ be given. Let $k 3 \_x$ boole_0 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r 1 \_$tarski : $\iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(( \right. \\
\left.\left.\left.r 1 \_ \text {tarski } X 0 X 1\right) \Leftrightarrow\left(r 1 \_ \text {tarski }\left(k 7 \_m e m b e r \_1 X 0\right)\left(k 7 \_m e m b e r \_1 X 1\right)\right)\right)\right) \tag{1}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 .\left(r 1 \_t a r s k i \quad X 0 X 1\right) \Rightarrow\left(k 3 \_x b o o l e \_0 X 0 X 1=X 0\right) \tag{2}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . r 1 \_t a r s k i\left(k 3 \_x b o o l e \_0 X 0 X 1\right) X 0 \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 . \forall X 2 . k 3 \_x b o o l e \_0\left(k 3 \_x b o o l e \_0 X 0\right. \\
X 1) X 2=k 3 \_x b o o l e \_0 X 0\left(k 3 \_x b o o l e \_0 X 1 X 2\right) \tag{4}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 . \forall X 2 .\left(r 1 \_t a r s k i X 0 X 1\right) \Rightarrow\left(r 1 \_t a r s k i\right.  \tag{5}\\
\left.\left(k 3 \_x b o o l e \_0 X 0 X 2\right) X 1\right)
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow((\right. \tag{6}
\end{equation*}
$$

$\left.\left.\left.r 1 \_t a r s k i X 0 X 1\right) \Rightarrow\left(r 1 \_t a r s k i\left(k 7 \_m e m b e r \_1 X 0\right)\left(k 7 \_m e m b e r \_1 ~ X 1\right)\right)\right)\right)$
Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(k 7 \_m e m b e r \_1\left(k 7 \_m e m b e r \_1 X 0\right)=X 0\right) \tag{7}
\end{equation*}
$$

Assume the following.

$$
\begin{array}{r}
\forall X 0 . \forall X 1 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(v 1 \_ m e m b e r e d \quad \left(k 3 \_x b o o l e \_0\right.\right. \\
X 1 X 0)) \tag{8}
\end{array}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 1 \_ m e m b e r e d ~ \left(k 3 \_x b o o l e \_0\right.\right.  \tag{9}\\
X 0 X 1))
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 7 \_m e m b e r \_1 X 0\right)\right) \tag{10}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . k 3 \_x b o o l e \_0 X 0 X 1=k 3 \_x b o o l e \_0 X 1 X 0 \tag{11}
\end{equation*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d \quad X 1\right) \Rightarrow\left(k 7 \_m e m b e r \_1\right.\right.$
$\left(k 3 \_x b o o l e \_0 X 0 X 1\right)=k 3 \_x b o o l e \_0\left(k 7 \_m e m b e r \_1 ~ X 0\right) ~\left(k 7 \_m e m b e r \_1\right.$ X1)))

