

t34\_xxreal\_3 (TMdyuJPuhuxWtpdKB-  
szFfM4vzSW8LJDnddb)

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Let  $v1\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $k1\_xxreal\_3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_xxreal\_3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_xxreal\_3 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xxreal\_0 X0) \Rightarrow (\forall X1.(v1\_xxreal\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xxreal\_0 X2) \Rightarrow ((v1\_xreal\_0 X0) \Rightarrow (k3\_xxreal\_3 (k1\_xxreal\_3 \\ & X0 X1) (k1\_xxreal\_3 X0 X2) = k3\_xxreal\_3 X1 X2)))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xxreal\_0 X0) \Rightarrow (\forall X1.(v1\_xxreal\_0 X1) \Rightarrow (( \\ & k2\_xxreal\_3 (k1\_xxreal\_3 (k2\_xxreal\_3 X0) X1) = k3\_xxreal\_3 X0 \\ & X1) \wedge (k2\_xxreal\_3 (k1\_xxreal\_3 (k2\_xxreal\_3 X0) X1) = k1\_xxreal\_3 \\ & X0 (k2\_xxreal\_3 X1)))) \end{aligned} \quad (2)$$

Assume the following.

$$\forall X0.(v1\_xxreal\_0 X0) \Rightarrow (k2\_xxreal\_3 (k2\_xxreal\_3 X0) = X0) \quad (3)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xxreal\_0 X0) \wedge (v1\_xxreal\_0 X1)) \Rightarrow (v1\_xxreal\_0 (k3\_xxreal\_3 X0 X1)) \quad (4)$$

Assume the following.

$$\forall X0.(v1\_xxreal\_0 X0) \Rightarrow (v1\_xxreal\_0 (k2\_xxreal\_3 X0)) \quad (5)$$

Assume the following.

$$\forall X0.(v1\_xxreal\_0 X0) \Rightarrow (\forall X1.(v1\_xxreal\_0 X1) \Rightarrow (k3\_xxreal\_3 X0 X1 = k1\_xxreal\_3 X0 (k2\_xxreal\_3 X1))) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xxreal\_0 X0) \wedge (v1\_xxreal\_0 X1)) \Rightarrow (k1\_xxreal\_3 X0 X1 = k1\_xxreal\_3 X1 X0) \quad (7)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(v1\_xxreal\_0 X0) \Rightarrow (\forall X1.(v1\_xxreal\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xxreal\_0 X2) \Rightarrow ((v1\_xxreal\_0 X0) \Rightarrow (k1\_xxreal\_3 (k3\_xxreal\_3 \\ & X1 X0) (k3\_xxreal\_3 X0 X2) = k3\_xxreal\_3 X1 X2)))) \end{aligned}$$