

# t35\_gcd\_1 (TMMsepoJGGXnhBMyFMB- CAX3vZuJmC23PBwz)

October 27, 2020

Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v6\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $v5\_group\_1 : \iota \Rightarrow o$  be given. Let  $v4\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v5\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v1\_vectsp\_2 : \iota \Rightarrow o$  be given. Let  $v3\_gcd\_1 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $m2\_gcd\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k5\_gcd\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_gcd\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $l4\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l2\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l5\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l4\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v6\_vectsp\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((\neg v6\_struct\_0 X0) \wedge ((v13\_algstr\_0 \\
& X0) \wedge ((v3\_group\_1 X0) \wedge ((v5\_group\_1 X0) \wedge ((v4\_vectsp\_1 X0) \wedge (( \\
& v5\_vectsp\_1 X0) \wedge ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 \\
& X0) \wedge ((v1\_vectsp\_2 X0) \wedge ((v3\_gcd\_1 X0) \wedge (l6\_algstr\_0 X0)))))))))) \Rightarrow \\
& (\forall X1. (m2\_gcd\_1 X1 X0) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X3. (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4. \\
& (m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow ((r2\_gcd\_1 X0 X4 (k5\_gcd\_1 X0 \\
& X1 X2 X3)) \Rightarrow ((r2\_gcd\_1 X0 X4 X2) \wedge (r2\_gcd\_1 X0 X4 X3))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge ((v3\_vectsp\_1 \\
& X0) \wedge (l4\_algstr\_0 X0))) \wedge ((m1\_subset\_1 X1 (u1\_struct\_0 X0)) \wedge ( \\
& m1\_subset\_1 X2 (u1\_struct\_0 X0)))) \Rightarrow (r2\_gcd\_1 X0 X1 X1)
\end{aligned} \tag{2}$$

Assume the following.

$$\forall X0. (l6\_algstr\_0 X0) \Rightarrow ((l2\_algstr\_0 X0) \wedge (l5\_algstr\_0 X0)) \tag{3}$$

Assume the following.

$$\forall X0. (l5\_algstr\_0 X0) \Rightarrow ((l4\_algstr\_0 X0) \wedge (l4\_struct\_0 X0)) \tag{4}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((\neg v2\_struct\_0 \\ & X0)\wedge((v3\_group\_1 X0)\wedge((v4\_vectsp\_1 X0)\wedge((v3\_gcd\_1 X0)\wedge(l4\_algstr\_0 \\ & X0))))))\wedge((m2\_gcd\_1 X1 X0)\wedge((m1\_subset\_1 X2 (u1\_struct\_0 X0))\wedge \\ & (m1\_subset\_1 X3 (u1\_struct\_0 X0))))\Rightarrow(m1\_subset\_1 (k5\_gcd\_1 \\ & X0 X1 X2 X3) (u1\_struct\_0 X0)) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.(((\neg v2\_struct\_0 X0)\wedge((v3\_group\_1 X0)\wedge((v4\_vectsp\_1 \\ & X0)\wedge((v3\_gcd\_1 X0)\wedge(l4\_algstr\_0 X0))))))\Rightarrow(\forall X1.(m2\_gcd\_1 \\ & X1 X0)\Rightarrow(\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0))\Rightarrow(\forall X3. \\ & (m1\_subset\_1 X3 (u1\_struct\_0 X0))\Rightarrow(\forall X4.(m1\_subset\_1 X4 \\ & (u1\_struct\_0 X0))\Rightarrow((X4 = k5\_gcd\_1 X0 X1 X2 X3)\Leftrightarrow((X4 \in X1)\wedge((r2\_gcd\_1 \\ & X0 X4 X2)\wedge((r2\_gcd\_1 X0 X4 X3)\wedge(\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 \\ & X0))\Rightarrow(((r2\_gcd\_1 X0 X5 X2)\wedge(r2\_gcd\_1 X0 X5 X3))\Rightarrow(r2\_gcd\_1 X0 X5 \\ & X4)))))))))) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0.(l4\_algstr\_0 X0)\Rightarrow(((\neg v2\_struct\_0 X0)\wedge(v4\_vectsp\_1 X0))\Rightarrow((\neg v2\_struct\_0 X0)\wedge((v3\_vectsp\_1 X0)\wedge(v6\_vectsp\_1 X0))) \quad (7)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(((\neg v2\_struct\_0 X0)\wedge((\neg v6\_struct\_0 X0)\wedge((v13\_algstr\_0 \\ & X0)\wedge((v3\_group\_1 X0)\wedge((v5\_group\_1 X0)\wedge((v4\_vectsp\_1 X0)\wedge(( \\ & v5\_vectsp\_1 X0)\wedge((v2\_rlvect\_1 X0)\wedge((v3\_rlvect\_1 X0)\wedge((v4\_rlvect\_1 \\ & X0)\wedge((v1\_vectsp\_2 X0)\wedge((v3\_gcd\_1 X0)\wedge(l6\_algstr\_0 X0))))))))))\Rightarrow \\ & (\forall X1.(m2\_gcd\_1 X1 X0)\Rightarrow(\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\ & X0))\Rightarrow(\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0))\Rightarrow(\forall X4. \\ & (m1\_subset\_1 X4 (u1\_struct\_0 X0))\Rightarrow(k5\_gcd\_1 X0 X1 (k5\_gcd\_1 X0 \\ & X1 X2 X3) X4 = k5\_gcd\_1 X0 X1 X2 (k5\_gcd\_1 X0 X1 X3 X4)))))) \end{aligned}$$