

t35_pboole (TMWCgyna-jSdx3395MRwzEV8ZJoG6K9vTenT)

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Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v4_relat_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r6_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k3_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r2_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1_relat_1 X1) \wedge ((v4_relat_1 X1 X0) \wedge \\ & (v1_funct_1 X1) \wedge (v1_partfun1 X1 X0))) \Rightarrow (\forall X2. ((v1_relat_1 \\ & X2) \wedge ((v4_relat_1 X2 X0) \wedge ((v1_funct_1 X2) \wedge (v1_partfun1 X2 X0)))) \Rightarrow \\ & (\forall X3. ((v1_relat_1 X3) \wedge ((v4_relat_1 X3 X0) \wedge ((v1_funct_1 \\ & X3) \wedge (v1_partfun1 X3 X0)))) \Rightarrow (r6_pboole X0 (k2_pboole X0 X1 (k3_pboole \\ & X0 X2 X3)) (k3_pboole X0 (k2_pboole X0 X1 X2) (k2_pboole X0 X1 X3)))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1_relat_1 X1) \wedge ((v4_relat_1 X1 X0) \wedge \\ & (v1_funct_1 X1) \wedge (v1_partfun1 X1 X0))) \Rightarrow (\forall X2. ((v1_relat_1 \\ & X2) \wedge ((v4_relat_1 X2 X0) \wedge ((v1_funct_1 X2) \wedge (v1_partfun1 X2 X0)))) \Rightarrow \\ & (r2_pboole X0 X1 (k2_pboole X0 X1 X2))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((v1_relat_1 X1) \wedge ((v4_relat_1 \\ & X1 X0) \wedge ((v1_funct_1 X1) \wedge (v1_partfun1 X1 X0)))) \wedge ((v1_relat_1 \\ & X2) \wedge ((v4_relat_1 X2 X0) \wedge ((v1_funct_1 X2) \wedge (v1_partfun1 X2 X0))))) \Rightarrow \\ & ((r6_pboole X0 X1 X2) \Leftrightarrow (X1 = X2)) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((v1_relat_1 X1) \wedge ((v4_relat_1 \\ & X1 X0) \wedge ((v1_funct_1 X1) \wedge (v1_partfun1 X1 X0)))) \wedge ((v1_relat_1 \\ & X2) \wedge ((v4_relat_1 X2 X0) \wedge ((v1_funct_1 X2) \wedge (v1_partfun1 X2 X0))))) \Rightarrow \\ & ((v1_relat_1 (k3_pboole X0 X1 X2)) \wedge ((v4_relat_1 (k3_pboole X0 \\ & X1 X2) X0) \wedge ((v1_funct_1 (k3_pboole X0 X1 X2)) \wedge (v1_partfun1 (k3_pboole \\ & X0 X1 X2) X0)))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned}
 & \forall X_0 \forall X_1 \forall X_2 (((v1_relat_1 X_1) \wedge ((v4_relat_1 \\
 & X_1 X_0) \wedge ((v1_funct_1 X_1) \wedge (v1_partfun1 X_1 X_0)))) \wedge ((v1_relat_1 \\
 & X_2) \wedge ((v4_relat_1 X_2 X_0) \wedge ((v1_funct_1 X_2) \wedge (v1_partfun1 X_2 X_0)))))) \Rightarrow \\
 & \quad ((v1_relat_1 (k2_pboole X_0 X_1 X_2)) \wedge ((v4_relat_1 (k2_pboole X_0 \\
 & X_1 X_2) X_0) \wedge ((v1_funct_1 (k2_pboole X_0 X_1 X_2)) \wedge (v1_partfun1 (k2_pboole \\
 & X_0 X_1 X_2) X_0)))) \\
 \end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned}
 & \forall X_0 \forall X_1 \forall X_2 (((v1_relat_1 X_1) \wedge ((v4_relat_1 \\
 & X_1 X_0) \wedge ((v1_funct_1 X_1) \wedge (v1_partfun1 X_1 X_0)))) \wedge ((v1_relat_1 \\
 & X_2) \wedge ((v4_relat_1 X_2 X_0) \wedge ((v1_funct_1 X_2) \wedge (v1_partfun1 X_2 X_0)))))) \Rightarrow \\
 & \quad (k2_pboole X_0 X_1 X_2 = k2_pboole X_0 X_2 X_1)
 \end{aligned} \tag{6}$$

Theorem 1

$$\begin{aligned}
 & \forall X_0 \forall X_1 (((v1_relat_1 X_1) \wedge ((v4_relat_1 X_1 X_0) \wedge \\
 & \quad ((v1_funct_1 X_1) \wedge (v1_partfun1 X_1 X_0)))) \Rightarrow (\forall X_2 (((v1_relat_1 \\
 & X_2) \wedge ((v4_relat_1 X_2 X_0) \wedge ((v1_funct_1 X_2) \wedge (v1_partfun1 X_2 X_0)))) \Rightarrow \\
 & \quad (\forall X_3 (((v1_relat_1 X_3) \wedge ((v4_relat_1 X_3 X_0) \wedge ((v1_funct_1 \\
 & X_3) \wedge (v1_partfun1 X_3 X_0)))) \Rightarrow ((r6_pboole X_0 (k3_pboole X_0 (k2_pboole \\
 & X_0 X_1 X_2) (k2_pboole X_0 X_1 X_3)) X_1) \Rightarrow (r2_pboole X_0 (k3_pboole X_0 X_2 \\
 & X_3) X_1)))
 \end{aligned}$$