

t35_polyred (TMNhB- WiLnF5dnrQfWsAwVXHWNhr2ZCkbx4T)

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Let $v3_ordinal1 : \iota \Rightarrow o$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k15_pre_poly : \iota \Rightarrow \iota$ be given. Let $v1_relat_2 : \iota \Rightarrow o$ be given. Let $v4_relat_2 : \iota \Rightarrow o$ be given. Let $v6_relat_2 : \iota \Rightarrow o$ be given. Let $v8_relat_2 : \iota \Rightarrow o$ be given. Let $v2_bagorder : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v7_struct_0 : \iota \Rightarrow o$ be given. Let $v13_algstr_0 : \iota \Rightarrow o$ be given. Let $v3_rlvect_1 : \iota \Rightarrow o$ be given. Let $v4_rlvect_1 : \iota \Rightarrow o$ be given. Let $l2_algstr_0 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $v1_polynom7 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r2_polyred : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k6_termord : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_polyred : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k5_termord : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $l2_struct_0 : \iota \Rightarrow o$ be given. Let $l1_struct_0 : \iota \Rightarrow o$ be given. Let $l1_algstr_0 : \iota \Rightarrow o$ be given. Let $v3_polynom7 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned}
& \forall X0.(v3_ordinal1 X0) \Rightarrow (\forall X1.((v1_partfun1 X1 (k15_pre_poly \\
& \quad X0)) \wedge ((v1_relat_2 X1) \wedge ((v4_relat_2 X1) \wedge ((v6_relat_2 X1) \wedge ((\\
& \quad v8_relat_2 X1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (k2_zfmisc_1 (k15_pre_poly \\
& \quad X0) (k15_pre_poly X0)))))))))) \Rightarrow (\forall X2.((\neg v7_struct_0 X2) \wedge \\
& \quad ((v13_algstr_0 X2) \wedge (v3_rlvect_1 X2) \wedge ((v4_rlvect_1 X2) \wedge (l2_algstr_0 \\
& \quad X2)))))) \Rightarrow (\forall X3.((v1_funct_1 X3) \wedge ((v1_funct_2 X3 (k15_pre_poly \\
& \quad X0) (u1_struct_0 X2)) \wedge ((v1_polynom1 X3 (k15_pre_poly X0) X2) \wedge \\
& \quad (m1_subset_1 X3 (k1_zfmisc_1 (k2_zfmisc_1 (k15_pre_poly X0) (\\
& \quad u1_struct_0 X2))))))) \Rightarrow (r1_polyred X0 X1 X2 (k5_termord X0 X1 X2 \\
& \quad X3) X3)))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v3_ordinal1\ X0) \Rightarrow (\forall X1.((v1_partfun1\ X1\ (k15_pre_poly\ X0)) \wedge ((v1_relat_2\ X1) \wedge ((v4_relat_2\ X1) \wedge ((v6_relat_2\ X1) \wedge ((v8_relat_2\ X1) \wedge ((v2_bagorder\ X1\ X0) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (k15_pre_poly\ X0)))))))))) \Rightarrow (\\
& \quad \forall X2.((\neg v7_struct_0\ X2) \wedge ((v13_algstr_0\ X2) \wedge ((v3_rlvect_1\ X2) \wedge ((v4_rlvect_1\ X2) \wedge (l2_algstr_0\ X2)))))) \Rightarrow (\forall X3.((v1_funct_1\ X3) \wedge ((v1_funct_2\ X3\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom7\ X3\ X0\ X2) \wedge ((v1_polynom1\ X3\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X3\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))))))) \Rightarrow \\
& (r2_polyred\ X0\ X1\ X2\ (k6_termord\ X0\ X1\ X2\ X3)\ (k5_termord\ X0\ X1\ X2\ X3))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v3_ordinal1\ X0) \Rightarrow (\forall X1.((v1_partfun1\ X1\ (k15_pre_poly\ X0)) \wedge ((v1_relat_2\ X1) \wedge ((v4_relat_2\ X1) \wedge ((v6_relat_2\ X1) \wedge ((v8_relat_2\ X1) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (k15_pre_poly\ X0)))))))))) \Rightarrow (\forall X2.((\neg v2_struct_0\ X2) \wedge (l2_algstr_0\ X2)) \Rightarrow (\forall X3.((v1_funct_1\ X3) \wedge ((v1_funct_2\ X3\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X3\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X3\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))))))) \Rightarrow (\forall X4.((v1_funct_1\ X4) \wedge ((v1_funct_2\ X4\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X4\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X4\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))))))) \Rightarrow ((r1_polyred\ X0\ X1\ X2\ X3\ X4) \Leftrightarrow (\neg r2_polyred\ X0\ X1\ X2\ X4\ X3))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v3_ordinal1\ X0) \Rightarrow (\forall X1.((v1_partfun1\ X1\ (k15_pre_poly\ X0)) \wedge ((v1_relat_2\ X1) \wedge ((v4_relat_2\ X1) \wedge ((v6_relat_2\ X1) \wedge ((v8_relat_2\ X1) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (k15_pre_poly\ X0)))))))))) \Rightarrow (\forall X2.((\neg v2_struct_0\ X2) \wedge (l2_algstr_0\ X2)) \Rightarrow (\forall X3.((v1_funct_1\ X3) \wedge ((v1_funct_2\ X3\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X3\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X3\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))))))) \Rightarrow (\forall X4.((v1_funct_1\ X4) \wedge ((v1_funct_2\ X4\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X4\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X4\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))))))) \Rightarrow (\forall X5.((v1_funct_1\ X5) \wedge ((v1_funct_2\ X5\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)) \wedge ((v1_polynom1\ X5\ (k15_pre_poly\ X0)\ X2) \wedge (m1_subset_1\ X5\ (k1_zfmisc_1\ (k2_zfmisc_1\ (k15_pre_poly\ X0)\ (u1_struct_0\ X2)))))))))) \Rightarrow (((r1_polyred\ X0\ X1\ X2\ X3\ X4) \wedge (r1_polyred\ X0\ X1\ X2\ X4\ X5)) \Rightarrow (r1_polyred\ X0\ X1\ X2\ X3\ X5))))))
\end{aligned} \tag{4}$$

Assume the following.

$$\forall X0.(l2_struct_0 X0) \Rightarrow (l1_struct_0 X0) \quad (5)$$

Assume the following.

$$\forall X0.(l2_algstr_0 X0) \Rightarrow ((l2_struct_0 X0) \wedge (l1_algstr_0 X0)) \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((v3_ordinal1 X0) \wedge \\ & (((v1_partfun1 X1 (k15_pre_poly X0)) \wedge (v1_relat_2 X1) \wedge (v4_relat_2 \\ & X1) \wedge (v6_relat_2 X1) \wedge (v8_relat_2 X1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 \\ & (k2_zfmisc_1 (k15_pre_poly X0) (k15_pre_poly X0)))))) \wedge ((\\ & (\neg v2_struct_0 X2) \wedge (v13_algstr_0 X2) \wedge (v3_rlvect_1 X2) \wedge (v4_rlvect_1 \\ & X2) \wedge (l2_algstr_0 X2)))) \wedge ((v1_funct_1 X3) \wedge ((v1_funct_2 X3 (\\ & k15_pre_poly X0) (u1_struct_0 X2)) \wedge (v1_polynom1 X3 (k15_pre_poly \\ & X0) X2) \wedge (m1_subset_1 X3 (k1_zfmisc_1 (k2_zfmisc_1 (k15_pre_poly \\ & X0) (u1_struct_0 X2)))))) \Rightarrow ((v1_funct_1 (k6_termord X0 X1 \\ & X2 X3)) \wedge (v1_funct_2 (k6_termord X0 X1 X2 X3) (k15_pre_poly X0) \\ & (u1_struct_0 X2)) \wedge (v1_polynom1 (k6_termord X0 X1 X2 X3) (k15_pre_poly \\ & X0) X2) \wedge (m1_subset_1 (k6_termord X0 X1 X2 X3) (k1_zfmisc_1 (k2_zfmisc_1 \\ & (k15_pre_poly X0) (u1_struct_0 X2)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((v3_ordinal1 X0) \wedge \\ & (((v1_partfun1 X1 (k15_pre_poly X0)) \wedge (v1_relat_2 X1) \wedge (v4_relat_2 \\ & X1) \wedge (v6_relat_2 X1) \wedge (v8_relat_2 X1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 \\ & (k2_zfmisc_1 (k15_pre_poly X0) (k15_pre_poly X0)))))) \wedge ((\\ & (\neg v2_struct_0 X2) \wedge (l2_struct_0 X2) \wedge (v1_funct_1 X3) \wedge ((v1_funct_2 \\ & X3 (k15_pre_poly X0) (u1_struct_0 X2)) \wedge (v1_polynom1 X3 (k15_pre_poly \\ & X0) X2) \wedge (m1_subset_1 X3 (k1_zfmisc_1 (k2_zfmisc_1 (k15_pre_poly \\ & X0) (u1_struct_0 X2)))))) \Rightarrow ((v1_funct_1 (k5_termord X0 X1 \\ & X2 X3)) \wedge (v1_funct_2 (k5_termord X0 X1 X2 X3) (k15_pre_poly X0) \\ & (u1_struct_0 X2)) \wedge (v3_polynom7 (k5_termord X0 X1 X2 X3) X0 X2) \wedge \\ & (m1_subset_1 (k5_termord X0 X1 X2 X3) (k1_zfmisc_1 (k2_zfmisc_1 \\ & (k15_pre_poly X0) (u1_struct_0 X2)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v2_struct_0 X1) \wedge (l2_struct_0 X1)) \Rightarrow \\ & (\forall X2. (m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 (k15_pre_poly \\ & X0) (u1_struct_0 X1)))) \Rightarrow (((v1_funct_1 X2) \wedge (v1_funct_2 X2 (k15_pre_poly \\ & X0) (u1_struct_0 X1)) \wedge (v3_polynom7 X2 X0 X1)) \Rightarrow ((v1_funct_1 X2) \wedge \\ & ((v1_funct_2 X2 (k15_pre_poly X0) (u1_struct_0 X1)) \wedge (v1_polynom1 \\ & X2 (k15_pre_poly X0) X1)))))) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0.(l1_struct_0 X0) \Rightarrow ((v2_struct_0 X0) \Rightarrow (v7_struct_0 X0)) \quad (10)$$

Theorem 1

$$\begin{aligned} & \forall X0.(v3_ordinal1 X0) \Rightarrow (\forall X1.((v1_partfun1 X1 (k15_pre_poly \\ & \quad X0)) \wedge ((v1_relat_2 X1) \wedge ((v4_relat_2 X1) \wedge ((v6_relat_2 X1) \wedge ((\\ & \quad v8_relat_2 X1) \wedge ((v2_bagorder X1 X0) \wedge (m1_subset_1 X1 (k1_zfmisc_1 \\ & \quad (k2_zfmisc_1 (k15_pre_poly X0) (k15_pre_poly X0)))))))))) \Rightarrow (\\ & \quad \forall X2.((\neg v7_struct_0 X2) \wedge ((v13_algstr_0 X2) \wedge ((v3_rlvect_1 \\ & \quad X2) \wedge ((v4_rlvect_1 X2) \wedge (l2_algstr_0 X2)))))) \Rightarrow (\forall X3.((v1_funct_1 \\ & \quad X3) \wedge ((v1_funct_2 X3 (k15_pre_poly X0) (u1_struct_0 X2)) \wedge ((v1_polynom7 \\ & \quad X3 X0 X2) \wedge ((v1_polynom1 X3 (k15_pre_poly X0) X2) \wedge (m1_subset_1 \\ & \quad X3 (k1_zfmisc_1 (k2_zfmisc_1 (k15_pre_poly X0) (u1_struct_0 X2))))))) \Rightarrow \\ & \quad (r2_polyred X0 X1 X2 (k6_termord X0 X1 X2 X3) X3))) \end{aligned}$$