# t36_member_1 <br> (TMauLBL21RBQyhsst9zmjG3x5DuxH4EhgNL) 

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Let $v 1 \_$membered $: ~ \iota \Rightarrow 0$ be given. Let $k 5 \_$member_1 : $\iota \Rightarrow \iota$ be given. Let $k 7 \_m e m b e r \_1: \iota \Rightarrow \iota$ be given. Let $v 1 \_x c m p l x \_0: \iota \Rightarrow o$ be given. Let $k 2_{2} b i n o p \_2$ : $\iota \Rightarrow \iota$ be given. Let $k 5 \_x c m p l x \_0: \iota \Rightarrow \iota$ be given. Let $k 4 \_x c m p l x \_0: \iota \Rightarrow \iota$ be given. Let $k 1 \_b i n o p \_2: ~ \iota \Rightarrow \iota$ be given. Let $m 1 \_$subset_1 : $\iota \Rightarrow \iota \Rightarrow 0$ be given. Let $k 2 \_n u m b e r s: \iota$ be given. Assume the following.

$$
\begin{align*}
& \forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow(( \right. \\
& \left.\left.\left.\quad k 2 \_b i n o p \_2 X 1 \in X 0\right) \Leftrightarrow\left(X 1 \in k 7 \_m e m b e r \_1 X 0\right)\right)\right) \tag{1}
\end{align*}
$$

Assume the following.

$$
\begin{align*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow & \left(k 5 \_x c m p l x \_0\left(k 4 \_x c m p l x \_0 X 0\right)=k 4 \_x c m p l x \_0\right. \\
& \left.\left(k 5 \_x c m p l x \_0 X 0\right)\right) \tag{2}
\end{align*}
$$

Assume the following.

$$
\begin{align*}
& \forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow(( \right. \\
& \left.\left.\left.k 1 \_b i n o p \_2 X 1 \in X 0\right) \Leftrightarrow\left(X 1 \in k 5 \_m e m b e r \_1 X 0\right)\right)\right) \tag{3}
\end{align*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 \quad X 0\right) \Rightarrow\left(k 2 \_b i n o p \_2 X 0=k 5 \_x c m p l x \_0 X 0\right) \tag{4}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(k 1 \_b i n o p \_2 X 0=k 4 \_x c m p l x \_0 X 0\right) \tag{5}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(k 7 \_m e m b e r \_1\left(k 7 \_m e m b e r \_1 X 0\right)=X 0\right) \tag{6}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(k 5 \_m e m b e r \_1\left(k 5 \_m e m b e r \_1 X 0\right)=X 0\right) \tag{7}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(k 2 \_b i n o p \_2\left(k 2 \_b i n o p \_2 X 0\right)=X 0\right) \tag{8}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(k 1 \_b i n o p \_2\left(k 1 \_b i n o p \_2 X 0\right)=X 0\right) \tag{9}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 7 \_m e m b e r \_1 X 0\right)\right) \tag{10}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(v 1 \_x c m p l x \_0\left(k 5 \_x c m p l x \_0 X 0\right)\right) \tag{11}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 5 \_m e m b e r \_1 X 0\right)\right) \tag{12}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(m 1 \_s u b s e t \_1\left(k 2 \_b i n o p \_2 X 0\right) k 2 \_n u m b e r s\right) \tag{13}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(m 1 \_s u b s e t \_1\left(k 1 \_b i n o p \_2 X 0\right) k 2 \_n u m b e r s\right) \tag{14}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_ \text {membered } X 1\right) \Rightarrow(( \right. \\
\left.\left.X 0=X 1) \Leftrightarrow\left(\forall X 2 .\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow((X 2 \in X 0) \Leftrightarrow(X 2 \in X 1))\right)\right)\right) \tag{15}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(m 1 \_s u b s e t \_1 \quad X 0 \text { k2_numbers }\right) \Rightarrow\left(v 1 \_x c m p l x \_0 X 0\right) \tag{16}
\end{equation*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(k 5 \_m e m b e r \_1\left(k 7 \_m e m b e r \_1 X 0\right)=k 7 \_m e m b e r_{-} 1\right.$ (k5_member_1 X0))

