

# t37\_ltlaxio1

(TMRxNL6SuDmGAcxt4cgqedX8fSjRwqNfjkQ)

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Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_hilbert1 : \iota$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $v3\_ltlaxio1 : \iota \Rightarrow o$  be given. Let  $v4\_ltlaxio1 : \iota \Rightarrow o$  be given. Let  $v5\_ltlaxio1 : \iota \Rightarrow o$  be given. Let  $v6\_ltlaxio1 : \iota \Rightarrow o$  be given. Let  $v7\_ltlaxio1 : \iota \Rightarrow o$  be given. Let  $v8\_ltlaxio1 : \iota \Rightarrow o$  be given. Let  $v9\_ltlaxio1 : \iota \Rightarrow o$  be given. Let  $r3\_ltlaxio1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k10\_ltlaxio1 : \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_margrel1 : \iota$  be given. Let  $k11\_ltlaxio1 : \iota \Rightarrow \iota$  be given. Let  $k1\_domain\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_hilbert1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_hilbert1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_ltlaxio1 : \iota \Rightarrow \iota$  be given. Let  $k7\_ltlaxio1 : \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k5\_ltlaxio1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_ltlaxio1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_ltlaxio1 : \iota \Rightarrow \iota$  be given. Let  $k1\_ltlaxio1 : \iota \Rightarrow \iota$  be given. Let  $r2\_ltlaxio1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_ltlaxio1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& \quad X1 k1\_hilbert1) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k5\_numbers) \Rightarrow (\forall X3. \\
& ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)) \wedge \\
& (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k1\_zfmisc\_1 \\
& k10\_ltlaxio1)))))) \Rightarrow (k3\_funct\_2 (k2\_zfmisc\_1 k5\_numbers k1\_hilbert1) \\
& k6\_margrel1 (k11\_ltlaxio1 X3) (k1\_domain\_1 k5\_numbers k1\_hilbert1 \\
& \quad X2 (k3\_hilbert1 (k4\_hilbert1 X0 X1) (k2\_ltlaxio1 (k7\_ltlaxio1 \\
& \quad \quad X1)))) = np\_1))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& X1 k1\_hilbert1) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k5\_numbers) \Rightarrow (\forall X3. \\
& ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)) \wedge \\
& (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k1\_zfmisc\_1 \\
& k10\_ltlaxio1)))))) \Rightarrow (k3\_funct\_2 (k2\_zfmisc\_1 k5\_numbers k1\_hilbert1) \\
& k6\_margrel1 (k11\_ltlaxio1 X3) (k1\_domain\_1 k5\_numbers k1\_hilbert1 \\
& X2 (k3\_hilbert1 (k5\_ltlaxio1 (k2\_ltlaxio1 X0) (k2\_ltlaxio1 (k4\_ltlaxio1 \\
& X1 (k4\_hilbert1 X1 X0)))) (k4\_hilbert1 X1 X0))) = np\_1)))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& X1 k1\_hilbert1) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k5\_numbers) \Rightarrow (\forall X3. \\
& ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)) \wedge \\
& (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k1\_zfmisc\_1 \\
& k10\_ltlaxio1)))))) \Rightarrow (k3\_funct\_2 (k2\_zfmisc\_1 k5\_numbers k1\_hilbert1) \\
& k6\_margrel1 (k11\_ltlaxio1 X3) (k1\_domain\_1 k5\_numbers k1\_hilbert1 \\
& X2 (k3\_hilbert1 (k4\_hilbert1 X0 X1) (k5\_ltlaxio1 (k2\_ltlaxio1 \\
& X1) (k2\_ltlaxio1 (k4\_ltlaxio1 X0 (k4\_hilbert1 X0 X1)))))) = np\_1)))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& X1 k5\_numbers) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 \\
& k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)))))) \Rightarrow (k3\_funct\_2 \\
& (k2\_zfmisc\_1 k5\_numbers k1\_hilbert1) k6\_margrel1 (k11\_ltlaxio1 \\
& X2) (k1\_domain\_1 k5\_numbers k1\_hilbert1 X1 (k3\_hilbert1 (k6\_ltlaxio1 \\
& X0) (k4\_ltlaxio1 X0 (k2\_ltlaxio1 (k6\_ltlaxio1 X0)))))) = np\_1)))
\end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& X1 k1\_hilbert1) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k5\_numbers) \Rightarrow (\forall X3. \\
& ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)) \wedge \\
& (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k1\_zfmisc\_1 \\
& k10\_ltlaxio1)))))) \Rightarrow (k3\_funct\_2 (k2\_zfmisc\_1 k5\_numbers k1\_hilbert1) \\
& k6\_margrel1 (k11\_ltlaxio1 X3) (k1\_domain\_1 k5\_numbers k1\_hilbert1 \\
& X2 (k3\_hilbert1 (k2\_ltlaxio1 (k3\_hilbert1 X0 X1)) (k3\_hilbert1 \\
& (k2\_ltlaxio1 X0) (k2\_ltlaxio1 X1)))) = np\_1)))
\end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\ X1 k5\_numbers) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 \\ k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ (k2\_zfmisc\_1 k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)))))) \Rightarrow (k3\_funct\_2 \\ (k2\_zfmisc\_1 k5\_numbers k1\_hilbert1) k6\_margrel1 (k11\_ltlaxio1 \\ X2) (k1\_domain\_1 k5\_numbers k1\_hilbert1 X1 (k3\_hilbert1 (k2\_ltlaxio1 \\ (k1\_ltlaxio1 X0)) (k1\_ltlaxio1 (k2\_ltlaxio1 X0)))) = np\_1))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\ X1 k5\_numbers) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 \\ k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ (k2\_zfmisc\_1 k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)))))) \Rightarrow (k3\_funct\_2 \\ (k2\_zfmisc\_1 k5\_numbers k1\_hilbert1) k6\_margrel1 (k11\_ltlaxio1 \\ X2) (k1\_domain\_1 k5\_numbers k1\_hilbert1 X1 (k3\_hilbert1 (k1\_ltlaxio1 \\ (k2\_ltlaxio1 X0)) (k2\_ltlaxio1 (k1\_ltlaxio1 X0)))) = np\_1))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow ((v9\_ltlaxio1 X0) \Leftrightarrow ( \\ \exists X1.(m1\_subset\_1 X1 k1\_hilbert1) \wedge (\exists X2.(m1\_subset\_1 \\ X2 k1\_hilbert1) \wedge (X0 = k3\_hilbert1 (k4\_hilbert1 X1 X2) (k2\_ltlaxio1 \\ (k7\_ltlaxio1 X2)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow ((v8\_ltlaxio1 X0) \Leftrightarrow ( \\ \exists X1.(m1\_subset\_1 X1 k1\_hilbert1) \wedge (\exists X2.(m1\_subset\_1 \\ X2 k1\_hilbert1) \wedge (X0 = k3\_hilbert1 (k5\_ltlaxio1 (k2\_ltlaxio1 X2) \\ (k2\_ltlaxio1 (k4\_ltlaxio1 X1 (k4\_hilbert1 X1 X2)))) (k4\_hilbert1 \\ X1 X2)))))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow ((v7\_ltlaxio1 X0) \Leftrightarrow ( \\ \exists X1.(m1\_subset\_1 X1 k1\_hilbert1) \wedge (\exists X2.(m1\_subset\_1 \\ X2 k1\_hilbert1) \wedge (X0 = k3\_hilbert1 (k4\_hilbert1 X1 X2) (k5\_ltlaxio1 \\ (k2\_ltlaxio1 X2) (k2\_ltlaxio1 (k4\_ltlaxio1 X1 (k4\_hilbert1 X1 \\ X2))))))))) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow ((v6\_ltlaxio1 X0) \Leftrightarrow ( \\ \exists X1.(m1\_subset\_1 X1 k1\_hilbert1) \wedge (X0 = k3\_hilbert1 (k6\_ltlaxio1 \\ X1) (k4\_ltlaxio1 X1 (k2\_ltlaxio1 (k6\_ltlaxio1 X1)))))) \end{aligned} \quad (11)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow ((v5\_ltlaxio1 X0) \Leftrightarrow ( \\ \exists X1.(m1\_subset\_1 X1 k1\_hilbert1) \wedge (\exists X2.(m1\_subset\_1 \\ X2 k1\_hilbert1) \wedge (X0 = k3\_hilbert1 (k2\_ltlaxio1 (k3\_hilbert1 X1 \\ X2)) (k3\_hilbert1 (k2\_ltlaxio1 X1) (k2\_ltlaxio1 X2)))))) \end{aligned} \quad (12)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow ((v4\_ltlaxio1 X0) \Leftrightarrow ( \\ \exists X1.(m1\_subset\_1 X1 k1\_hilbert1) \wedge (X0 = k3\_hilbert1 (k2\_ltlaxio1 \\ (k1\_ltlaxio1 X1)) (k1\_ltlaxio1 (k2\_ltlaxio1 X1)))))) \end{aligned} \quad (13)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow ((v3\_ltlaxio1 X0) \Leftrightarrow ( \\ \exists X1.(m1\_subset\_1 X1 k1\_hilbert1) \wedge (X0 = k3\_hilbert1 (k1\_ltlaxio1 \\ (k2\_ltlaxio1 X1)) (k2\_ltlaxio1 (k1\_ltlaxio1 X1)))))) \end{aligned} \quad (14)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 (k1\_zfmisc\_1 k1\_hilbert1)) \Rightarrow (\forall X1. \\ (m1\_subset\_1 X1 k1\_hilbert1) \Rightarrow ((r3\_ltlaxio1 X0 X1) \Leftrightarrow (\forall X2. \\ ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 k5\_numbers (k1\_zfmisc\_1 k10\_ltlaxio1)) \wedge \\ (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k1\_zfmisc\_1 \\ k10\_ltlaxio1)))))) \Rightarrow ((r2\_ltlaxio1 X2 X0) \Rightarrow (r1\_ltlaxio1 X2 X1)))))) \end{aligned} \quad (15)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers (k1\_zfmisc\_1 \\ k10\_ltlaxio1)) \wedge (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers \\ (k1\_zfmisc\_1 k10\_ltlaxio1)))))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 \\ k1\_hilbert1) \Rightarrow ((r1\_ltlaxio1 X0 X1) \Leftrightarrow (\forall X2.(m1\_subset\_1 \\ X2 k5\_numbers) \Rightarrow (k3\_funct\_2 (k2\_zfmisc\_1 k5\_numbers k1\_hilbert1) \\ k6\_margrel1 (k11\_ltlaxio1 X0) (k1\_domain\_1 k5\_numbers k1\_hilbert1 \\ X2 X1) = np\_1)))))) \end{aligned} \quad (16)$$

**Theorem 1**

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\ X1 (k1\_zfmisc\_1 k1\_hilbert1)) \Rightarrow (((\neg(\neg v3\_ltlaxio1 X0) \wedge ((\neg v4\_ltlaxio1 \\ X0) \wedge ((\neg v5\_ltlaxio1 X0) \wedge ((\neg v6\_ltlaxio1 X0) \wedge ((\neg v7\_ltlaxio1 X0) \wedge \\ ((\neg v8\_ltlaxio1 X0) \wedge (\neg v9\_ltlaxio1 X0)))))) \Rightarrow (r3\_ltlaxio1 X1 \\ X0)))) \end{aligned}$$