

## t38\_fuzzy\_2

(TMXh9h76gjh5vKGfeBZQbWhNwM638cFcGQ2)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_rcomp\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_numbers : \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_fuzzy\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_fuzzy\_1 : \iota \Rightarrow \iota$  be given. Let  $k5\_fuzzy\_1 : \iota \Rightarrow \iota$  be given. Let  $k3\_fuzzy\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_fuzzy\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow & ((r2\_funct\_2 X0 k1\_numbers (k3\_fuzzy\_1 \\ X0 (k4\_fuzzy\_1 X0)) (k5\_fuzzy\_1 X0)) \wedge & (r2\_funct\_2 X0 k1\_numbers \\ (k3\_fuzzy\_1 X0 (k5\_fuzzy\_1 X0)) (k4\_fuzzy\_1 X0))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow & (\forall X1. ((v5\_relat\_1 X1 (k1\_rcomp\_1 \\ k6\_numbers np\_1)) \wedge & ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 X0 k1\_numbers) \wedge \\ (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers)))))) \Rightarrow & \\ ((r2\_funct\_2 X0 k1\_numbers (k2\_fuzzy\_2 X0 X1 (k4\_fuzzy\_1 X0)) ( & \\ k4\_fuzzy\_1 X0)) \wedge (r2\_funct\_2 X0 k1\_numbers (k2\_fuzzy\_2 X0 X1 (k5\_fuzzy\_1 & \\ X0)) X1))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow & (\forall X1. ((v5\_relat\_1 X1 (k1\_rcomp\_1 \\ k6\_numbers np\_1)) \wedge & ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 X0 k1\_numbers) \wedge \\ (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers)))))) \Rightarrow & \\ (\forall X2. ((v5\_relat\_1 X2 (k1\_rcomp\_1 k6\_numbers np\_1)) \wedge & \\ (v1\_funct\_1 X2) \wedge & ((v1\_funct\_2 X2 X0 k1\_numbers) \wedge (m1\_subset\_1 \\ X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers)))))) \Rightarrow & (r2\_funct\_2 \\ X0 k1\_numbers (k3\_fuzzy\_2 X0 X1 X2) (k3\_fuzzy\_1 X0 (k2\_fuzzy\_2 X0 & \\ (k3\_fuzzy\_1 X0 X1) (k3\_fuzzy\_1 X0 X2)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((v1\_funct\_1 X2)\wedge \\ & ((v1\_funct\_2 X2 X0 X1)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X1)))))\wedge((v1\_funct\_1 X3)\wedge((v1\_funct\_2 X3 X0 X1)\wedge(m1\_subset\_1 \\ & X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1))))))\Rightarrow((r2\_funct\_2 X0 X1 X2 \\ & X3)\Leftrightarrow(X2 = X3)) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge((v5\_relat\_1 X1 (k1\_rcomp\_1 \\ & k6\_numbers np\_1))\wedge((v1\_funct\_1 X1)\wedge((v1\_funct\_2 X1 X0 k1\_numbers)\wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers))))))\Rightarrow \\ & (k3\_fuzzy\_1 X0 (k3\_fuzzy\_1 X0 X1) = X1) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow((v5\_relat\_1 (k5\_fuzzy\_1 X0) (k1\_rcomp\_1 \\ & k6\_numbers np\_1))\wedge((v1\_funct\_1 (k5\_fuzzy\_1 X0))\wedge((v1\_funct\_2 \\ & (k5\_fuzzy\_1 X0) X0 k1\_numbers)\wedge(m1\_subset\_1 (k5\_fuzzy\_1 X0) ( \\ & k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow((v5\_relat\_1 (k4\_fuzzy\_1 X0) (k1\_rcomp\_1 \\ & k6\_numbers np\_1))\wedge((v1\_funct\_1 (k4\_fuzzy\_1 X0))\wedge((v1\_funct\_2 \\ & (k4\_fuzzy\_1 X0) X0 k1\_numbers)\wedge(m1\_subset\_1 (k4\_fuzzy\_1 X0) ( \\ & k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.((\neg v1\_xboole\_0 X0)\wedge(((v5\_relat\_1 \\ & X1 (k1\_rcomp\_1 k6\_numbers np\_1))\wedge((v1\_funct\_1 X1)\wedge((v1\_funct\_2 \\ & X1 X0 k1\_numbers)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 \\ & k1\_numbers))))))\wedge((v5\_relat\_1 X2 (k1\_rcomp\_1 k6\_numbers np\_1))\wedge \\ & ((v1\_funct\_1 X2)\wedge((v1\_funct\_2 X2 X0 k1\_numbers)\wedge(m1\_subset\_1 \\ & X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers))))))\Rightarrow((v5\_relat\_1 \\ & (k3\_fuzzy\_2 X0 X1 X2) (k1\_rcomp\_1 k6\_numbers np\_1))\wedge((v1\_funct\_1 \\ & (k3\_fuzzy\_2 X0 X1 X2))\wedge((v1\_funct\_2 (k3\_fuzzy\_2 X0 X1 X2) X0 k1\_numbers)\wedge \\ & (m1\_subset\_1 (k3\_fuzzy\_2 X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 \\ & k1\_numbers)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. ((\neg v1\_xboole\_0 X0) \wedge ((v5\_relat\_1 X1 (k1\_rcomp\_1 \\
& k6\_numbers np\_1)) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 X0 k1\_numbers) \wedge \\
& (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers)))))) \Rightarrow \\
& ((v5\_relat\_1 (k3\_fuzzy\_1 X0 X1) (k1\_rcomp\_1 k6\_numbers np\_1)) \wedge \\
& ((v1\_funct\_1 (k3\_fuzzy\_1 X0 X1)) \wedge ((v1\_funct\_2 (k3\_fuzzy\_1 X0 \\
& X1) X0 k1\_numbers) \wedge (m1\_subset\_1 (k3\_fuzzy\_1 X0 X1) (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 X0 k1\_numbers))))))
\end{aligned} \tag{9}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. ((\neg v1\_xboole\_0 X0) \wedge (((v5\_relat\_1 \\
& X1 (k1\_rcomp\_1 k6\_numbers np\_1)) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 \\
& X1 X0 k1\_numbers) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 \\
& k1\_numbers)))))) \wedge ((v5\_relat\_1 X2 (k1\_rcomp\_1 k6\_numbers np\_1)) \wedge \\
& ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 k1\_numbers) \wedge (m1\_subset\_1 \\
& X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers)))))) \Rightarrow ((v5\_relat\_1 \\
& (k2\_fuzzy\_2 X0 X1 X2) (k1\_rcomp\_1 k6\_numbers np\_1)) \wedge ((v1\_funct\_1 \\
& (k2\_fuzzy\_2 X0 X1 X2)) \wedge ((v1\_funct\_2 (k2\_fuzzy\_2 X0 X1 X2) X0 k1\_numbers) \wedge \\
& (m1\_subset\_1 (k2\_fuzzy\_2 X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 \\
& k1\_numbers))))))
\end{aligned} \tag{10}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. ((v5\_relat\_1 X1 (k1\_rcomp\_1 \\
& k6\_numbers np\_1)) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 X0 k1\_numbers) \wedge \\
& (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers)))))) \Rightarrow \\
& ((r2\_funct\_2 X0 k1\_numbers (k3\_fuzzy\_2 X0 X1 (k4\_fuzzy\_1 X0)) X1) \wedge \\
& (r2\_funct\_2 X0 k1\_numbers (k3\_fuzzy\_2 X0 X1 (k5\_fuzzy\_1 X0)) (k5\_fuzzy\_1 \\
& X0)))
\end{aligned}$$