

## t38\_pdiff\_5

(TMX55Z EZ8rrxpaFcU9UTQWXNcYCuhPkWTiV)

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Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_euclid : \iota \Rightarrow \iota$  be given. Let  $np\_3 : \iota$  be given. Let  $k1\_numbers : \iota$  be given. Let  $m2\_finseq\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_rcomp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_seq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_pdiff\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_2 : \iota$  be given. Let  $r2\_pdiff\_5 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_pdiff\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_pdiff\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $v2\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_fdiff\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_numbers : \iota$  be given. Let  $v3\_funct\_1 : \iota \Rightarrow o$  be given. Let  $k2\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $k3\_valued\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_comseq\_2 : \iota \Rightarrow o$  be given. Let  $k20\_valued\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k37\_valued\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k47\_valued\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_pdiff\_5 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_seq\_2 : \iota \Rightarrow \iota$  be given. Let  $k11\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_fdiff\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r3\_pdiff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_rvsum\_1 : \iota \Rightarrow \iota$  be given. Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $k1\_fdiff\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m1\_finseq\_2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $v6\_membered : \iota \Rightarrow o$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v3\_fdiff\_1 : \iota \Rightarrow o$  be given. Let  $v2\_fdiff\_1 : \iota \Rightarrow o$  be given. Let  $k9\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((v1\_funct\_1 X0) \wedge (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
 & \quad (k1\_euclid np\_3) k1\_numbers)))) \Rightarrow (\forall X1.(m2\_finseq\_2 X1 \\
 & \quad k1\_numbers (k1\_euclid np\_3)) \Rightarrow ((\exists X2.(m1\_subset\_1 X2 k1\_numbers) \wedge \\
 & \quad (\exists X3.(m1\_subset\_1 X3 k1\_numbers) \wedge (\exists X4.(m1\_subset\_1 \\
 & \quad X4 k1\_numbers) \wedge ((X1 = k11\_finseq\_1 X2 X3 X4) \wedge (r1\_fdiff\_1 (k1\_pdiff\_2 \\
 & \quad np\_3 np\_2 X0 X1) X3)))))) \Leftrightarrow (r3\_pdiff\_1 np\_3 np\_2 X0 X1))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k1\_numbers) \Rightarrow (\forall X1.((v2\_relat\_1 \\
& X1) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 k5\_numbers k1\_numbers) \wedge \\
& ((v1\_fdiff\_1 X1 k6\_numbers) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& k5\_numbers k1\_numbers)))))) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge \\
& ((v3\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 k5\_numbers k1\_numbers) \wedge (m1\_subset\_1 \\
& X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow (( \\
& k2\_relset\_1 k1\_numbers X2 = k1\_tarski X0) \Rightarrow ((v2\_comseq\_2 X2) \wedge ( \\
& (k2\_seq\_2 X2 = X0) \wedge ((v2\_comseq\_2 (k3\_valued\_1 k5\_numbers k1\_numbers \\
& k1\_numbers X1 X2)) \wedge (k2\_seq\_2 (k3\_valued\_1 k5\_numbers k1\_numbers \\
& k1\_numbers X1 X2) = X0))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& (k1\_relset\_1 (k1\_euclid np\_3) (k1\_pdiff\_1 np\_2 np\_3) = k1\_euclid \\
& np\_3) \wedge ((k1\_rsum\_1 (k1\_pdiff\_1 np\_2 np\_3) = k1\_numbers) \wedge ( \\
& \forall X0.(m1\_subset\_1 X0 k1\_numbers) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& X1 k1\_numbers) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k1\_numbers) \Rightarrow (k1\_seq\_1 \\
& (k1\_pdiff\_1 np\_2 np\_3) (k11\_finseq\_1 X0 X1 X2) = X1))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(m2\_finseq\_2 X0 k1\_numbers (k1\_euclid np\_3)) \Rightarrow (\forall X1. \\
& ((v1\_funct\_1 X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 ( \\
& k1\_euclid np\_3) k1\_numbers)))) \Rightarrow ((r2\_pdiff\_5 X1 X0) \Leftrightarrow (r3\_pdiff\_1 \\
& np\_3 np\_2 (k1\_pdiff\_3 np\_1 np\_3 X1) X0)))
\end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_funct\_1 X0) \wedge (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& \quad k1\_numbers k1\_numbers)))) \Rightarrow (\forall X1.(v1\_xreal\_0 X1) \Rightarrow (\forall X2. \\
& \quad (m1\_rcomp\_1 X2 X1) \Rightarrow (((r1\_fdiff\_1 X0 X1) \wedge (r1\_tarski X2 (k1\_relset\_1 \\
& \quad k1\_numbers X0))) \Rightarrow (\forall X3.((v2\_relat\_1 X3) \wedge ((v1\_funct\_1 \\
& X3) \wedge ((v1\_funct\_2 X3 k5\_numbers k1\_numbers) \wedge ((v1\_fdiff\_1 X3 k6\_numbers) \wedge \\
& (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\
& \quad (\forall X4.((v1\_funct\_1 X4) \wedge ((v3\_funct\_1 X4) \wedge ((v1\_funct\_2 \\
& X4 k5\_numbers k1\_numbers) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& k5\_numbers k1\_numbers)))))) \Rightarrow (((k2\_relset\_1 k1\_numbers X4 = k1\_tarski \\
& X1) \wedge (r1\_tarski (k2\_relset\_1 k1\_numbers (k3\_valued\_1 k5\_numbers \\
& k1\_numbers k1\_numbers X3 X4)) X2) \Rightarrow ((v2\_comseq\_2 (k20\_valued\_1 \\
& k5\_numbers k1\_numbers k1\_numbers (k37\_valued\_1 k5\_numbers k1\_numbers \\
& X3) (k47\_valued\_1 k5\_numbers k1\_numbers k1\_numbers (k8\_funct\_2 \\
& k5\_numbers k1\_numbers k1\_numbers (k3\_valued\_1 k5\_numbers k1\_numbers \\
& k1\_numbers X3 X4) X0) (k8\_funct\_2 k5\_numbers k1\_numbers k1\_numbers \\
& X4 X0))) \wedge (k1\_fdiff\_1 X0 X1 = k2\_seq\_2 (k20\_valued\_1 k5\_numbers \\
& k1\_numbers k1\_numbers (k37\_valued\_1 k5\_numbers k1\_numbers X3) \\
& (k47\_valued\_1 k5\_numbers k1\_numbers k1\_numbers (k8\_funct\_2 k5\_numbers \\
& k1\_numbers k1\_numbers (k3\_valued\_1 k5\_numbers k1\_numbers k1\_numbers \\
& X3 X4) X0) (k8\_funct\_2 k5\_numbers k1\_numbers k1\_numbers X4 X0))))))))) \Rightarrow \\
& \hspace{15em} (5)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k1\_numbers) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& X1 k1\_numbers) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k1\_numbers) \Rightarrow (\forall X3. \\
& \quad (m2\_finseq\_2 X3 k1\_numbers (k1\_euclid np\_3)) \Rightarrow (\forall X4.(( \\
& v1\_funct\_1 X4) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid \\
& np\_3) k1\_numbers)))) \Rightarrow (((X3 = k11\_finseq\_1 X0 X1 X2) \wedge (r2\_pdfiff\_5 \\
& X4 X3)) \Rightarrow (k2\_pdfiff\_5 X4 X3 = k1\_fdiff\_1 (k1\_pdfiff\_2 np\_3 np\_2 ( \\
& \quad k1\_pdfiff\_3 np\_1 np\_3 X4) X3) X1)))))) \Rightarrow \\
& \hspace{15em} (6)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& ((v2\_xxreal\_0 np\_3) \wedge (m2\_subset\_1 np\_3 k1\_numbers k5\_numbers)) \wedge \\
& ((m1\_subset\_1 np\_3 k5\_numbers) \wedge (m1\_subset\_1 np\_3 k1\_numbers)) \Rightarrow \\
& \hspace{15em} (7)
\end{aligned}$$

Assume the following.

$$\neg v1\_xboole\_0 np\_3 \hspace{15em} (8)$$

Assume the following.

$$\begin{aligned}
& ((v2\_xxreal\_0 np\_2) \wedge (m2\_subset\_1 np\_2 k1\_numbers k5\_numbers)) \wedge \\
& ((m1\_subset\_1 np\_2 k5\_numbers) \wedge (m1\_subset\_1 np\_2 k1\_numbers)) \Rightarrow \\
& \hspace{15em} (9)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& ((v2\_xxreal\_0 np\_1) \wedge (m2\_subset\_1 np\_1 k1\_numbers k5\_numbers)) \wedge \\
& ((m1\_subset\_1 np\_1 k5\_numbers) \wedge (m1\_subset\_1 np\_1 k1\_numbers)) \Rightarrow \\
& \hspace{15em} (10)
\end{aligned}$$

Assume the following.

$$\forall X0.\forall X1.(m1\_finseq\_2 X1 X0)\Rightarrow(\forall X2.(m2\_finseq\_2 X2 X0 X1)\Leftrightarrow(m1\_subset\_1 X2 X1)) \quad (11)$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (12)$$

Assume the following.

$$v6\_membered k4\_ordinal1 \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.((m1\_subset\_1 X0 k5\_numbers)\wedge \\ & (((\neg v1\_xboole\_0 X1)\wedge(m1\_subset\_1 X1 k5\_numbers)\wedge((v1\_funct\_1 \\ & X2)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X1) \\ & k1\_numbers))))))\Rightarrow((v1\_funct\_1 (k1\_pdiff\_3 X0 X1 X2))\wedge((v1\_funct\_2 \\ & (k1\_pdiff\_3 X0 X1 X2) (k1\_euclid X1) k1\_numbers)\wedge(m1\_subset\_1 \\ & (k1\_pdiff\_3 X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X1) \\ & k1\_numbers)))))) \end{aligned} \quad (14)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((m1\_subset\_1 X0 \\ & k5\_numbers)\wedge((m1\_subset\_1 X1 k5\_numbers)\wedge(((v1\_funct\_1 X2)\wedge \\ & (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X0) k1\_numbers))))\wedge \\ & (m1\_subset\_1 X3 (k1\_euclid X0))))\Rightarrow((v1\_funct\_1 (k1\_pdiff\_2 \\ & X0 X1 X2 X3))\wedge(m1\_subset\_1 (k1\_pdiff\_2 X0 X1 X2 X3) (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 k1\_numbers k1\_numbers)))) \end{aligned} \quad (15)$$

Assume the following.

$$\forall X0.(v7\_ordinal1 X0)\Rightarrow(m1\_finseq\_2 (k1\_euclid X0) k1\_numbers) \quad (16)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_funct\_1 X0) \wedge (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& \quad (k1\_euclid\ np\_3) k1\_numbers)))) \Rightarrow (\forall X1.(m2\_finseq\_2 X1 \\
& \quad k1\_numbers (k1\_euclid\ np\_3)) \Rightarrow ((r2\_pdiff\_5 X0 X1) \Leftrightarrow (\exists X2. \\
& (m1\_subset\_1 X2 k1\_numbers) \wedge (\exists X3.(m1\_subset\_1 X3 k1\_numbers) \wedge \\
& \quad (\exists X4.(m1\_subset\_1 X4 k1\_numbers) \wedge ((X1 = k11\_finseq\_1 X2 \\
& \quad X3 X4) \wedge (\exists X5.(m1\_rcomp\_1 X5 X3) \wedge (r1\_tarski X5 (k1\_relset\_1 \\
& \quad k1\_numbers (k1\_pdiff\_2\ np\_3\ np\_2) (k1\_pdiff\_3\ np\_1\ np\_3 X0) \\
& \quad X1)))) \wedge (\exists X6.((v1\_funct\_1 X6) \wedge ((v3\_fdiff\_1 X6) \wedge (m1\_subset\_1 \\
& \quad X6 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k1\_numbers k1\_numbers)))))) \wedge (\exists X7. \\
& ((v1\_funct\_1 X7) \wedge ((v2\_fdiff\_1 X7) \wedge (m1\_subset\_1 X7 (k1\_zfmisc\_1 \\
& \quad (k2\_zfmisc\_1 k1\_numbers k1\_numbers)))))) \wedge (\forall X8.(m1\_subset\_1 \\
& \quad X8 k1\_numbers) \Rightarrow ((X8 \in X5) \Rightarrow (k9\_real\_1 (k1\_seq\_1 (k1\_pdiff\_2\ np\_3 \\
& \quad np\_2) (k1\_pdiff\_3\ np\_1\ np\_3 X0) X1) X8) (k1\_seq\_1 (k1\_pdiff\_2 \\
& \quad np\_3\ np\_2) (k1\_pdiff\_3\ np\_1\ np\_3 X0) X1) X3) = k7\_real\_1 (k1\_seq\_1 \\
& \quad X6 (k9\_real\_1 X8 X3)) (k1\_seq\_1 X7 (k9\_real\_1 X8 X3))))))))))))) \\
& \hspace{20em} (17)
\end{aligned}$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k1\_numbers) \Rightarrow (v1\_xreal\_0 X0) \hspace{10em} (18)$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v6\_membered X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 X0) \Rightarrow \\
& \quad (v7\_ordinal1 X1)) \hspace{10em} (19)
\end{aligned}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((v1\_funct\_1 X0) \wedge (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& \quad (k1\_euclid\ np\_3) k1\_numbers)))) \Rightarrow (\forall X1.(m2\_finseq\_2 X1 \\
& \quad k1\_numbers (k1\_euclid\ np\_3)) \Rightarrow (\forall X2.(m1\_rcomp\_1 X2 (k1\_seq\_1 \\
& \quad (k1\_pdiff\_1\ np\_2\ np\_3) X1)) \Rightarrow (((r2\_pdiff\_5 X0 X1) \wedge (r1\_tarski \\
& \quad X2 (k1\_relset\_1 k1\_numbers (k1\_pdiff\_2\ np\_3\ np\_2 (k1\_pdiff\_3 \\
& \quad np\_1\ np\_3 X0) X1)))) \Rightarrow (\forall X3.((v2\_relat\_1 X3) \wedge ((v1\_funct\_1 \\
& X3) \wedge ((v1\_funct\_2 X3 k5\_numbers k1\_numbers) \wedge ((v1\_fdiff\_1 X3 k6\_numbers) \wedge \\
& (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\
& \quad (\forall X4.((v1\_funct\_1 X4) \wedge ((v3\_funct\_1 X4) \wedge ((v1\_funct\_2 \\
& X4 k5\_numbers k1\_numbers) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& k5\_numbers k1\_numbers)))))) \Rightarrow (((k2\_relset\_1 k1\_numbers X4 = k1\_tarski \\
& \quad (k1\_seq\_1 (k1\_pdiff\_1\ np\_2\ np\_3) X1)) \wedge (r1\_tarski (k2\_relset\_1 \\
& k1\_numbers (k3\_valued\_1 k5\_numbers k1\_numbers k1\_numbers X3 X4)) \\
& X2)) \Rightarrow ((v2\_comseq\_2 (k20\_valued\_1 k5\_numbers k1\_numbers k1\_numbers \\
& \quad (k37\_valued\_1 k5\_numbers k1\_numbers X3) (k47\_valued\_1 k5\_numbers \\
& k1\_numbers k1\_numbers (k8\_funct\_2 k5\_numbers k1\_numbers k1\_numbers \\
& \quad (k3\_valued\_1 k5\_numbers k1\_numbers k1\_numbers X3 X4) (k1\_pdiff\_2 \\
& \quad np\_3\ np\_2 (k1\_pdiff\_3\ np\_1\ np\_3 X0) X1)) (k8\_funct\_2 k5\_numbers \\
& \quad k1\_numbers k1\_numbers X4 (k1\_pdiff\_2\ np\_3\ np\_2 (k1\_pdiff\_3\ np\_1 \\
& \quad np\_3 X0) X1)))))) \wedge (k2\_pdiff\_5 X0 X1 = k2\_seq\_2 (k20\_valued\_1 k5\_numbers \\
& \quad k1\_numbers k1\_numbers (k37\_valued\_1 k5\_numbers k1\_numbers X3) \\
& \quad (k47\_valued\_1 k5\_numbers k1\_numbers k1\_numbers (k8\_funct\_2 k5\_numbers \\
& k1\_numbers k1\_numbers (k3\_valued\_1 k5\_numbers k1\_numbers k1\_numbers \\
& \quad X3 X4) (k1\_pdiff\_2\ np\_3\ np\_2 (k1\_pdiff\_3\ np\_1\ np\_3 X0) X1)) ( \\
& \quad k8\_funct\_2 k5\_numbers k1\_numbers k1\_numbers X4 (k1\_pdiff\_2\ np\_3 \\
& \quad np\_2 (k1\_pdiff\_3\ np\_1\ np\_3 X0) X1)))))))))
\end{aligned}$$