

## t39\_group\_7

(TMZX6hVhqmZBnWDwJE2pBJUPVR3DkySt4gf)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_group\_1 : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $l3\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $r1\_group\_6 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_group\_7 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k9\_finseq\_1 : \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_group\_6 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_group\_7 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_finseq\_1 : \iota \Rightarrow \iota$  be given. Let  $v2\_group\_7 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_group\_7 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v3\_group\_7 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v15\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v1\_monoid\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge ((v3\_group\_1 \\
 & X0) \wedge (l3\_algstr\_0 X0)))) \Rightarrow (\forall X1. ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 \\
 & X1 (u1\_struct\_0 X0) (u1\_struct\_0 (k2\_group\_7 (k1\_tarski np\_1) \\
 & (k9\_finseq\_1 X0)))) \wedge ((v1\_group\_6 X1 X0 (k2\_group\_7 (k1\_tarski \\
 & np\_1) (k9\_finseq\_1 X0))) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
 & (u1\_struct\_0 X0) (u1\_struct\_0 (k2\_group\_7 (k1\_tarski np\_1) ( \\
 & k9\_finseq\_1 X0)))))))))) \Rightarrow ((\forall X2. (m1\_subset\_1 X2 (u1\_struct\_0 \\
 & X0)) \Rightarrow (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 (k2\_group\_7 ( \\
 & k1\_tarski np\_1) (k9\_finseq\_1 X0))) X1 X2 = k4\_group\_7 X0 X2)) \Rightarrow ( \\
 & v3\_funct\_2 X1 (u1\_struct\_0 X0) (u1\_struct\_0 (k2\_group\_7 (k1\_tarski \\
 & np\_1) (k9\_finseq\_1 X0))))))
 \end{aligned}
 \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge ((v3\_group\_1 \\
& X0) \wedge (l3\_algstr\_0 X0)))) \Rightarrow (\forall X1.((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 \\
& X1 (u1\_struct\_0 X0) (u1\_struct\_0 (k2\_group\_7 (k1\_tarski np\_1) \\
& (k9\_finseq\_1 X0)))) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 (k2\_group\_7 (k1\_tarski np\_1) ( \\
& k9\_finseq\_1 X0)))))) \Rightarrow ((\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\
& X0)) \Rightarrow (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 (k2\_group\_7 ( \\
& k1\_tarski np\_1) (k9\_finseq\_1 X0))) X1 X2 = k4\_group\_7 X0 X2)) \Rightarrow ( \\
& (v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& (k2\_group\_7 (k1\_tarski np\_1) (k9\_finseq\_1 X0)))) \wedge ((v1\_group\_6 \\
& X1 X0 (k2\_group\_7 (k1\_tarski np\_1) (k9\_finseq\_1 X0))) \wedge (m1\_subset\_1 \\
& X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 (k2\_group\_7 \\
& (k1\_tarski np\_1) (k9\_finseq\_1 X0))))))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0 : \iota \Rightarrow \iota. \forall X1. \forall X2. \exists X3. ((v1\_funct\_1 \\
& X3) \wedge ((v1\_funct\_2 X3 X2 X1) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& X2 X1)))) \wedge (\forall X4.(m1\_subset\_1 X4 X2) \Rightarrow (k3\_funct\_2 X2 X1 X3 \\
& X4 = X0 X4))
\end{aligned} \tag{3}$$

Assume the following.

$$\forall X0. k9\_finseq\_1 X0 = k5\_finseq\_1 X0 \tag{4}$$

Assume the following.

$$\forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge (l3\_algstr\_0 X0))) \Rightarrow (v2\_group\_7 (k5\_finseq\_1 X0) (k1\_tarski np\_1)) \tag{5}$$

Assume the following.

$$\forall X0. ((\neg v2\_struct\_0 X0) \wedge (l3\_algstr\_0 X0)) \Rightarrow ((v1\_partfun1 (k5\_finseq\_1 X0) (k1\_tarski np\_1)) \wedge (v1\_group\_7 (k5\_finseq\_1 X0))) \tag{6}$$

Assume the following.

$$\forall X0. ((\neg v2\_struct\_0 X0) \wedge (l3\_algstr\_0 X0)) \Rightarrow (v4\_relat\_1 (k5\_finseq\_1 X0) (k1\_tarski np\_1)) \tag{7}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge ( \\
& (v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge ((v1\_group\_7 X1) \wedge (v3\_group\_7 \\
& X1 X0)))))) \Rightarrow ((v15\_algstr\_0 (k2\_group\_7 X0 X1)) \wedge (v3\_group\_1 ( \\
& k2\_group\_7 X0 X1)))
\end{aligned} \tag{8}$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge \\ (v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge ((v1\_group\_7 X1) \wedge (v2\_group\_7 \\ X1 X0)))))) \Rightarrow ((v15\_algstr\_0 (k2\_group\_7 X0 X1)) \wedge (v2\_group\_1 ( \\ k2\_group\_7 X0 X1))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge \\ (v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge (v1\_group\_7 X1)))) \Rightarrow (( \\ \neg v2\_struct\_0 (k2\_group\_7 X0 X1)) \wedge ((v15\_algstr\_0 (k2\_group\_7 \\ X0 X1)) \wedge (v1\_monoid\_0 (k2\_group\_7 X0 X1)))) \end{aligned} \quad (10)$$

Assume the following.

$$\forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v3\_group\_1 X0) \wedge (l3\_algstr\_0 \\ X0))) \Rightarrow (v3\_group\_7 (k5\_finseq\_1 X0) (k1\_tarski\_np\_1)) \quad (11)$$

Assume the following.

$$\forall X0. (v1\_relat\_1 (k9\_finseq\_1 X0)) \wedge (v1\_funct\_1 (k9\_finseq\_1 \\ X0)) \quad (12)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge \\ (v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge (v1\_group\_7 X1)))) \Rightarrow (( \\ v15\_algstr\_0 (k2\_group\_7 X0 X1)) \wedge (l3\_algstr\_0 (k2\_group\_7 X0 \\ X1))) \end{aligned} \quad (13)$$

Assume the following.

$$\begin{aligned} \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge ((v3\_group\_1 \\ X0) \wedge (l3\_algstr\_0 X0)))) \Rightarrow (\forall X1. ((\neg v2\_struct\_0 X1) \wedge ((v2\_group\_1 \\ X1) \wedge ((v3\_group\_1 X1) \wedge (l3\_algstr\_0 X1)))) \Rightarrow ((r1\_group\_6 X0 X1) \Leftrightarrow \\ (\exists X2. ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (u1\_struct\_0 X0) \\ (u1\_struct\_0 X1)) \wedge ((v1\_group\_6 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X1)))))) \wedge (v3\_funct\_2 \\ X2 (u1\_struct\_0 X0) (u1\_struct\_0 X1)))))) \end{aligned} \quad (14)$$

**Theorem 1**

$$\forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge ((v3\_group\_1 \\ X0) \wedge (l3\_algstr\_0 X0)))) \Rightarrow (r1\_group\_6 X0 (k2\_group\_7 (k1\_tarski \\ np\_1) (k9\_finseq\_1 X0)))$$