

# t39\_msualg\_2 (TM- Rcz6JmAWxnWGiS6KcYAgAgPbo3FizwMte)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_msualg\_1 : \iota \Rightarrow o$  be given. Let  $l3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m3\_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $u3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_msualg\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_msualg\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_setfam\_1 : \iota \Rightarrow \iota$  be given. Let  $k3\_card\_3 : \iota \Rightarrow \iota$  be given. Let  $v3\_msualg\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_msualg\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. (r1\_tarski X0 X1) \Leftrightarrow (\forall X2. (X2 \in X0) \Rightarrow (X2 \in X1)) \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge (l1\_msualg\_1 \\ & X0))) \Rightarrow (\forall X1. (l3\_msualg\_1 X1 X0) \Rightarrow (\forall X2. (X2 = k6\_msualg\_2 \\ & X0 X1) \Leftrightarrow (\forall X3. (X3 \in X2) \Leftrightarrow ((X3 \in k9\_funct\_2 (u1\_struct\_0 X0) \\ & (k9\_setfam\_1 (k3\_card\_3 (u3\_msualg\_1 X0 X1)))) \wedge ((m3\_pboole X3 \\ & (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1)) \wedge (\forall X4. (m3\_pboole \\ & X4 (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1)) \Rightarrow ((X4 = X3) \Rightarrow (v3\_msualg\_2 \\ & X4 X0 X1)))))))))) \quad (2) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge (l1\_msualg\_1 \\ & X0))) \Rightarrow (\forall X1. (l3\_msualg\_1 X1 X0) \Rightarrow (\forall X2. (m3\_pboole \\ & X2 (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1)) \Rightarrow (\forall X3. (X3 = k5\_msualg\_2 \\ & X0 X1 X2) \Leftrightarrow (\forall X4. (X4 \in X3) \Leftrightarrow ((X4 \in k9\_funct\_2 (u1\_struct\_0 X0) \\ & (k9\_setfam\_1 (k3\_card\_3 (u3\_msualg\_1 X0 X1)))) \wedge ((m3\_pboole X4 \\ & (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1)) \wedge (\forall X5. (m3\_pboole \\ & X5 (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1)) \Rightarrow ((X5 = X4) \Rightarrow ((v3\_msualg\_2 \\ & X5 X0 X1) \wedge ((r2\_pboole (u1\_struct\_0 X0) (k2\_msualg\_2 X0 X1) X5) \wedge \\ & (r2\_pboole (u1\_struct\_0 X0) X2 X5)))))))))) \quad (3) \end{aligned}$$

**Theorem 1**

$$\forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge (l1\_msualg\_1 X0))) \Rightarrow (\forall X1. (l3\_msualg\_1 X1 X0) \Rightarrow (\forall X2. (m3\_pboole X2 (u1\_struct\_0 X0) (u3\_msualg\_1 X0 X1)) \Rightarrow (r1\_tarski (k5\_msualg\_2 X0 X1 X2) (k6\_msualg\_2 X0 X1))))))$$