

t39\_qc\_lang3 (TM-  
FCs7G8SV6ugbA8zCbnZJXGX5H7T6wXh9U)

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Let  $m1\_qc\_lang1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k9\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Let  $k4\_qc\_lang3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k13\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k12\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $v2\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_qc\_lang3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k17\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k18\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v4\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k19\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k20\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v5\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k22\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\forall X1.((\neg v1\_xboole\_0 X1) \wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_qc\_lang1 X0)))) \Rightarrow ((k4\_qc\_lang3 \\ & X0 X1 (k12\_qc\_lang1 X0) = k1\_xboole\_0) \wedge ((\forall X2.(m1\_subset\_1 \\ & X2 (k9\_qc\_lang1 X0)) \Rightarrow ((v2\_qc\_lang1 X2 X0) \Rightarrow (k4\_qc\_lang3 X0 X1 X2 = \\ & k1\_qc\_lang3 X0 (k17\_qc\_lang1 X0 X2) X1)))) \wedge ((\forall X2.(m1\_subset\_1 \\ & X2 (k9\_qc\_lang1 X0)) \Rightarrow ((v3\_qc\_lang1 X2 X0) \Rightarrow (k4\_qc\_lang3 X0 X1 X2 = \\ & k4\_qc\_lang3 X0 X1 (k18\_qc\_lang1 X0 X2)))) \wedge ((\forall X2.(m1\_subset\_1 \\ & X2 (k9\_qc\_lang1 X0)) \Rightarrow ((v4\_qc\_lang1 X2 X0) \Rightarrow (k4\_qc\_lang3 X0 X1 X2 = \\ & k4\_subset\_1 X1 (k4\_qc\_lang3 X0 X1 (k19\_qc\_lang1 X0 X2)) (k4\_qc\_lang3 \\ & X0 X1 (k20\_qc\_lang1 X0 X2)))) \wedge (\forall X2.(m1\_subset\_1 X2 (k9\_qc\_lang1 \\ & X0)) \Rightarrow ((v5\_qc\_lang1 X2 X0) \Rightarrow (k4\_qc\_lang3 X0 X1 X2 = k4\_qc\_lang3 X0 \\ & X1 (k22\_qc\_lang1 X0 X2)))))))))) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0.\forall X1.((m1\_qc\_lang1 X0) \wedge (m1\_subset\_1 X1 (k9\_qc\_lang1 X0))) \Rightarrow (m1\_subset\_1 (k13\_qc\_lang1 X0 X1) (k9\_qc\_lang1 X0)) \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.(m1\_qc\_lang1 X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k9\_qc\_lang1 \\ & X0)) \Rightarrow ((v3\_qc\_lang1 X1 X0) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k9\_qc\_lang1 \\ & X0)) \Rightarrow ((X2 = k18\_qc\_lang1 X0 X1) \Leftrightarrow (X1 = k13\_qc\_lang1 X0 X2)))))) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_qc\_lang1\ X0) \Rightarrow (\forall X1.(m1\_subset\_1\ X1\ (k9\_qc\_lang1 \\ X0)) \Rightarrow ((v3\_qc\_lang1\ X1\ X0) \Leftrightarrow (\exists X2.(m1\_subset\_1\ X2\ (k9\_qc\_lang1 \\ X0)) \wedge (X1 = k13\_qc\_lang1\ X0\ X2)))) \end{aligned} \quad (4)$$

**Theorem 1**

$$\begin{aligned} \forall X0.(m1\_qc\_lang1\ X0) \Rightarrow (\forall X1.(m1\_subset\_1\ X1\ (k9\_qc\_lang1 \\ X0)) \Rightarrow (\forall X2.((\neg v1\_xboole\_0\ X2) \wedge (m1\_subset\_1\ X2\ (k1\_zfmisc\_1 \\ (k2\_qc\_lang1\ X0)))) \Rightarrow (k4\_qc\_lang3\ X0\ X2\ (k13\_qc\_lang1\ X0\ X1) = k4\_qc\_lang3 \\ X0\ X2\ X1))) \end{aligned}$$